# Model-Based Calibration Toolbox 

For Use with MATLAB ${ }^{\circledR}$ and Simulink ${ }^{\circledR}$

Computation

- Visualization
- Programming

Simulation

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## Model-Based Calibration Toolbox CAGE User's Guide

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## Getting Started

This section includes the following topics:

| What Is CAGE? (p. 1-2) | Introducing the CAGE browser <br> part of the Model-Based Calibration <br> Toolbox. You can use CAGE to <br> calibrate lookup tables using <br> models and data. You can trade off <br> competing objectives, and validate <br> calibrations against data. |
| :--- | :--- |
| Nowigating CAGE (p. 1-4) | How to find your way around CAGE <br> and navigate between processes, <br> tables, data, variables, and models. |
| How to Use This Manual (p. 1-9) | How to find information in this |
|  | User's Guide, with links to reference <br> chapters for all CAGE functionality. |

## What Is CAGE?

CAGE (CAlibration GEneration) is an easy-to-use graphical interface for calibrating lookup tables for your electronic control unit (ECU).

As engines get more complicated, and models of engine behavior more intricate, it is increasingly difficult to rely on intuition alone to calibrate lookup tables. CAGE provides analytical methods for calibrating lookup tables.

CAGE uses models of the engine control subsystems to calibrate lookup tables. With CAGE you fill and optimize lookup tables in existing ECU software using models from the Model Browser part of the Model-Based Calibration Toolbox. From these models, CAGE builds steady-state ECU calibrations.

CAGE also compares lookup tables directly to experimental data for validation.

## Feature Calibration

A feature calibration compares a model of an estimated signal with a lookup table (or algebraic collection of tables) that estimates the same signal in the ECU. CAGE finds the optimum calibration for the lookup table(s).

For example, a typical engine subsystem controls the spark angle to produce the peak torque; that is, the Maximum Brake Torque (MBT) spark. Using the Model Browser, you can build a statistically sound model of MBT spark, over a range of engine speeds and relative air charges, or loads. Use the feature calibration to fill a lookup table by comparing the table to the model.

## Tradeoff Calibration

A tradeoff calibration fills lookup tables by comparing models of different engine characteristics at key operating points.

For example, there are several models of important engine characteristics, such as torque and nitrous oxides (NOX) emissions. Both models depend on the spark angle. At a particular operating point, a slight reduction of torque can result in a dramatic reduction of NOX emissions. Thus, the calibrator
uses the value of the spark angle that gives this reduction in NOX emissions instead of the spark angle that generates maximum torque.

## Optimization

CAGE can optimize calibrations with reference to models, including single- and multi-objective optimizations, sum optimizations, user-defined optimizations, and automated tradeoff.

## Comparing Calibrations to Data

You can compare your calibrations to experimental data for validation.
For example, after completing a calibration, you can import experimental data from a spreadsheet. You can use CAGE to compare your calibration to the data.

## Starting the CAGE Browser

To start the application, type
cage
at the MATLAB ${ }^{\circledR}$ command prompt.

## Navigating CAGE

The view of CAGE depends on two things:

- Which button you select in the Processes and Data Objects panes
- The item you highlight in the tree display

When you open CAGE, it looks like this.


CAGE includes a Processes pane and a Data Objects pane to help you identify the type of calibration you want to do and the data objects that
you intend to use. Use the buttons in these panes to navigate between the different sections of functionality in CAGE.

## CAGE Views and Processes

The Processes pane has three buttons:

- Feature shows the Feature view, with the tables and strategies that are associated with that feature. See "Feature View" on page 4-41.

A feature is a strategy (or collection of tables) and a model used to calibrate those tables. In the Feature view, you can fill tables by comparing a strategy to a model. See Chapter 4, "Feature Calibrations". You can import existing strategies or construct new ones using Simulink ${ }^{\circledR}$ from the feature view.

From the feature node in the tree display, you can access the Surface Viewer to examine the strategy or model or both. See Chapter 8, "Surface Viewer".

- Tradeoff shows the Tradeoff view, with a list of the tables and models to display. Here you can see graphically the effects of manually altering variables to trade off different objectives (such as maximizing torque while minimizing emissions). At the tradeoff node, you can calibrate table values to achieve the best compromise between competing objectives. You can calibrate using single or multimodel tradeoffs. See Chapter 5, "Tradeoff Calibrations". You can also use the optimization functionality of CAGE to run automated tradeoffs, described in the Optimization section (see below).
- Optimization shows the Optimization view. From here you can set up and run optimizations, including automated tradeoffs. There are standard routines available and also templates provided so you can write your own optimization routines. You can find full instructions in Chapter 6, "Optimization".

You can reach the Calibration Manager from the Feature and Tradeoff process views, and from the Tables view, but not Optimization. In the Calibration Manager you can set up the size and contents of tables (manually or using existing calibration files) and edit the precision used for values (to match the kind of electronic control unit you are going to use). See "Calibration Manager" on page 3-20.


The Data Objects pane has four buttons:

- Variable Dictionary stores all the variables, constants, and formulas in your session. Here you can view, add, and edit any variables in any part of your session. See "Setting Up Variable Items" on page 2-3.
- Tables enables you to see all the tables and normalizers in your session. You can also calibrate tables manually here if you want. You can add and delete tables from the project. From any table display (here, or in other views) you can access the History Display to manage changes in your tables and normalizers. You can use the History Display to reverse changes. See "Setting Up Tables" on page 3-3.
- Models stores all the models in your session. Here you can view a graphical display of these models, including a diagram of the model's input structure. This is useful because a model can have other models as inputs. You can change the inputs here. For example, you can change your model's input Spark to be connected to a model for Spark rather than to the variable Spark. You can also access the surface viewer here to examine models. See "Setting Up Models" on page 2-11 and Chapter 8, "Surface Viewer".
- Data Sets enables you to evaluate your models and features over a custom set of input values. Here you can create and edit a set of input values and view several models or features evaluated at these points. You can compare your tables and models with experimental data to validate your calibrations. You can also fill tables directly from experimental data by
loading the experimental data as a new data set. See Chapter 7, "Data Sets".



## How to Use This Manual

This manual is the CAGE User's Guide. See also the Model Browser User's Guide for information on the other main interface of the Model-Based Calibration Toolbox.

## Learning CAGE

See the Getting Started guide for tutorials and case studies.

## Using CAGE

- Chapter 2, "Variables and Models" describes how to set up CAGE sessions before performing calibrations and gives an overview of where in CAGE to find all the functionality for different processes.
- Chapter 3, "Tables" describes how to create and use tables and normalizers, including using the Calibration Manager and History Viewer.
- Chapter 4, "Feature Calibrations" describes how to calibrate lookup tables by reference to models built using the model browser.
- Chapter 5, "Tradeoff Calibrations" describes how to calibrate lookup tables by adjusting many values to fulfill different objectives.
- Chapter 6, "Optimization" describes how to use the optimization functions, including automated tradeoffs, and describes all the functions available for user-defined optimizations.
- Chapter 7, "Data Sets" describes how to use CAGE to compare calibrations to experimental data, and how to use experimental data to fill lookup tables.
- Chapter 8, "Surface Viewer" describes how to use the Surface Viewer.


## Variables and Models

The following sections describe how to set up variables and models before performing calibrations.

Setting Up Variable Items (p. 2-3)

Setting Up Models (p. 2-11)

Model Properties (p. 2-20)

Before you can perform a calibration using CAGE, you need to set up the variables and constants you want to use. This section describes how to use the Variable Dictionary view to create, import, edit, and export variables and constants.

Before you can perform a calibration using CAGE, you need to set up the models you want to use. This section describes how to use the Model view to import and rename models, edit model inputs, and create new function models.

Use the Model Properties dialog to switch model output between model values and boundary or PEV values, and view information such as the model type, definition, inputs, creation date, user name, and toolbox version.

CAGE Import Tool (p. 2-24)

This section describes how to use the CAGE Import Tool to get models and other items from any Model-Based Calibration Toolbox project file produced in CAGE or the Model Browser. You can use this to replace existing items in your CAGE project.

Specifying Locations of Files (p. 2-27) How to use file preferences in CAGE.

## Setting Up Variable Items

The Variable Dictionary is a store for all the variables, constants, and formulae in your session.

To view or edit the items in the Variable Dictionary, click the button, shown, in the Data Objects pane.


Selecting the Variable Dictionary view displays the variables, constants, and formulae in the current project.

This section describes the following:

- "Importing and Exporting a Variable Dictionary" on page 2-5
- "Adding and Editing Variable Items" on page 2-6
- "Using the Variable Menu" on page 2-8
- "Using Aliases" on page 2-9

Note that if you have existing CAGE projects you can use the "CAGE Import Tool" on page 2-24 to import variable items and other CAGE items directly from other projects.

Following is an example of the Variable Dictionary view.
List of all the constants, variables, and formulas in the project


Edit boxes to change the settings of the selected constant, variable, or formula

The upper pane shows a list of all the current variables, constants, and formulas. The lower pane displays edit boxes so you can specify the settings of the selected variable, constant, or formula.

## Different Variable Dictionary Items

- Variables - standard items that feed into models, strategies and tables, and define ranges for these items
- Constant - used for inputs that you do not want to change
- Formulae - used when you want a variable item to depend on another


## Importing and Exporting a Variable Dictionary

A variable dictionary contains all the variable items for your calibrations. You can set up your variable dictionary once, and use it in many calibrations.

If you import a model, it has variables associated with it, in which case you might not have to import a variable dictionary.

## Importing a Variable Dictionary

To import a dictionary of variables from an .xml file,

## 1 Select File > Import > Variable Dictionary.

2 Select the correct dictionary file.
Note you can also import variable items directly from other CAGE projects using the "CAGE Import Tool" on page 2-24.

## Exporting a Variable Dictionary

After setting up a variable dictionary, you can save the dictionary for use in many different calibrations.

To export a dictionary of variables to an .xml file,
1 Select File > Export > Variable Dictionary.
2 Select a suitable name for the dictionary file.

## See Also

- "Setting Up Variable Items" on page 2-3
- "Adding and Editing Variable Items" on page 2-6


## Adding and Editing Variable Items

To add variable items you can use the Variable Dictionary toolbar, shown, or you can select items from the File -> New -> Variable Items menu.

## Variable Dictionary Toolbar



## Adding a Variable

To add a variable,

$$
\text { I Select File }>\text { New }>\text { Variable Item }>\text { Variable. }
$$

A new variable is added to the variable dictionary.
2 Select Edit > Rename to alter the name of the variable.
3 Specify the Minimum and Maximum values of the variable in the edit boxes in the lower pane.

4 Specify the value of the Set Point in the edit box.
Using Set Points in the Variable Dictionary. The set point of a variable is a point that is of particular interest in the range of the variable. You can edit set points in the variable dictionary or the models view.

For example, for the air/fuel ratio variable, AFR, the range of values is typically 11 to 17 . However, whenever only one value of AFR is required, it is preferable to choose 14.3 , the stoichiometric constant, over any other value. So enter 14.3 as the Set Point.

CAGE uses the set point as the default value of the variable wherever one value from the variable range is required. For instance, CAGE uses the set point when evaluating a model over the range of a different variable.

For example, a simple model for torque depends on AFR, engine speed, and relative air charge. CAGE uses the set point of AFR when it calculates the values of the model over the ranges of the engine speed and relative air charge.

## Adding a Constant

To add a constant,
1 Select File > New > Variable Item > Constant.
A new constant is added to the variable dictionary.
2 Select Edit > Rename to alter the name of the constant.
3 Specify the value of the constant in the Set Point edit box, in the lower pane.

## Adding Formulas

You might want to add a formula to your session. For example, the formula
where afr is the air/fuel ratio and stoich is the stoichiometric constant.
To add a formula,

## 1 Select File > New > Variable Item > Formula.

The Add Formula dialog box appears.
2 In the dialog, enter the right side of the formula, as in this example $\mathrm{afr} / \mathrm{stoich}$. Note it is normal to create inputs to a formula first. If you do not use pre-existing variable names then those inputs are created, so be careful to get input names exactly correct. Follow these requirements for a valid formula string:

- A formula can only have exactly one variable input
- No formulae as inputs
- Not circular (i.e. self referencing)
- Must not error when evaluated
- Must produce a vector for a vector input
- Must be invertible

Click OK and a new formula is added to the variable dictionary.
3 Select Edit -> Rename to alter the name of the formula.

## See Also

- "Setting Up Variable Items" on page 2-3
- "Adding and Editing Variable Items" on page 2-6


## Using the Variable Menu

The Variable menu in the variable dictionary enables you to alter variable items. These choices are also available in the right-click context menu on the list view.

Change item to:

## - Alias

Changes the selected item to be an alias of another item in the current project. For example, if you have two variables, engine_speed and n, you can change $n$ to be an alias of engine_speed, with its maximum and minimum values. For more information, see the next section, "Using Aliases" on page 2-9.

## - Formula

Changes a variable or constant into a formula. You have to define the right side of the formula, and you can select the check box to calculate the range.

- Constant

Changes a variable or formula into a constant. The value of the constant is the set point of the old item.

- Variable

Changes a constant or formula into a variable. The range is from 0 to twice the constant's value (negative values have a maximum of 0 ).

## See Also.

- "Setting Up Variable Items" on page 2-3
- "Using Aliases" on page 2-9


## Using Aliases

The variable dictionary enables you to use the same set of variables, constants, and formulas with many different models and calibrations.

## Why Use Aliases?

It is possible that in one model or strategy the engine speed has been defined as N , and in another it has been defined as rpm. The alias function enables you to automatically link inputs with various names to a single CAGE variable when you import models and strategies.

## Creating an Alias

For example, in a variable dictionary there are two variables:

- $N$, with a range of 500 to 6500
- rpm, with a range of 2500 to 3500

To set rpm to be an alias of N ,
1 Highlight the variable rpm.
2 Select Variable > Change item to > Alias.
3 In the dialog, choose N from the list.
This eliminates the variable rpm from your variable dictionary, and every model and calibration that refers to rpm now refers to N instead.

Note If $N$ is made an alias of rpm in the preceding example, the range of N is restricted to the range of rpm, 2500 to 3500.

You can also add aliases to existing items by entering a list of names in the Alias edit box.

## See Also

- "Setting Up Variable Items" on page 2-3


## Setting Up Models

CAGE generally calibrates lookup tables by reference to models. The Models view is a storage place for all the models in your session.

To view and edit the models in your session, select Models by clicking the button shown in the Data Objects pane.


This section describes the following:

- "Importing Models" on page 2-13
- "Adding New Function Models" on page 2-15
- "Renaming and Editing Models" on page 2-17

The Models view displays the following:

- A list of all the models in the current project.
- The model connections. That is, which constants, variables, and models are inputs to the selected model. You can use the View menu or the right-click context menu on the graph to zoom in and out, zoom to fit, and reset.
- An image of the response surface of the selected model; you can select factors to display. Use the View menu to choose between:
- No Constraint Display - Shows entire model surface.
- Show Constraint - Areas outside the boundary constraint model (if any) are yellow.
- Clip to Constraint - The surface is only shown within the boundary constraint model.

View > Edit Input Set Points opens a dialog box where you can edit the set points of your model variables. This setting alters the model display and also any calculations involving the set points throughout CAGE. Altering this setting is the same as altering the set points in the Variable Dictionary, see "Using Set Points in the Variable Dictionary" on page 2-6.

Following is an example of the Models display.
List of the current models


The icons in the Models list indicate the type of model, as listed in the Type column. As shown in the following illustration, a model can be a Model Browser statistical model, the boundary of a model, the prediction error variance (PEV) of a model, a user-defined function model, or a feature model (converted from a feature).

You can use the "Model Properties" on page 2-20 dialog to switch a model output between the model value and the boundary or PEV of the model. For function models see "Adding New Function Models" on page 2-15. You can convert a feature to a model by selecting Feature > Convert to Model.

## Importing Models

CAGE enables you to calibrate lookup tables by referring to models constructed in the Model Browser.

CAGE can only open Model-Based Calibration Toolbox model files. You can import models from project files (.mat, . cag) and from exported model files (.exm).

## Import Models From Project

You can use the CAGE Import Tool to select models to import from any Model-Based Calibration Toolbox project file produced in CAGE or the Model Browser (.mat or .cag). You can replace suitable models in your current CAGE project (note that Model Browser models must have exactly the same input names as the CAGE model you are replacing).

See "CAGE Import Tool" on page 2-24 for instructions.

## Import Exported Models File

To import models from a Model Browser exported models file (.exm):

## 1 Select File > Import > Model.

2 A file browser dialog opens. Locate the desired file or files. You can select multiple files. Examples can be found in matlab/toolbox/mbc/mbctraining.
a If the model is saved as an .exm file, select MBC Model (*.exm) from the drop-down menu.
b If the model is not saved as an .exm file, select All files (*.*) from the Files of type drop-down menu. For example, the file extension might be accidentally changed.

Click to select the model file then click Open .
This opens the Model Import Wizard.
3 Select the models that you want to import by highlighting the models from the list, or click Select All if you want every model.

4 Either:

- Select the check box Automatically assign/create inputs, then you can click Finish.
- Alternatively if you do not want to automatically assign or create inputs, instead click Next to match these up manually.

5 Associate the model factors with the available inputs in your session.
For example, to associate the model factor spark with the variable spk in your session,

a Highlight a model factor, spark, in the list on the left and the corresponding variable, SPK, in the list on the right.
b Click the select input button, shown.

c Repeat 5 a and 5 b for all the model factors.
6 Click Finish to close the wizard and return you to the Models view.

Note You can skip steps 5 and 6 by selecting the Automatically assign/create inputs box at step 6 .

You can now see a display of the model surface and the model connections (inputs).

## See Also

- "Setting Up Models" on page 2-11
- "Adding New Function Models" on page 2-15
- "Renaming and Editing Models" on page 2-17


## Adding New Function Models

A function model is a model that is expressed algebraically. The function can be any MATLAB function (including user-defined functions). The only restriction is that the function must be vectorized, that is, take in column vectors and return a column vector of the same size, as in this example:

```
function y = foo(x1, x2)
y = x1 .* x2;
```

Once you have a function like this, you can create a function model applying it to any models or variables in your session, like the following example.

```
foo(NOX, SPK)
```

For example, you might want to view the behavior of torque efficiency. So you create a function model of torque efficiency $=$ torque/peak torque.

To add a function model to your session,

## 1 Select File $>$ New $>$ Function Model.

This opens the Function Model Wizard.
2 In the dialog box, enter the formula for your function model. For example, enter torque_efficiency=torque/peak_torque.

3 Press Enter. CAGE checks that the function is recognized; if so, you can click Next. If the function is incorrectly entered, you cannot click Next.

4 Select the models that you want to import by highlighting the models from the list.

## 5 Click Next.



6 You can select the check box to Automatically assign/create inputs and click Finish to close the wizard and return you to the Models view, or you
can click Next and go to the next screen. Here you can manually associate the model factors with the available inputs as follows:
a Highlight a model factor, e.g. peak_torque, in the list on the left and the corresponding model, peak_torque, in the list on the right.
b Click the select input button, shown.


Repeat a and b for all the model factors. Click Finish to close the wizard and return you to the Models view.

You can now see a display of the model and its connections (inputs).

## See Also

- "Setting Up Models" on page 2-11
- "Importing Models" on page 2-13
- "Renaming and Editing Models" on page 2-17


## Renaming and Editing Models

## Renaming Models

To rename a model,
1 Highlight the model that you want to rename.
2 Select Edit > Rename.
3 Enter the new name for the model and press Enter.
You can also rename the model by selecting a model and clicking the name, or pressing F2.

## Editing Model Inputs

You can adjust a model so that variables, formulas, or other models are the factors of the model. For example, a model of torque depends on the spark angle. In place of the spark angle variable, you can use a model of the maximum brake torque (MBT) as the spark input.

To edit the inputs of a model,
1 Highlight the model.
2 Select Model > Edit Inputs.
This opens the Edit Inputs dialog box, shown.


3 Highlight the model factor that you want to adjust, in the list on the left.
4 Highlight the new input for that factor, in the list on the right.
5 Click the Select Input button, shown.


6 To close the dialog box, click Finish.

Note If you want to change the range of a variable in the session, change the range in the variable dictionary. For more information, see "Using the Variable Menu" on page 2-8.

## Model Properties

Select Model > Properties (or right-click) to view information about the selected model. This opens the Model Properties dialog where you can see the model type, definition, inputs, availability of PEV and constraints, creation date, user name, and toolbox version on the following tabs:

- "Model Properties: General" on page 2-20
- "Model Properties: Inputs" on page 2-21
- "Model Properties: Model" on page 2-22
- "Model Properties: Information" on page 2-23


## Model Properties: General



Here you can see the model type (such as MBC model or function model), the number of inputs, and the availability of constraints and Prediction Error.

You can use the radio buttons to select the Output Quantity to be the

- Model Value
- Prediction error variance of model
- Boundary constraint of model

You can enter values in the Output saturation limits edit boxes to set bounds on the model output values.

## Model Properties: Inputs



Here you can view all the immediate inputs and variable dependencies of your model. For some models the two lists will be the same; in the example shown one of the inputs is another model (MBT) so the variable dependencies list also shows the variable inputs for that model. This information is shown graphically in the Connections pane.

## Model Properties: Model



Here you can view the model definition, the project file, and the model path. Function model definitions are shown here. For MBC models the model definition (showing the parameters and coefficients of the model formula) is the same information you would see in the Model Browser part of the toolbox when selecting View > Model Definition.

## Model Properties: Information



Here you can see the user name associated with the model, the date of creation and the version number of the Model-Based Calibration Toolbox used to create the model. If you added any comments to the export information in the Model Browser Export Models dialog this information also appears here.

## CAGE Import Tool

You can use the CAGE Import Tool to select items to import from any Model-Based Calibration Toolbox project file produced in CAGE or the Model Browser (.mat or .cag). This can greatly simplify setting up new projects, and also making changes to existing projects, for example to make use of new models in an existing optimization and calibration.

You can import Model Browser models from any project file or direct from the Model Browser when it is open. You can import the following CAGE items from any CAGE project: models (including feature and function models), variables, normalizers, tables, features, optimizations, datasets and tradeoffs.

You can replace suitable items in your current CAGE project with imported items. You can see if an item is replaceable in the Import dialog, where the Replace action becomes available.

Note that Model Browser models (but not CAGE models) must have exactly the same input names as the CAGE model you want to replace. You can replace models, variables, normalizers, tables and features. You cannot replace optimizations, datasets or tradeoffs. You cannot replace tables used in tradeoffs with tables of a different size.

To use the CAGE Import Tool:

## 1 Select File > Import > From Project.

The CAGE Import Tool appears.
2 You can choose a project file or import directly from the Model Browser if it is open. Use the toolbar buttons, or select File > Select Project File, or File > Import From Model Browser.

If you are choosing a project file, a file browser dialog opens. Locate the desired file and click Open.

3 The CAGE Import Tool displays the available items. Select the items you want to import from the list. Press Ctrl+A to select all items, or Ctrl+click or Shift+click to select multiple items in the list.


You can use the Find and Type controls to filter the item list:

- If you are importing from a Model Browser project you can select Response, Switch, Datum or Response Feature from the Type list to display a single model type only.
- If you are importing from a CAGE project you can select Variable, Model, Normalizer, Table, Feature, Optimization, Dataset, or Tradeoff from the CAGE items in the Type list. For models the Subtype column displays whether a model item is an MBC model, function model or feature model.
- Enter text in the Find edit box to find particular model names. You can also select the box to Match case

4 Click the Import Selected Items toolbar button ( ${ }^{\text {『 }}$ ) or select File > Import Selected Items.

5 The Import dialog opens displaying the items you selected for import.


- Double-click the CAGE Item Name column cells to edit item names.
- If it is not possible to replace items in the current CAGE session then Create new is displayed in the Action column. If it is possible to replace an item in the current CAGE session with an imported item, the Action column cell becomes a drop-down menu where you can select Replace or Create new. If an exact name match item is available to be replaced the Action drop-down menu automatically displays Replace. Change this to Create new if you do not want to replace the existing item.
- When replacing items, double-click the CAGE Item Name column cells to open a dialog to select the correct item to replace.
- Clear the View new item check box if you do not want CAGE to switch to the appropriate view for the top item in the import list when you dismiss the dialog. The CAGE Import Tool remains open either way.
- Click OK to import the items.

6 Click the Close button or select File > Close to close the CAGE Import Tool when you have finished importing items.

See also:

- "Importing and Exporting a Variable Dictionary" on page 2-5
- "Import Exported Models File" on page 2-13


## Specifying Locations of Files

You can specify preferred locations of project and data files, using File > Preferences.

Project files have the file extension .cag and store entire CAGE sessions.
Data files are the files that form part of the CAGE session. For example, the following is a list of some of the data files used in CAGE:

- Simulink diagrams (.mdl)
- Experimental data (.xls, .csv, or .mat)
- Variable dictionaries (.xml)
- Models (.exm)

To specify preferred locations for files,
1 Select File > Preferences. This opens the dialog box shown.


2 Enter the directory or directories where your CAGE files are stored.
Alternatively, click to browse for a directory. You can specify directories for projects, data files, model files and strategy files.

3 Click OK.

2 Variables and Models

## Tables

This section includes the following topics:

Setting Up Tables (p. 3-3)

Adding, Duplicating and Deleting Tables (p. 3-4)
Table View (p. 3-6)

Using the History Display (p. 3-16)

Calibration Manager (p. 3-20)

Table Properties (p. 3-24)

An overview of the functionality in the Tables view.

How to add, copy and remove tables.

How to view and edit tables, fill tables by extrapolation, and use the Table menu.

Comparing and reverting to previous versions.

The Calibration Manager dialog box enables you to manage the sizes, values, and precision of all items that can be calibrated. You can set these properties manually or from a calibration file. This section describes how to use the Calibration Manager to set up tables and copy table data from other sources.

How to change table properties to specific precision (floating-point, polynomial ratio fixed point, or lookup table fixed point) to suit your ECU.

About Normalizers (p. 3-30)

Normalizer View (p. 3-32)

Inverting a Table (p. 3-39)
Importing and Exporting Calibrations (p. 3-46)

What are normalizers? A normalizer is the axis of your lookup table. It is the same as the collection of the breakpoints in your table.

This section describes what you can see when you highlight a normalizer in the tree display: the input/output display, normalizer display, and breakpoint spacing display; and how to edit, lock and delete breakpoints.
How to use CAGE to invert tables.
How to export your calibrations.

## Setting Up Tables

Select the Tables view by clicking the Tables button. It opens automatically if you add a table using the File > New > Table menu items.


The Tables view lists all the tables and normalizers in the current CAGE session.

Here you can add or delete tables and normalizers, and you can calibrate them manually. Once you have added new tables here you can also fill them using experimental data by going to the Data Sets view.

The next sections cover:

- "Adding, Duplicating and Deleting Tables" on page 3-4
- "Using the History Display" on page 3-16
- "Calibration Manager" on page 3-20
- "About Normalizers" on page 3-30

You can use the History display (from any other table or normalizer view in CAGE) to view and reverse changes and revert to previous versions of your tables. Use the Calibration Manager to set up tables manually or from calibration files.

See also

- "Table View" on page 3-6 for information on using the table view functionality once you have added tables to your project


## Adding, Duplicating and Deleting Tables

To add or delete tables, you can first select the Tables view. CAGE automatically switches to this view if you add a table using the File > New menu items.

The Tables view lists all the tables and normalizers in the current CAGE session.

## Adding Tables

To add a table to a session,
1 Decide whether you want to add a one- or a two-dimensional table.
For example if you want to add a modifier table to account for the variation in exhaust gas recirculation, add a one-dimensional table (which has one input). If, however, you want to add a table with speed and load as its normalizer inputs, then add a two-dimensional table.

2 Select File > New > 1D Table or File > New > 2D Table as appropriate.
Adding new tables automatically switches you to the Tables view.
3 In the Table Setup dialog you can enter the table name, number of rows and columns and initial value, and select the input variable (or variables) from the drop-down menus.

4 Click OK to add the new table. CAGE automatically initializes the normalizers of the table by spacing the breakpoints evenly over the ranges of the selected input variables.

Note You can also select Tools > Calibration Manager to change the size of a table. For information, see "Setting Up Tables" on page 3-3.

You can rename tables by first selecting the table, then

- Press F2, or
- Select Edit > Rename.

You can manually calibrate by entering values in any table. You can also fill tables using experimental data or optimization output by going to the Data Sets view; see "Tutorial: Filling Tables from Data" in the Getting Started documentation.

## Duplicating Tables

To copy a table or a normalizer from a session,
1 Select the Tables view.
2 Highlight the required table or normalizer.
3 Select Edit > Duplicate table_name ('table_name' is the currently selected table).

See also "CAGE Import Tool" on page 2-24 to add existing tables from other CAGE project files.

## Deleting Tables

When you are calibrating a collection of tables using either Feature or Tradeoff calibrations, you cannot easily delete tables without affecting the entire calibration. When deleting items, you must delete from the highest level down. For example, you cannot delete a table that is part of a feature; you must delete the feature first.

To delete a table or a normalizer from a session,
1 Select Tables view.
2 Highlight the required table or normalizer.
3 Click . or press Delete; or select Edit > Delete table_name ('table_name' is the currently selected table).

## Table View

When you select a table in the tree (under feature or tables), you see the Table view. The following sections describe:

- "Viewing and Editing a Table" on page 3-8
- "Using the Graph of the Table" on page 3-10
- "Filling a Table by Extrapolation" on page 3-11
- "Table Menu" on page 3-12

Note For feature calibration (filling and optimizing table values by comparing a strategy and a model), see "Calibrating the Tables" on page 4-24.

In CAGE, a table is defined to be either a one-dimensional or a two-dimensional lookup table. One-dimensional tables are sometimes known as characteristic lines or functions. Two-dimensional tables are also known as characteristic maps or tables. CAGE regards them both as similar objects.

Each lookup table has either one or two axes associated with it. These axes are normalizers. See "About Normalizers" on page 3-30.

For example, a simple MBT feature has two tables:

- A two-dimensional table with speed and relative air charge as its normalizers
- A one-dimensional table with AFR as its normalizer

The example following is a feature view. In the Tables view for manual calibration, you do not see the lower comparison pane because you are not comparing tables with a model.

## Table Display in Feature Calibration



The parts of the display are numbered and labeled as follows:
1 The table displays the values of the breakpoints and the values of the table.

The table breakpoint values are not necessarily identical to the normalizer breakpoints. When you create a table the breakpoint values are the same as the normalizer values. If you delete breakpoints from the normalizers the table size does not change, so the table column and row breakpoint values are interpolated between the remaining normalizer breakpoints. (See "Viewing and Editing a Table" on page 3-8.)

2 The graph of the table pane displays the table values graphically. (See "Using the Graph of the Table" on page 3-10.)

3 The comparison-of-results pane displays a comparison between the current output of the strategy and the feature model. (Only visible when calibrating a feature, see "Inverting a Table" on page 3-39.)

Note You can view the History display by selecting View > History. For information, see "Using the History Display" on page 3-16.

This section describes each of these parts in detail.

## Viewing and Editing a Table

The table displays the values of your lookup table and displays the breakpoints of the normalizers. For example, the following table shows a lookup table with speed and relative air charge (load) as its normalizers.


To edit a value in the table, double-click the cell, then you can enter a value. Selected cells are blue except for the focussed cell which is white and outlined (typing edits the focussed cell). You can also edit table values using the table graph, see below.

See also "Filling a Table by Extrapolation" on page 3-11, and "Adjust Cell Values" on page 3-13 for information on applying arithmetic operations to selected cell values or whole tables.

## Locking and Unlocking Cell Values

When you are satisfied with a region of the table, you might want to lock the cell values in that region, to ensure that those values do not change.

To lock or unlock a cell value, right-click the cell and select from the menu. Locked cells have a padlock icon in the display. You can also lock an entire table using the Table menu.

## Using the Graph of the Table

The table view displays both the table values and a graph of the table. This gives a useful display of the table's behavior. Shown is an example of a graph in dragging and rotation mode.


- In the default mode, you can rotate the graph of the table by clicking and dragging the axes.
- Select View > Edit Table Surface to alter values in the table by clicking and dragging vertically any point. In this mode, when you click a point, a blue line indicates the selected point in the table. To return to table rotation mode without altering table values, select View > Rotate Table Surface.

Note When editing the table surface you may drag a value unintentionally - to return to previous table values, use the History display. See "Using the History Display" on page 3-16.

## Filling a Table by Extrapolation

Filling a table by extrapolation fills the table with values based on the values already placed in the extrapolation mask. Using the extrapolation mask is described below.

To fill a table by extrapolating over a preselected mask, click Table > Extrapolate.

This extrapolation does one of the following:

- If the extrapolation mask has only one value, all the cell values change to the value of the cell in the mask.
- If the extrapolation mask has two or more collinear values, the cell values change to create a plane parallel to the line of values in the mask.
- If the extrapolation mask has three or more coplanar values, the cell values change to create that plane.
- If the extrapolation mask has four or more ordered cells (in a grid), the extrapolation routine fills the cells by a grid extrapolation.
- If the extrapolation mask has four or more unordered (scattered) cells, the extrapolation routine fills the cell values using a thin plate spline interpolant (a type of radial basis function).


## Using the Extrapolation Mask

The extrapolation mask defines a set of cells that form the basis of any extrapolation.

For example, a speed-load (or relative air charge) table has values in the following ranges that you consider to be accurate:

- Speed 3000 to 5000 rpm
- Load 0.4 to 0.6

You can define an extrapolation mask to include all the cells in these ranges. You can then fill the rest of your table based on these values.

To add or remove a cell from the extrapolation mask,

1 Right-click the table.
2 Select Add To Mask or Remove From Mask from the menu.
Cells included in the extrapolation mask are colored yellow.
Cells that are locked and in the extrapolation mask are yellow and have a padlock icon.

When using feature calibration you can also generate the extrapolation mask from the boundary model or from the predicted error of the model. See "Filling the Table by Extrapolation" on page 4-30.

## Table Menu

All the toolbar button functions are also found in the table menu: Initialize, Fill, Extrapolate, Fill by Inversion. For information on these see "Calibrating the Tables" on page 4-24.

The Table menu contains the following other options

- Adjust Cell Values. This opens a dialog where you can specify an arithmetic operation to apply to either the whole table or only the cells currently selected. Arguments to operations can be numeric (plus 10) or percentages (minus $5 \%$ ). You can set the selected cells to a value or to the mean. You can also apply user-defined functions. See "Adjust Cell Values" on page 3-13. This function is also in the table context menu.


## - Extrapolation Mask

The following items are also in the table context menu:

- Add Selection - Adds selected cells to the extrapolation mask.
- Remove Selection - Removes selected cells from the extrapolation mask.
- Clear Mask - This ensures that none of the cells are in the extrapolation mask.
- Generate From PE - Generate extrapolation mask depending on the value of prediction error (PE). Only available for tables in feature calibration, as you must have a model to calculate PE. A dialog opens
where you can specify the threshold value of PE below which you want to include cells in the mask. The dialog contains information about the range and mean of prediction error for the model to help you select a threshold.
- Generate From Boundary Model - Generate extrapolation mask to include only cells within the boundary model. Only available for tables in feature calibration, as you must have a boundary model.
- Extrapolate - Extrapolates values from the cells in the extrapolation mask to fill the whole table. Also in the toolbar.
- Table Cell Locks The following items are also in the table context menu:
- Lock Selection - Locks the selected cells and a padlock icon appears..
- Unlock Selection - Unlocks the selected cells.
- Lock Entire Table - Locks every cell in the current table.
- Clear All Locks - Unlocks all cells in the table.
- Convert to Model. This option converts a table directly to a model.
- Properties. This opens the Table Properties dialog where you can set the precision type of the table data. You can also reach this from the Calibration Manager. See "Table Properties" on page 3-24.


## Adjust Cell Values

This Table menu item (or right-click context menu item) opens a dialog where you can specify an arithmetic operation to apply.

1 Select the operation to apply from the list - plus, minus, times, divide, set to value, set to mean, or custom operation. Use the custom operation to specify your own function in an M-file.

2 Use the Value edit box to enter an argument. All operators accept a numeric argument (e.g. operator $=$ plus, value $=10$ ). You can also enter a percentage for the operators plus, minus, and set to value (e.g. 'minus ' ' $1 \%$ ').

3 Select the radio buttons to apply the operation to either the whole table or only the cells currently selected, and click OK.

You can use the custom operation option to apply user-defined functions.

The custom function is called in this way:

```
newvalues = customfcn( currentvalue, selectedregion )
```

Where currentvalue is the matrix of table values and selectedregion is a logical matrix the same size as the table, that is "true" where a cell is selected by the user, and false otherwise.

The newvalues matrix should be the same size as currentvalue, and these numbers are put straight into the table.

## EXAMPLES:

```
function table = addOne( table, region )
table(region) = table(region) + 1;
return;
function table = randomtable( table, region )
table( region ) = rand( nnz( region ), 1 );
function table = saturate( table, region )
maxValueAllowed = 150;
table( region & table>maxValueAllowed ) = maxValueAllowed;
minValueAllowed = 100;
table( region & table<minValueAllowed ) = minValueAllowed ;
return
```

As an illustration, to use the saturate example:
1 Save the function text in an M-file named saturate.m.
2 Click and drag to select a region of cells in a CAGE table.
3 Right-click and select Adjust Cell Values.
4 In the dialog:

- Select custom operation from the Operation list
- Enter saturate in the Value edit box (the first function of that name found on the MATLAB path will be used), or click the browse button to locate the M-file.
- Select the radio button to Apply to selected table cells, and click OK.

The selected table cells are saturated between the ranges specified in the function M-file (between 100-150).

## Using the History Display

The History display enables you to view the history of any table or normalizer in a CAGE session.

The History display lets you

- Revert to previous versions of tables and normalizers (See "Resetting to Previous Versions" on page 3-17.)
- Compare different versions of tables and normalizers (See "Comparing Versions" on page 3-19.)

You can view the History display of a table or normalizer by selecting View > History.


The upper pane of the History display lists all the versions of the highlighted object.

The lower pane displays the normalizer or table of the highlighted version.

## Resetting to Previous Versions

To reset the normalizer or table to a previous version, select View > History to open the History display.

1 Highlight the previous version that you want to revert to.

## 2 Click Reset.

3 Click Close to see the updated table view.

> Note Tables are independent of normalizers, so if you reset a table to a previous version you must also reset the normalizers to that version (if they have changed).

To remove previous versions of the object or comments,
1 Highlight the version that you want to remove.
2 Click Remove.

## Adding and Editing Comments About Versions

To add comments,
1 Click Add.
2 In the dialog box enter your comment.
3 Click OK. A new History set point is added when you add a comment.
To edit comments,
1 Select the comment that you want to edit.

## 2 Click Edit comment.

3 In the dialog box, edit the comment.
4 Click OK.

## Comparing Versions

To compare two different versions of a normalizer or table, highlight the two versions using Ctrl+click. Note the following:

- The lower pane shows the difference between the later and the earlier versions.
- Cells that have no entries have no difference.
- Cells that have red entries have a higher value in the later version.
- Cells that have blue entries have a lower value in the earlier version.

| Input |
| ---: |
|  |
| -1.621 |
| -3.266 |
| $1.694 \mathrm{E}-3$ |
| -9.094 |
| -18.105 |
| -25.8 |
| -30.091 |
| -15.32 |
| -5.626 |
| -29.554 |

## Calibration Manager

To change the size of tables in CAGE, you use the Calibration Manager dialog box. Open this tool by selecting Tools > Calibration Manager or by clicking蟹 on the toolbar.

You can either set up your tables manually or from a calibration file. You can also copy table data from other sources.

Note that you can enter the required inputs, number of rows and columns and an initial value for table cells when you add a new table using the File > New menu items. See "Adding, Duplicating and Deleting Tables" on page 3-4. You can use the Calibration Manager to change the sizes, values and precision of tables.

## Setting Up Tables Manually

1 Select the normalizer or table to set up from the list on the left.
2 Enter the number of rows and columns in the edit boxes on the left and select initial values for each cell in the table.

3 Click Apply.


Note When initializing tables for a feature calibration (comparing a model to a strategy) you should think about your strategy. CAGE cannot fill those tables if you try to divide by zero. Modifier tables should be initialized with a value of 1 for all cells if they are multipliers, and a value of 0 if they are to be added to other tables. See "Initializing Table Values" on page 4-25.

4 Check the display of your table, then click Close.

## Setting Up Tables Using an Existing Calibration File

1 Open the file by clicking $\stackrel{\text { 家. }}{ }$.
This opens the Import Calibration Data dialog box.
2 You can select whether you want to import from File or from ATI Vision. See "Importing and Exporting Calibrations" on page 3-46 for details.

3 If importing from file, browse to the calibration file, select it, and click Open. Note that empty data is filtered out and any empty variables will not appear.

Note tutorialcal.mat is an example calibration file in the mbctraining folder.

If importing from ATI Vision, use the Connection Manager dialog to select the required calibration. See "Importing and Exporting Calibrations" on page 3-46 for instructions.

4 Highlight both the table in the Calibration File Contents pane and the table in the Project Calibration Items pane that you want to associate with it.

5 Associate these two items by clicking


To associate all the items listed in the Project Calibration Items pane with items having the same names listed in the Calibration File Contents pane, click <-.Auto …

6 To find particular names in a large calibration file, click the Calibration File Contents list, and type the first few letters of the item that you are searching for. The cursor moves to the letters specified as you type.

7 Check the display of your table, then click Close.


Note You can add additional file formats to configure CAGE to work with your processes.

Contact The MathWorks for details about adding file formats at http:/www.mathworks.com/products/mbc/.

## Copying Table Data from Other Sources

You can paste table values from other applications, such as Excel, by copying the array in the other application and clicking Paste in the Calibration Manager:

1 Open the desired file and copy the array that you want to import.
2 In the Calibration Manager dialog box, click Paste 绩 .
You can also set up a table from a text file:
1 Click Set Up From ASCII File 照 in the toolbar.
2 Select the desired file, then click Open.

Note If the size of the table is different from the file that you are copying, CAGE changes the size of the table in the session.

## Table Properties

Table properties allow you to edit the precision of the number in selected tables and normalizers according to the way tables are implemented in the electronic control unit (ECU). The ECU designer chooses the type of precision for each element to make best use of available memory or processor power.

To edit the precision of a table or normalizer,
1 Click the Edit Precisionbutton in the Calibration Manager dialog box.
Alternatively, if you highlight a table in a calibration (in the Tables or Feature views), display the table properties by selecting Table > Properties.

2 Decide whether you want the precision to be writable, then either select or clear the Properties Read-only check box.

3 Select the Precision type you require for the table:

- Floating Point (See "Floating-Point Precision" on page 3-25.)
- Polynomial Ratio, Fixed Point (See "Polynomial Ratio, Fixed Point" on page 3-26.)
- Lookup Table, Fixed Point (See "Lookup Table, Fixed Point" on page 3-28.)

The following sections describe these types of precision in detail.

## Floating-Point Precision

The advantage of using floating-point precision is the large range of numbers that you can use, but that makes the computation slower.


There are three types of floating-point precision that you can choose from:

- IEEE double precision (64 bit)
- IEEE single precision (32 bit)
- Custom precision

If you choose Custom precision, you must specify the following:

- Number of mantissa bits
- Number of exponent bits

You can use the Range edit boxes to set a range of values restricting the values in the table.

When you are done, click OK.

## See Also

- For more information on IEEE double precision in MATLAB ${ }^{\circledR}$, see Moler, C., "Floating points," The MathWorks Company Newsletter, 1996.


## Polynomial Ratio, Fixed Point

The advantage of using fixed-point precision is the reduction in computation needed for such numbers. However, it restricts the numbers available to the user.

For example, the polynomial ratio is of the form (see the ratio shown)

$$
y=\frac{50 x+0}{0+255}
$$



To edit the polynomial ratio,

1 Select the Numerator Coefficients edit box and enter the coefficients. In the preceding example, enter 500.

The number of coefficients determines the order of the polynomial, and the coefficients are ordered from greatest to least.

2 Select the Denominator Coefficients edit box and enter the coefficients. In the preceding example, enter 0255.

3 Determine the range of values that you want to have in the table. In the preceding example, enter 050.

To edit the size of the precision, choose from

- BYTE (8 bits)
- WORD (16 bits)
- LONG (32 bits)
- CUSTOM (Enter the Number of bits in the edit box)

Next, select the radio button to determine whether you want the numbers to be Signed (negative and positive) or Unsigned (nonnegative).

You can use the Range edit boxes to set a range of values restricting the allowable values in the table, though there are also limits inherent in the storage format.

## Lookup Table, Fixed Point



The advantage of using fixed-point precision is the reduction in computation needed for such numbers. However, it restricts the numbers available to the user.

For example, consider using a lookup table for the physical quantity spark advance for maximum brake torque (MBT spark). Typically, the range of values of MBT spark is 0 to 50 degrees. This is the physical data. The ECU can only store bytes of information and you want to restrict the hardware store to a range of 0 to 8 , with at most one decimal place stored.

To adjust the fixed-point precision of the lookup table,
1 Select the Physical Data edit box and enter the range of the physical data. In the example shown it is0 50 .

2 Select the Hardware Data and enter the range to store. In the example shown it is 08 .

3 Determine the range of values that you want to have in the table. In the example shown it is0 50 .

To edit the size of the precision, choose from

- BYTE (8 bits)
- WORD (16 bits)
- LONG (32 bits)
- CUSTOM (Enter the Number of bits in the edit box)

In the example shown, the hardware is restricted to 8 bytes and to one decimal place.

Choose whether you want the numbers to be Signed (negative and positive) or Unsigned (nonnegative) by clicking the radio buttons.

You can use the Range edit boxes to set a range of values restricting the values in the table.

## About Normalizers

What are normalizers? A normalizer is the axis of your lookup table. It is the same as the collection of the breakpoints in your table.

For information on using the controls, see "Normalizer View" on page 3-32
CAGE distinguishes between the normalizers and the tables that they belong to. Using models to calibrate lookup tables enables you to perform analysis of the models to determine where to place the breakpoints in a normalizer. This is a very powerful analytical process.

Note For information on optimizing breakpoints with reference to a model (in feature calibration), see "Calibrating the Normalizers" on page 4-12.

It is important to stress that in CAGE a lookup table can be either one-dimensional or two dimensional. One-dimensional tables are sometimes known as characteristic lines or functions. Two-dimensional tables are also known as characteristic maps or tables. This is important because normalizers are very similar to characteristic lines.

For example, a simple strategy to calibrate the behavior of torque in an engine might have a two-dimensional table in speed and relative air charge (a measure of the load). Additionally, this strategy might take into account the factors of air/fuel ratio (AFR) and spark angle. Each of these compensating factors is accounted for by the use of a simple characteristic line. In CAGE, these characteristic lines are one-dimensional tables. In the example strategy, there are the following tables and normalizers:

- One characteristic map: the torque table
- Six characteristic lines:
- Two tables: one for AFR and one for spark angle
- Four normalizer functions: speed, load, AFR, and spark angle

Notice also that a breakpoint is a point on the normalizer where you set values for the lookup table.

Thus, when you calibrate a normalizer you place the individual breakpoints over the range of the table's axis.

## Normalizer View

The normalizer node shows the Normalizer view, which displays

- One normalizer if the table selected is one-dimensional
- Both normalizers if the table is two-dimensional

Note If the table has two normalizers, both are displayed, the normalizer for the table columns at the top, the normalizer for the table rows below. This is true whichever normalizer on the tree is highlighted.

See "Editing Breakpoints" on page 3-33.
The parts of the display as shown in the example below are:

- "Input/Output Display" on page 3-35. This shows the breakpoints of the normalizer.
- "Normalizer Display" on page 3-35. This is a graphical representation of the Input Output display.
- "Breakpoint Spacing Display" on page 3-36. This shows a slice of the model (in feature calibration) over the range of the breakpoints.
- The comparison pane (for feature calibration with reference to a model). For information, see "Viewing the Normalizer Comparison Pane" on page 4-21.


## Normalizer View



## Editing Breakpoints

To edit breakpoints:

- Double-click on a cell in the Input or Output column and edit the value.
- Click and drag a breakpoint in the Normalizer Display graph or the Breakpoint Spacing display.

To view the history of the normalizer function, select View > History from the menu. This opens the History dialog box where you can view and revert to
previous versions. For a more detailed description of the History dialog box, see "Using the History Display" on page 3-16.

## Locking and Unlocking Breakpoints

Locking breakpoints ensures that the locked breakpoint does not alter. You might want to lock a breakpoint when you are satisfied that it has the correct value.

To lock a breakpoint, do one of the following:

- Right-click the selected breakpoint in the Input/Output display and select Lock. Locked breakpoint cells have padlock icons.
- Right-click the selected breakpoint in the Normalizer Display or Breakpoint Spacing display and select Lock Breakpoint. Locked breakpoints are black.

Similarly use the right-click context menus to unlock breakpoints.

## Deleting Breakpoints

Deleting breakpoints removes them from the normalizer table. There are still table values for the deleted breakpoints: CAGE determines the positions of the deleted breakpoints by spacing them linearly by interpolation between the nondeleted breakpoints.

Deleting breakpoints frees ECU memory. For example, a speed normalizer runs from 500 to 5500 rpm . Six breakpoints are spaced evenly over the range of speed, that is, at $500,1500,2500,3500,4500$, and 5500 rpm . If you delete all the breakpoints except the endpoints, 500 and 5500 rpm , you reduce the amount stored in the ECU memory. The ECU calculates where to place the breakpoints by linearly spacing the breakpoints between the 500 rpm breakpoint and the 5500 rpm breakpoint.

To delete a breakpoint, right-click the breakpoint and select Delete Breakpoint.

Deleted breakpoints are green in the Breakpoint Spacing display. You can restore them by right-clicking and selecting Add Breakpoint.

## Input/Output Display

| Input | Output |
| :---: | :---: |
| 500 | 0 |
| 1055 | 1 |
| 1609 | 2 |
| 2164 | 3 |
| 2718 | 4 |
| 3273 | 5 |
| 3828 | 6 |
| 4332 | 7 |
| 4836 | 8 |
| 5391 | 9 |
| 5895 | 10 |
| 6500 | 11 |

The table consists of the breakpoints of the normalizer function.
The table has inputs and outputs:

- The inputs are the values of the breakpoints.
- The outputs refer to the row/column indices of the attached table.

To change values of the normalizers in the Input Output display, double-click a cell in the Input column and change its value.

## Normalizer Display

This displays the values of the breakpoints plotted against the marker numbers of the table (that is, the inputs against the outputs).

Click and drag the breakpoints to move them.

## Example of the Normalizer Display



## Breakpoint Spacing Display

The Breakpoint Spacing display shows

- A slice through the model in blue (when feature calibrating with reference to a model)
- The breakpoints in red

To move breakpoints, click and drag.

## Example of the Breakpoint Spacing Display



## Show the Model's Curvature

You might want to view the curvature of the model to manually move breakpoints to where the model's curvature is greatest.

To display the model slice as its second-order derivative, the curvature of the model,

- Right-click the model in the Breakpoint Spacing display and select Display > Model Curvature..

You can revert to displaying the model by selecting Display > Modelfrom the right-click menu.

## Multiple Slice View

By default the Breakpoint Spacing display shows one slice through the model, shown.

## Slice Through a Model Surface



Viewing many slices of the model gives a better impression of the curvature of the model. For example, see the following figure.

## Many Slices Through a Model

 Surface

To view multiple slices through the model,

- Right-click the model slice in the Breakpoint Spacing display and select Number of Lines and choose the number of slices that you want to view from the list.


## Inverting a Table

You can use CAGE to produce a table that is the inverse of another table. This involves swapping a table input with a table output, and you can invert 1-D or 2-D tables.


Inverting a table allows you to link a forward strategy to a backward strategy; that is, swapping inputs and outputs. This process is desirable when you have a "forward" strategy, for example predicting torque as a function of speed and load, and you want to reverse this relationship in a "backward strategy" to find out what value of load would give a particular torque at a certain speed.

Normally you fill tables in CAGE by comparing with data or models. Ideally you want to fill using the correct strategy, but that might not be possible to find or measure. If you only have a forward strategy but want a backward one, you can fill using the forward strategy (tables or model) and then invert the table.

For example, to fill a table normally from a model, you need the model response to be the table output, and the model inputs to be a function of the table inputs (or it should be possible to derive the input -- for example, air mass from manifold pressure). If the available model is "inverted"(the model response is a table input and the table output is a model input) and you cannot change the model, you can invert the table in CAGE.


In the diagram of a table shown, the $x$ - and $y$-axes represent the normalizers (which you want to be spark and load) and the $z$-axis is the output at each breakpoint (torque). To fill this table correctly from the model is a two-step process. First you need to fill a table that has the same input and output as the model, and then fill a second table by inversion.

For the inversion to be deterministic and accurate, the table to be inverted must be monotonic; that is, always increasing or decreasing. This requirement is explained by the following one-dimensional example. Every point on the $y$-axis must correspond to a unique point on the $x$-axis. The same problem applies also to two-dimensional tables: for any given output in the first table there must be a unique input condition; that is, every point on the $z$-axis should correspond to a unique point in the x-y plane. Some table inversions have multiple values and so do not meet this requirement, just as the square root function can take either positive or negative values. You can use the inversion wizard in CAGE to handle this problem; you can control the inversion process and determine what to do in these cases.

The following example illustrates a table with multiple values. There are two solutions for a single value of torque. CAGE has a table inversion wizard that can help overcome this problem. You can specify whether you want to use the upper or lower values for filling certain parts of the table; this allows you to successfully invert a multiple-valued function. See the inversion instructions for 1-D and 2-D tables in the next sections.


The process of inverting a one-dimensional table is different from the process of inverting a two-dimensional table.

## Inverting One-Dimensional Tables

To invert a one-dimensional table,
1 Ensure that your session contains two tables:
a The first table from your forward strategy, filled
b The second table from your backward strategy, which you want to fill
2 Highlight the second table.
3 Click $\mathrm{F}^{*}$ or select Table > Fill by Inversion.
The lower pane now acts as a wizard.
4 In the lower pane, highlight the table that you want to invert. Click Next.
5 The next page asks what CAGE should do if it encounters multiple values. The options are

- Minimum selects the lower of the two if a given number has two possible inverses (like selecting the negative square root of a number).
- Maximum selects the uppermost range if a given number has two possible inverses (like selecting the positive square root of a number).
- Intermediate selects the middle range if a given number has more than two possible inverses.
- Automatic selects the range that produces the least error (see below; the last page of the wizard plots the error metric).

For example, the function $y=x^{2}$ is impossible to invert over the range -1 to 1. You can specify to invert the range from 0 to 1 , sacrificing the inversion in the lower range, or the reverse. To select the range from 0 to 1 , highlight Maximum.

The display shows a comparison between the table (green) and the function $x=f^{-1}(f(x))$.

Choose one of these options, then click Next.
6 The last page of the wizard has a comparison plot that shows how successful the inversion has been. If your forward function is $y=f(x)$, and your inverse function is $x=g(y)$, then, combining these, in an ideal world, you should have $\mathrm{x}=\mathrm{g}(\mathrm{f}(\mathrm{x}))$. The plot then displays a red line showing x against x and a green line showing $x$ against $g(f(x))$. The closeness of these two lines indicates how good the inversion has been: a perfect inverse would show the lines exactly on top of each other.

In the following example, the lines are together and then diverge; this plot can show you which part of your table has not successfully inverted and where you should try a different routine.

## Inverting a One-Dimensional Table



Note The automatic inversion routine tries to minimize the total distance between these lines. This can sometimes lead to unexpected results. For example, given the function $f(x)=x^{\wedge} 2$ between -1 and 1 , if you select either positive or negative square root as the inverse, this induces a large error in the combined inverse. If you choose $g(y)=\operatorname{sqrt}(\mathrm{y})$, then $\mathrm{g}(\mathrm{f}(-1))=1$, an error of 2 . To minimize this, the automatic routine might choose to send everything to zero and accept a medium error over the whole range rather than a large error over half the range. The more knowledge you have of the form of the "forward" table, the more you can make an informed choice about which routine to select.

7 Click Finish to accept the inversion or Cancel to ignore the result and return to the original table.

## Inverting Two-Dimensional Tables

To invert a two-dimensional table,
1 Ensure that your session contains two tables:
a The first table from your forward strategy, filled
b The second table from your backward strategy, which you want to fill
2 Highlight the second table.
3 Click $\mathrm{F}^{*}$ or select Table > Fill by Inversion.
The lower pane now acts as a wizard.
4 In the lower pane, highlight the table that you want to invert and click Next.

5 Identify the corresponding signals.
The forward table and backward table share a common input. This page of the wizard lists all possible combinations of inputs into the forward and backward tables and asks you to highlight the combination that gives the two common inputs. To illustrate this, if the forward table gives torque in terms of the variables engine speed and load, whereas you want the backward table to give load in terms of RPM and Tq, then the list would read

- RPM and engine speed
- RPM and load
- Tq and engine speed
- Tq and load

In this case, you would select the first option.
Highlight the part of the table to invert, then click Next.
6 CAGE asks what to do if it encounters multiple values. The choices are

- Maximum selects the uppermost range (like choosing a positive square root of a number).
- Minimum selects the lower value if there are two choices (like choosing a negative square root of a number).
- Intermediate selects the middle range when there are more than two choices.
- Automatic selects the range that produces the least error. CAGE tries to choose values to put in the inverse table that minimize an
error metric similar to the error metric for 1-D tables (see "Inverting One-Dimensional Tables" on page 3-41).

Choose one of these options and click Next.
7 The last page of the wizard has a comparison plot that shows how successful the inversion has been. If the forward function is $z=f(x, y)$, and the inverse function is $x=g(y, z)$, then, combining these, in an ideal world you should have $\mathrm{x}=\mathrm{g}(\mathrm{y}, \mathrm{f}(\mathrm{x}, \mathrm{y}))$. The plot then displays a plane showing x plotted against x and y , and a colored surface showing $\mathrm{g}(\mathrm{y}, \mathrm{f}(\mathrm{x}, \mathrm{y}))$ plotted against x and y . The closeness of these two planes indicates how good the inversion is.

Following is an example. In this case, the forward table is a quadratic (z $=y^{\wedge} 2$ ); the backward table is inverted using the positive square root of z (maximum range). As you can see, this leads to large errors at negative values of $y$, but good inversion for positive values of $y$.


Click Finish to accept the result or Cancel to ignore the result and return to the original table.

## Importing and Exporting Calibrations

You can import and export calibrations in various formats.

- You can import/export the following File formats:
- Simple CSV file
- Simple M file
- Simple MAT file
- ATI Vision MAT file
- ETAS INCA DCM file (version 1)
- Or directly to/from ATI Vision (Version 2.3.3).

Note Note to use the Vision interface you must first enter mbcconfig -visioninterface at the command line.

## Importing Calibrations

1 Select File > Import > Calibration > File or ATI Vision.
Similarly, from the Calibration Manager, if you click Open Calibration File in the toolbar, you can select File or ATI Vision in the dialog and proceed to import in the same way.

2 If importing a file, a file browser dialog opens.
a Select the type of file you want from the Files of type drop-down list, or leave the default All files (*.*) and CAGE will try to load the file based on the file extension.
b Browse to the file and click Open to import.
If importing from ATI Vision, the ATI Vision Connection Manager dialog appears.

a The Computer field is optional. Leave this field blank if you are using Vision on the local machine. If you want to connect to a remote machine, you can enter a machine name or an IP address.
b Click Connect.
If Vision is already running on the machine that you try to connect to, MATLAB connects to Vision. If Vision is not running then it is launched, typically with no project loaded and with the application window invisible.
c If there is a project (.prj file) currently loaded in Vision it appears in the Project field. If this field is blank then there is no project loaded. Type a project file name to load that project. Note that the project file path is relative to the machine on which Vision is running.
d Select the appropriate Vision Device, Strategy and Calibration within your project, and click OK to import.

## Exporting Calibrations

## 1 Select File > Export > Calibration > Selected Item or All Items.

2 The Export Calibration dialog appears. Select the format you want to export to:

- ATI Vision
- ATI Vision MAT file
- INCA DCM file
- Simple CSV file
- Simple MAT file
- Simple M file

Click OK.
3 If you select ATI Vision, the ATI Vision Connection Manager dialog appears, as for importing calibrations.

If you select a file format, a file browser appears. Choose a location and filename and click Save.
If you choose All Items, all tables, normalizers, curves and constants in the project are exported.

What you export when you choose Selected Item depends on which node is highlighted:

- Selecting a Normalizer node outputs the values of the normalizer.
- Selecting a Table node outputs the values of the table and its normalizers.
- Selecting a Feature or Tradeoff node outputs the whole feature or tradeoff (all tables, normalizers, curves and constants).

When exporting to an existing calibration file, the exported items replace the existing items. (There is no merging of existing items and new exported items.)

When exporting to Vision, the items in the CAGE project are matched by name with the items in the Vision calibration and the values are replaced. It is not possible to add new items to a Vision project by exporting from CAGE.

## Feature Calibrations

This section includes the following topics:

## Performing Feature Calibrations (p. 4-2) <br> Setting Up a Feature Calibration (p. 4-5)

Calibrating the Normalizers (p. 4-12)

Calibrating the Tables (p. 4-24)

Calibrating the Feature Node (p. 4-32)

Feature View (p. 4-41)

Introduction to feature calibrations and an overview of the processes involved.

How to add a new feature, assign a model, and set up your strategy and tables.

How to calibrate the normalizers by spacing the breakpoints. This covers initializing, filling, and optimizing breakpoints with reference to a model.

How to initialize, fill, extrapolate and optimize your table values with reference to a model.
How to calibrate a whole feature at once, rather than table by table, using the Feature Fill Wizard.
Functionality available in the Feature view.

## Performing Feature Calibrations



A 'feature' calibration is the process of calibrating lookup tables and their normalizers by comparing an ECU strategy (represented by a Simulink diagram) to a model.

The strategy is an algebraic collection of lookup tables. It is used to estimate signals in the engine that cannot be measured and that are important for engine control.

CAGE calibrates an electronic control unit (ECU) subsystem by directly comparing it with a plant model of the same feature.

There are advantages to feature calibration compared with simply calibrating using experimental data. Data is noisy (that is, there is measurement error) and this can be smoothed by modeling; also models can make predictions for areas where you have no data. This means you can calibrate more accurately while reducing the time and effort required for gathering experimental data.

The basic procedure for performing feature calibrations is as follows:
1 Set up the variables and constants. (See "Setting Up Variable Items" on page 2-3.)

2 Set up the model or models. (See "Setting Up Models" on page 2-11.)
3 Set up the feature calibration. (See "Setting Up a Feature Calibration" on page 4-5.)

4 Calibrate the normalizers. (See "Calibrating the Normalizers" on page 4-12.)

5 Calibrate the tables. (See "Calibrating the Tables" on page 4-24.)
6 Calibrate and view the entire feature. (See "Calibrating the Feature Node" on page 4-32.)

7 Export the normalizers, tables, and features. (See "Importing and Exporting Calibrations" on page 3-46.)

The normalizers, tables, and features form a hierarchy of nodes, each with its own view and toolbar. The feature view is shown.


## Setting Up a Feature Calibration

A feature calibration is the process of calibrating lookup tables and their normalizers by comparing a collection of lookup tables to a model. The collection of lookup tables is determined by a strategy.

A feature refers to the object that contains the model and the collection of lookup tables. For example, a simple feature for calibrating the lookup tables for the maximum brake torque (MBT) consists of

- A model of MBT
- A strategy that adds the two following tables:
- A speed ( $N$ ), load ( $L$ ) table
- A table to account for the behavior of the air/fuel ratio (A)

Having already set up your variable items and models, you can follow the procedure below to set up your feature calibration:

1 Add a feature. This is described in the next section, "Adding a Feature" on page 4-6.

2 Assign a model. This is described in "Assigning a Model" on page 4-6.
3 Set up your strategy. This is described in "Setting Up Your Strategy" on page 4-6.

4 Set up the tables. This is described in "Setting Up Tables" on page 3-3.
This section describes steps 1,2 , and 3 in turn.
When you have completed these four steps, you are ready to calibrate the normalizers, tables, and features.

## Adding a Feature

A feature consists of a model and a collection of lookup tables, organized in a strategy.

To add a feature to your session, select File -> New -> Feature. This automatically switches you to the Feature view and adds an empty feature to your session.

An incomplete feature is a feature that does not contain both an assigned model and a strategy. If a feature is incomplete, it is displayed asto in the tree display. If a feature is complete, it is displayed as in the tree display.

## Assigning a Model

Having already added a feature and a model to your session, you can assign a model to your feature.

To assign a model to your feature,
1 Highlight the top feature node in the tree display.
2 Click Select Model to select the model you want to work with. A dialog box appears.

3 Highlight the correct model to assign to your feature and click OK. You will see the model name and inputs appear above the Select Model button.

## Setting Up Your Strategy

A strategy is an algebraic collection of tables, and forms the structure of the feature.

For example, a simple strategy to calibrate a feature for MBT adds two tables:

- A table ranging over the variables speed and load
- A table to account for the behavior of the model as the AFR varies

To evaluate the feature side by side with the model, you need to have a strategy that takes some or all of the same variables as the model. The
strategy is expressed using Simulink diagrams. You can either import a strategy or you can construct a strategy.

The following topics are described next:

- "Importing a Strategy" on page 4-7
- "Constructing a Strategy" on page 4-8
- "Exporting Strategies" on page 4-10


## Importing a Strategy

To import a Simulink strategy,
1 Highlight the top feature node in the tree display.

## 2 Select File > Import > Strategy.

3 Select the appropriate .mdl file. CAGE checks the strategy for more than one outport.

4 Select the outport that you want to use.
If there is more than one outport to your strategy, a Simulink window opens. Double-click the correct blue outport to parse (or import) the strategy to your feature.

If there is only one outport to your strategy, a dialog box opens.

- Click Automatic to parse the strategy without viewing it.
- Click Manual to edit the strategy. When you are finished editing double-click the blue outport circle to parse the strategy to your feature. The Simulink windows close and parse this strategy to your feature.

To view a representation of your strategy, select the Feature node. Your strategy is represented in the Strategy pane. Select View > Full Strategy Display to switch between the full description and the simplified expression. You can select and copy the strategy equation to the clipboard.

For information about using Simulink to amend strategies, see "Constructing a Strategy" on page 4-8.
 Simulink diagram called tutorial.mdl. If you import this and click Manual in the dialog box, you see the following diagram.


Double-click the Torque-Output outport to parse the strategy into the Strategy pane.

## Constructing a Strategy

For you to perform a feature calibration, the strategy and the model must have some variables in common.

To construct a strategy using Simulink,
1 Highlight the correct feature by clicking the Feature node.
2 Select Feature > Graphical Strategy Editor or press Ctrl+E.
Three Simulink windows open:

- The strategy window for editing your strategy, like the following example.

- A library window with all the blocks available for building a strategy.

- A library window with all the existing blocks in your session, organized in libraries.


3 In the strategy window, build your strategy using the blocks available in the library windows.

4 Double-click the blue outport circle to parse the strategy into the CAGE session.

Note This closes all three Simulink windows and parses your strategy into the feature.

For more information about using Simulink to build your strategy, see Simulink Help.

## Exporting Strategies

Simulink strategies can be exported. For example, you might want to

- Include a strategy in a Simulink vehicle model
- Compile the strategy using Real-Time Workshop ${ }^{\circledR}$ to produce C code
- Evaluate the strategy using Simulink

To export a strategy from CAGE,
1 Highlight the Feature node that contains the strategy that you want to save.
2 Select File > Export > Strategy.
3 Assign a name for your strategy.
The strategy is saved as a Simulink model (.mdl) file.

## Calibrating the Normalizers

Select a normalizer in the tree display. This displays the Normalizer view, where you can calibrate the normalizers.

This section describes how you can use CAGE to space the breakpoints over the range of the normalizers.

## Normalizer Toolbar



To space the breakpoints, either click the buttons on the toolbar or select from the following options on the Normalizer menu:

## - Initialize

This spaces the breakpoints evenly along the normalizer. For more information, see "Initializing Breakpoints" on page 4-13.

## - Fill

This spaces the breakpoints by reference to the model. For example, you can place more breakpoints where the model curvature is greatest. For more information, see "Filling Breakpoints" on page 4-13.

- Optimize

This moves the breakpoints to minimize the least square error over the range of the axis. For more information, see "Optimizing Breakpoints" on page 4-17.

The next sections describe each of these in detail.

Note Fill and Optimize are only available when you are calibrating with reference to a model, when you are performing Feature calibrations.

For more information about the Normalizer view controls, see "Normalizer View" on page 3-32.

## Initializing Breakpoints

Initializing the breakpoints places the breakpoints at even intervals along the range of the variable defined for the normalizer. When you add a table and specify the inputs in the Table Setup dialog, CAGE automatically initializes the normalizers of the table by spacing the breakpoints evenly over the ranges of the selected input variables. If you have edited breakpoints you can return to even spacing by using the Initialize function.

To space the breakpoints evenly,
1 Click $\|_{\text {W }}$ on the toolbar or select Normalizer > Initialize.
2 In the dialog box, enter the range of values for the normalizer.

## 3 Click OK.

For example, for a torque table with two normalizers of engine speed and load, you can evenly space the breakpoints of both normalizers over the range 500 rpm to 6500 rpm for speed and 0.1 to 1 for the relative air charge. To do this, in the dialog box you enter 5006500 for the speed normalizer, N , , and 0.11 for the load normalizer, $L$.

## Filling Breakpoints

Filling breakpoints spaces the breakpoints by reference to the model. For example, one method places the majority of the breakpoints where the curvature of the model is greatest. This option is only available when you are performing Feature calibrations.

For example, a model of the spark angle that produces the maximum brake torque (MBT) has the following inputs: engine speed $N$, relative air charge $L$, and air/fuel ratio $A$. You can space the breakpoints for engine speed and relative air charge over the range of these variables by referring to the model.

To space the breakpoints based on model curvature, perform the following steps:

## 1 Click $\mathbb{E}^{\text {or }}$ select Normalizer $>$ Fill.

The Breakpoint Fill Options dialog box opens.


2 Choose the appropriate method to space your breakpoints, from the drop-down menu in the dialog box.

The preceding example shows ShareAveCurv. For more information about the methods for spacing the breakpoints, see "Filling Methods" on page 4-15.

3 Enter the ranges of the values for the normalizers.
The preceding example shows Range N 500 6500, and Range L, 0.11 .
4 Enter the ranges of the other model variables.
CAGE spaces the breakpoints by reference to the model. It does this at selected points of the other model variables. The example shows 1117 for the Range of $\mathbf{A}$ and 2 for the Number of points. This takes two slices through the model at $A=11$ and $A=17$. Each slice is a surface in $N$ and $L$. That is, $M B T(N, L, 11)$ and $M B T(N, L, 17)$.

CAGE computes the average value of these two surfaces to give an average model $M B T_{\mathrm{AV}}(N, L)$.

## 5 Click OK.

Note If any of the breakpoints is locked, each group of unlocked breakpoints is independently spaced according to the selected algorithm.

If you increase the number of slices through the model, you increase the computing time required to calculate where to place the breakpoints.

## Filling Methods

This section describes in detail the methods for spacing the breakpoints of your normalizers in CAGE.

- For one-dimensional tables, the two fill methods are
- ReduceError
- ShareAveCurv
- For two-dimensional tables, the two fill methods are
- ShareAveCurv
- ShareCurvThenAve


## ReduceError

Spacing breakpoints using ReduceError uses a greedy algorithm:
1 CAGE locks two breakpoints at the extremities of the range of values.
2 Then CAGE interpolates the function between these two breakpoints.
3 CAGE calculates the maximum error between the model and the interpolated function.

4 CAGE places a breakpoint where the error is maximum.
5 Steps 2, 3, and 4 are repeated.
6 The algorithm ends when CAGE locates all the breakpoints.

## ShareAveCurv and ShareCurvThenAve

Consider calibrating the normalizers for speed, $N$, and relative air-charge, $L$, in the preceding MBT model.

In both cases, CAGE approximates the $M B T_{\text {AV }}(N, L)$ model, in this case using a fine mesh.

The breakpoints of each normalizer are calibrated in turn. In this example, these routines calibrate the normalizer in $N$ first.

Spacing breakpoints using ShareAveCurv or ShareCurvThenAve calculates the curvature, $K$, of the model $M B T_{\mathrm{AV}}(N, L)$,

$$
K=\sum_{i=1}^{\text {fine mesh }}\left(M B T_{A V}(N, L)\right)^{1 / 2}
$$

as an approximation for

$$
K=\int_{750}^{6000}\left|M B T_{A V^{\prime \prime}(N, L)}\right|^{1 / 2} d N
$$

Both routines calculate the curvature for a number of slices of the model at various values of $L$. For example, the figure shown has a number of slices of a model at various values of $L$.

## Model Slices at Various Values of $\mathbf{L}$



Then

- ShareAveCurv averages the curvature over the range of $L$, then spaces the breakpoints by placing the $i^{\text {th }}$ breakpoint according to the following rule.
- ShareCurvThenAve places the $i^{\text {th }}$ breakpoint according to the rule, then finds the average position of each breakpoint.

Rule for Placing Breakpoints. If $j$ breakpoints need to be placed, the $i^{\text {th }}$ breakpoint, $N_{\mathrm{i}}$, is placed where the average curvature so far is

$$
\int_{150}^{N_{i}}\left|M B T_{A V}{ }^{\prime \prime}(N, L)\right|^{1 / 2} d N=\frac{i-1}{j-1} \times K
$$

Essentially this condition spaces out the breakpoints so that an equal amount of curvature (in an appropriate metric) occurs in each breakpoint interval. The breakpoint placement is optimal in the sense that the maximum error between the lookup table estimate and the model decreases with the optimal convergence rate of $\mathrm{O}\left(\mathrm{N}^{-2}\right)$. This compares with an order of $\mathrm{O}\left(\mathrm{N}^{-1 / 2}\right)$ for equally spaced breakpoints.

The theorem for determing the position of the unequally spaced breakpoints is from the field of Approximation Theory - page 46 of the following reference: de Boor, C., A Practical Guide to Splines, New York, Springer-Verlag, 1978.

## Optimizing Breakpoints

Optimizing breakpoints alters the position of the table normalizers so that the total square error between the model and the table is reduced.

This routine improves the fit between your strategy and your model. The following illustration shows how the optimization of breakpoint positions can reduce the difference between the model and the table. The breakpoints are moved to reduce the peak error between breakpoints. In CAGE this happens in two dimensions across a table.


To see the difference between optimizing breakpoints and optimizing table values, compare with the illustration in "Optimizing Table Values" on page 4-26.

See "Filling Methods" on page 4-15 for details on how the optimal breakpoint spacing is calculated.

For an example of breakpoint optimization, say you have a model of the spark angle that produces the MBT (maximum brake torque). The model has the following inputs: engine speed, $N$, relative air charge, $L$, and air/fuel ratio, $A$. You can optimize the breakpoints for $N$ and $L$ over the ranges of these variables.

To optimize the breakpoints, perform the following steps:

1 Ensure that the optimization routine works over reasonable values for the table by choosing one of these methods:
a Select Normalizer > Initialize.
b Select Normalizer > Fill .
2 Click $\mathbf{O}$ on the toolbar or select Normalizer > Optimize.
This opens the following dialog box.


3 Enter the ranges for the normalizers.
The example shows 0.20 .811 for the Range of $\mathbf{L}$, and 7506500 for $\mathbf{N}$.
4 Enter the appropriate number of grid points for the optimization.

This defines a grid over which the optimization works. In the preceding example, the number of grid points is 36 for both $L$ and $N$. This mesh is combined using cubic splines to approximate the model.

5 Enter ranges and numbers of points for the other model variables.
The example shows a Range of $\mathbf{A}$ of 14.3 and the Number of points is 1 .
6 Decide whether or not to reorder deleted breakpoints, by clicking the radio button.

If you choose to reorder deleted breakpoints, the optimization process might redistribute them between other nondeleted breakpoints (if they are more useful in a different position).

For information about deleting breakpoints, see "Editing Breakpoints" on page $3-33$.

## 7 Click OK.

CAGE calculates the table filled with the mesh at the current breakpoints. Then CAGE calculates the total square error between the table values and the mesh model.

The breakpoints are adjusted until this error is minimized, using nonlinear least squares optimization (lsqnonlin).

When optimizing the breakpoints, it is worth noting the following:

- The default range for the normalizer variable is the range of the variable.
- The default value for all other model variables is the set point of the variable.
- The default number of grid points is three times the number of breakpoints.


## See Also

- Reference page for lsqnonlin


## Viewing the Normalizer Comparison Pane

To view or hide the comparison pane, select View > Feature/Model Comparison. Alternatively, click $\quad$, the "snapper point" at the bottom of the normalizer display panes.


The comparison pane displays a comparison between the following:

- A full factorial grid filled using these breakpoints
- The model

Note This is not a comparison between the current table values and the model. To compare the current table values and the model, see "Comparing the Strategy and the Model" on page 4-28.

To make full use of the comparison pane,
1 Adjust the ranges of the variables that are common to the model and table.
2 Adjust the values selected for any variables in the model that are not in the selected table.

The default for this is the set point of the variable, as specified in the variable dictionary. For more information, see "Using Set Points in the Variable Dictionary" on page 2-6.

3 Check the number of points at which the display is calculated.
4 Check the comparison between the table and the model.
Right-click the comparison graph to view the error display.
5 Check some of the error statistics for the comparison, and use the comparison to locate where improvements can be made.

## Error Display

The comparison pane can also be used to display the error between the model and the 'generated table' (grid filled using these breakpoints).

## Error Display in the Comparison Pane



To display the error, select one of the Error items from the Plot type drop-down list.

This changes the graph to display the error between the model and the table values at these breakpoints.

You can display the error data in one of the following ways:

- Error (Table Model). This is the difference between the feature and the model.
- Squared Error. This is the error squared.
- Absolute Error. This is the absolute value of the error.
- Relative Error. This is the error as a percentage of the value of the table.
- Absolute Relative Error (\%). This is the absolute value of the relative error.


## See Also

- "Comparing the Strategy and the Model" on page 4-28

This describes the comparison made when a table node is selected in the tree display.

## Calibrating the Tables

After you set up your session and your tables, you can calibrate your tables.
Highlight a table in the tree display to see the Table view. For more information about the Table view, see "Table View" on page 3-6.

In CAGE, a table is defined to be either a one-dimensional or a two-dimensional lookup table. One-dimensional tables are sometimes known as characteristic lines or functions. Two-dimensional tables are also known as characteristic maps or tables.

Each lookup table has either one or two axes associated with it. These axes are normalizers. See "About Normalizers" on page 3-30 for more information.

For example, a simple MBT feature has two tables:

- A two-dimensional table with speed and relative air charge as its normalizer inputs
- A one-dimensional table with AFR as its normalizer input

Before you can calibrate your tables, you must calibrate your normalizers. For information, see "Calibrating the Normalizers" on page 4-12.

This section describes how you can use CAGE to fill your lookup tables by reference to a model.

To fill the table values, either click the buttons in the toolbar,
 or select from the following options in the Table menu:

## - Initialize Table

Sets each cell in the lookup table to a specified value. For information, see "Initializing Table Values" on page 4-25.

## - Fill Table

Fills and optimizes the table values by reference to the model. For information, see "Filling Table Values" on page 4-26.

## - Fill by Inversion

Fills the table by creating an inversion of another table. For information, see "Inverting a Table" on page 3-39.

## - Fill by Extrapolation

Fills the table values based on the cells specified in the extrapolation mask. You can choose values in cells that you trust to define the extrapolation mask and fill the rest of the table using only those cells for extrapolation. For information, see "Filling the Table by Extrapolation" on page 4-30.

The next sections describe each of these toolbar options in detail. See the "Table Menu" on page 3-12 for other menu options.

## Initializing Table Values

Initializing table values sets the value of every cell in the selected table to a constant. You can do this when you set up a table (see "Adding, Duplicating and Deleting Tables" on page 3-4) or later.

To initialize the values of the table,

## 1 Click $\vDash$ or select Table > Initialize.

2 In the dialog box that appears, select the constant value that you want to insert into each cell.

When initializing tables, you should think about your strategy. Filling with zeros can cause a problem for some strategies using "modifier" tables. For example, your strategy might use several speed-load tables for different values of AFR, or you might use an AFR table as a "modifier" to add to a single speed-load table to adjust for the effects of different AFR levels on your torque output.

Be careful not to initialize modifier tables with 0 if they are multipliers in your strategy. In this case, solving results in trying to divide by zero. This operation will fail. If your table is a modifier that is added to other tables, you should initially fill it with zeros; if it is a modifier that multiplies other tables, you should fill it with 1 s .

## Filling Table Values

To fill and optimize the table values by reference to the model,

- Click $E$ or select Table $>$ Fill.

This opens the Feature Fill Wizard. You can fill multiple tables at once using the wizard, and you can Fill from the top feature node or from any table node in a feature. See "Feature Fill Wizard" on page 4-34 for instructions.

## Optimizing Table Values

The Feature Fill Wizard optimizes the table values to minimize the current total square error between the feature values and the model.

This routine optimizes the fit between your strategy and your model. Using Fill places values into your table. The optimization process shifts the cell values up and down to minimize the overall error between the interpolation between the model and the strategy.

This process is illustrated by the following example; the green shaded areas show the error between the mesh model (evaluated at the number of grid points you choose) and the table values.


To see the difference between optimizing table values and optimizing the positions of breakpoints, compare with the illustration in "Optimizing Breakpoints" on page 4-17.

CAGE evaluates the model over the number of grid points specified in the Feature Fill Wizard, then calculates the total square error between this mesh model and the feature values. CAGE adjusts the table values until this error is minimized, using lsqnonlin if there are no gradient constraints, otherwise fmincon is used with linear constraints to specify the gradient of the table at each cell.

## See Also.

- Reference page for lsqnonlin
- "Calibrating the Tables" on page 4-24


## Comparing the Strategy and the Model

When you calibrate a strategy, or collection of tables, by reference to a model, it is useful to compare the strategy and the model. The comparison pane provides a graphical tool for investigating this, as shown in the following example.

Note This is a comparison between the current strategy values and the model, unlike the comparison pane from the normalizer node, which compares the model and a full factorial grid filled using the breakpoints.


To make full use of the comparison-of-results pane,
1 Check the ranges of the variables that are common to the model and table. For each variable check the number of points at which the display is calculated. Double-click to edit any variable range or number of points.

2 Check the values selected for any variables in the model that are not in the selected table. The default for this is the set point of the variable's range. Double-click to edit.

3 Check the comparison between the table and the model. You can rotate this comparison by clicking and dragging, so that you can view all parts of the comparison easily.

4 Use the Plot Type drop-down menu to display the error statistics for the comparison.

## Error Display

The comparison-of-results pane can also be used to display the error between the model and the strategy.


To display the error, select one of the Error options from the Plot Type drop-down menu. This changes the graph to display the error between the model and the strategy.

You can display the error data in one of the following ways:

- Error (Feature-Model). This is the difference between the feature and the model.
- Squared Error. This is the error squared.
- Absolute Error. This is the absolute value of the error.
- Relative Error (\%). This is the erroras a percentage of the value of the model.
- Absolute Relative Error (\%). This is the absolute value of the relative error.

When you have completed a calibration, you can export your feature. For information, see "Exporting Calibrations" on page 3-47.

## Filling the Table by Extrapolation

Filling a table by extrapolation fills the table with values based on the values already placed in the extrapolation mask. The extrapolation mask is described below. You can also choose to extrapolate automatically after filling cells in the mask in the "Feature Fill Wizard" on page 4-34.

To fill a table by extrapolating over a preselected mask, click Table > Extrapolate .

This extrapolation does one of the following:

- If the extrapolation mask has only one value, all the cell values change to the value of the cell in the mask.
- If the extrapolation mask has two or more colinear values, the cell values change to create a plane parallel to the line of values in the mask.
- If the extrapolation mask has three or more coplanar values, the cell values change to create that plane.
- If the extrapolation mask has four or more ordered cells (in a grid), the extrapolation routine fills the cells by a grid extrapolation.
- If the extrapolation mask has four or more unordered (scattered) cells, the extrapolation routine fills the cell values using a thin plate spline interpolant (a type of radial basis function).


## Using the Extrapolation Mask

The extrapolation mask defines a set of cells that form the basis of any extrapolation.

For example, a speed-load (or relative air charge) table has values in the following ranges that you consider to be accurate:

- Speed 3000 to 5000 rpm
- Load 0.4 to 0.6

You can define an extrapolation mask to include all the cells in these ranges. You can then fill the rest of your table based on these values.

To add or remove a cell from the extrapolation mask,
1 Right-click the table.

## 2 Select Add To Extrapolation Mask or Remove From Extrapolation Mask from the menu.

Cells included in the extrapolation mask are colored yellow.

## Creating a Mask from the Boundary Model or Predicted Error

You can automatically generate an extrapolation mask based on the boundary model or prediction error. Prediction error (PE) is the standard deviation of the error between the model and the data used to create the model.

To generate a mask automatically,

## 1 Select Table > Extrapolation Mask > Generate From Boundary Model or Generate From PE

2 If you select PE, a dialog appears where you must set the PE threshold to apply, and click OK.

The cells in the table either within the boundary model or where the prediction error is within the threshold now form the extrapolation mask, and thus are colored yellow.

## Calibrating the Feature Node

Selecting a Feature node displays the Feature view. For more information about the Feature view, see "Feature View" on page 4-41.

The Feature view enables you to calibrate the entire feature, that is, fill all the table values by referring to a model.

To calibrate the feature, either click the buttons on the toolbar, $\succeq \mathbb{E}^{\text {, or }}$ select from the following options on the Feature menu described in these sections:

1 "Initializing the Feature" on page 4-32
2 "Feature Fill Wizard" on page 4-34

## Initializing the Feature

For example, a simple feature for maximum brake torque (MBT) consists of the following tables:

- A speed ( $N$ ), load ( $L$ ) table
- A table to account for the behavior of air/fuel ratio $(A)$

Initializing this feature sets the values of the normalizers for speed, load, and AFR over the range of each variable and put specified values into each cell of the two tables.

A table that is already initialized provides a useful starting point for a more detailed calibration.

To initialize the feature, perform the following steps:

1 Click $\vDash$. This opens the Feature Initialization Options dialog box, as shown.


2 Enter the ranges for the breakpoints in your normalizers. In the preceding example, these are the breakpoint ranges:

- L has range 0.20 .811 .
- N has range 7506500 .
- A has range 11 17.6.

3 Enter the initial table value for each cell in each table. Above, the cell values are

- Table_NL has initial value 0.
- Fn_A has initial value 0 .

4 Click OK to initialize the feature.

Note The default values in this dialog box are taken from the variable dictionary. If you clear any Enable box, the associated table or normalizer is left unchanged.

## Feature Fill Wizard

Use the Feature Fill Wizard to fill and optimize the values in tables by reference to the model. You can fill multiple tables at once using the wizard, and you can Fill from the top feature node or from any table node in a feature.

Note you could also optimize the breakpoints for the normalizers before using the Feature Fill Wizard. (See "Filling Breakpoints" on page 4-13 and "Optimizing Breakpoints" on page 4-17.)

This section describes how to use the Feature Fill Wizard. For a detailed description about the filling processes, see "Filling Table Values" on page 4-26.

To fill feature tables, perform the following steps:

1 Click ${ }^{\Sigma}$. This opens the Feature Fill Wizard.


Screen 1: Select tables to fill.
Select the check boxes of the tables you want to fill. For each table you can set the following options:

- Clear Mask - select this check box to clear any table mask and fill all unlocked table cells (locked cells are never altered). Clear this check box to fill unlocked cells in the current extrapolation mask only, or all unlocked cells if there is no mask.
- Extrapolate - select this to extrapolate across the whole table after filling cells. The extrapolation is based on the filled cells in the mask and any locked cells.
- Table Bounds - enter values here to set bounds on the table values
- Gradient Bounds - enter values here to set bounds on the gradient (slope) between rows (left edit box) and between columns (right edit box). For example, entering 0 Inf in the left edit box imposes the constraint that the gradient must be positive (increasing) between successive rows. When you have selected filling options for each table, click Next.

2 Choose models and links.


- Click Select Model to choose a model to fill the tables from. The feature filler adjusts the table cells so that the value of the feature across the range of inputs best matches the value of this model.
- Click Select Constraint to choose a constraint to use in the filling process. You can use Linear, 1-D table, 2-D table, ellipsoid and model constraints (see "Constraint Editor" on page 6-27). The feature filler limits its activity to within this constraint, for example, the boundary constraint of a model. While boundary models are often used as model constraints in this setting you can use any model. For example, you can use a function that returns a logical output (true for valid, false for invalid) by setting up the model constraint $>=0.5$.
- Click Link to associate a model, feature or table (selected on the right side) with a variable (selected on the left side). Linking replaces the variable inputs to any relevant models and features with the linked item. This enables useful operations such as feeding a table into a model, for example, an optimal cam schedule into a torque model, without needing
to make a separate function model. Click Unlink to disassociate any pair.
Click Next.
3 Set variable values.
By default the table's normalizer breakpoints and the set points of other variables are selected, so the number of grid points is the number of table cells. To increase the grid size you can enter more points for variables by editing the Value fields, or you can interleave values between breakpoints (see below). Increasing the number of grid points increases the quality of the approximation and minimizes interpolation error, but also increases the computation time.

- You can edit normalizers manually, or you can click the Initialize From Normalizer button to reach a dialog box where you can select normalizers and interleave values between breakpoints. Interleaving values can minimize interpolation error by adding values between each normalizer value. In this way you can create a grid of more points than table cells to optimize over. Select normalizers in the dialog box to use those breakpoints as a variable's value.

In this dialog box, you can enter a value in the Number of values between breakpoints edit box to add values between breakpoints. By default, the feature filler compares the feature and model at the table breakpoints. Choose a positive value to compare the feature and model on a finer grid. A positive value further enhances the comparison between feature and model to account also for errors introduced by linear interpolation in the table (see "Optimizing Table Values" on page 4-26). A value of 1 inserts one grid point between each pair of breakpoints, and so on. Click OK to return to the Feature Fill Wizard.

- Edit set point values in the Value fields to optimize over a range rather than at a single point. If you choose a range of values the table will be filled using the average model value at each cell. For example, if you enter -5:5:50 for the variable spark, the optimization of table values will be carried out at values of spark between -5 and 50 in steps of 5 degrees.


## Click Next.

4 Fill Tables. Click Fill Tables to fill the tables.
CAGE evaluates the model over the number of grid points specified, then calculates the total square error between this mesh model and the feature values. CAGE adjusts the table values until this error is minimized, using lsqnonlin if there are no gradient constraints, otherwise fmincon is used with linear constraints to specify the gradient of the table at each cell.

The graph shows the change in RMSE as the optimization progresses.


- You can enter a value in the Smoothing edit box to apply a smoothing penalty to the optimization. The Smoothness penalty uses the second derivative to avoid steep jumps between adjacent table values. There is a penalty as smoothing trades smoother tables for increased error. Enter a smoothing factor ( $0-$ Inf) and click Fill Tables to observe the difference in the resulting RMSE and the table shape. Keep increasing the value until you reach the required smoothness. If you go too far the results will be a flat plane.
- Select the check boxes to display plots when you close the Wizard. You can see plots of error against all the variables (Plot), error between feature and model (Error), table surface and error surface.
- Select the check box to create a dataset containing the output values at each specified grid point.

You can click Back to return to previous screens and fill more tables, or you can click Finish. When you click Finish to dismiss the wizard, the plots with selected check boxes appear.

When you have completed a calibration, you can export your feature. For information, see "Importing and Exporting Calibrations" on page 3-46.

## Feature View

As you select a Feature node you see the Feature view, shown. This section describes the Feature view and the Feature menu options.


The parts of the Feature view include
1 The strategy for the selected feature. This is the algebraic collection of the tables that you are using to calibrate the selected feature.

2 The model associated with the selected feature.
3 The Feature History pane, which displays the history of the feature.

## Feature Menu

The Feature menu has the following options:

## - Select Model

Use this to select the correct model for your feature.

- Deselect Model

Use this to clear the current model from your feature.

- Convert to Model

Takes the current feature and converts it to a model, which you can view by clicking the Model button.

- Graphical Strategy Editor

Opens your current strategy for editing. For more information, see "Setting Up Your Strategy" on page 4-6.

## - Parse Strategy Diagram

Performs the same function as double-clicking the blue outport of your strategy diagram. For more information, see "Setting Up Your Strategy" on page 4-6.

## - Clear Strategy

Clears the current strategy from your feature.

- Initialize

Initializes the feature; also in the toolbar. See "Initializing the Feature" on page 4-32 for details.

- Fill

Fills and optimizes the feature; also in the toolbar. See "Feature Fill Wizard" on page 4-34 for details.

## Tradeoff Calibrations

This section includes the following topics:

Performing a Tradeoff Calibration (p. 5-2)

Setting Up a Tradeoff Calibration (p. 5-5)

Calibrating Tables in a Tradeoff Calibration (p. 5-10)

Using Regions (p. 5-21)

Multimodel Tradeoffs (p. 5-23)

Automated Tradeoff (p. 5-30)

An overview of the steps required for tradeoff calibration.

How to set up a new tradeoff, add tables, and display models.
An overview of how to calibrate tables in a tradeoff calibration; setting values for other variables and determining suitable values at specific operating points.

How to use regions to fill specific parts of your table by extrapolation.

How to set up and use multimodel tradeoffs.

How to use optimizations to automate tradeoff calibrations.

## Performing a Tradeoff Calibration

## A <br> A <br> Tradeoff

A tradeoff calibration is the process of calibrating lookup tables by adjusting the control variables to result in table values that achieve some desired aim.

For example, you might want to set the spark angle and the air/fuel ratio (AFR) to achieve the following objectives:

- Maximize torque
- Restrict CO emissions

The data in the tradeoff is presented in such a way as to aid the calibrator in making the correct choices. For example, sometimes the model is such that only a slight reduction in torque results in a dramatic reduction in CO emissions.

The basic procedure for performing tradeoff calibrations is as follows:
1 Set up the variables and constants. (See "Setting Up Variable Items" on page 2-3.)

2 Set up the model or models. (See "Setting Up Models" on page 2-11.)
3 Set up the tradeoff calibration. (See "Setting Up a Tradeoff Calibration" on page $5-5$.)

4 Calibrate the tables. (See "Calibrating Tables in a Tradeoff Calibration" on page 5-10.)

5 Export the normalizers, tables, and tradeoffs. (See "Exporting Calibrations" on page 3-47.)

You can also use regions to enhance your calibration. (See "Using Regions" on page 5-21.)

See also

- "Tutorial: Tradeoff Calibration" in the Getting Started documentation. This is a tutorial giving an example of how to set up and complete a simple tradeoff calibration.
- "Automated Tradeoff" on page 6-87 is a guide to using the optimization functionality in CAGE for tradeoffs.

The normalizers, tables, and tradeoff form a hierarchy of nodes, each with its own view and toolbar.


## Setting Up a Tradeoff Calibration

A tradeoff calibration is the process of filling lookup tables by balancing different objectives.

Typically there are many different and conflicting objectives. For example, a calibrator might want to maximize torque while restricting nitrogen oxides (NOX) emissions. It is not possible to achieve maximum torque and minimum NOX together, but it is possible to trade off a slight reduction in torque for a reduction of NOX emissions. Thus, a calibrator chooses the values of the input variables that produce this slight loss in torque instead of the values that produce the maximum value of torque.

A tradeoff also refers to the object that contains the models and tables. Thus, a simple tradeoff can involve balancing the torque output while restricting NOX emissions.

After you set up your variable items and models, you can follow the procedure below to set up your tradeoff calibration:

1 Add a tradeoff. This is described in the next section, "Adding a Tradeoff" on page 5-5.

2 Add tables to the tradeoff. This is described in "Adding Tables to a Tradeoff" on page 5-6.

3 Display the models. This is described in "Displaying Models in Tradeoff" on page 5-8.

This section describes steps 1,2 , and 3 in turn.
When you finish these steps, you are ready to calibrate the tables.

## Adding a Tradeoff

To add a tradeoff to your session, select File $>$ New $>$ Tradeoff. This automatically switches you to the Tradeoff view and adds an empty tradeoff to your session.

An incomplete tradeoff is a tradeoff that does not contain any tables. If a tradeoff is incomplete, it is displayed as 煰 in the tree display. If a tradeoff is complete, it is displayed as 閪 in the tree display.

After you add a tradeoff you must add tables to your tradeoff.

## Adding Tables to a Tradeoff

1 Add a table by selecting Tradeoff -> Add New Table or click in the toolbar. You can also add existing tables from your CAGE session; see "Adding Existing Tables" on page 5-8.

Note that you must select the top tradeoff node in the tree display to use the Tradeoff menu. This is automatically selected if your tradeoff has no tables yet (it is the only node). You must also add at least three variables (in the variable dictionary) to your project before you can add a table, because CAGE needs a variable to fill the table and two more variables to define each of the two normalizers.

A dialog box opens.


2 Enter the name for the table.
If your tradeoff already contains one or more tables, when you add additional tables they must be the same size and have the same inputs (and therefore have the same normalizers). So if your tradeoff has existing tables, you can only enter the new table name and the initial value.

For the first table in a tradeoff, you must set the normalizer inputs and sizes:
a Edit the names for the X and Y normalizer inputs (the first two variables in the current variable dictionary are automatically selected here).
b Enter sizes for each of the normalizers (Yinput = rows, X input = columns)
3 Enter an initial value to fill the table cells, or leave this at zero.
4 Click Select to choose a filling item for a table. A dialog opens where you can select from the models and variables in your session.

a Depending on what kind of input you want, click the radio buttons to display models or variables or both. You can choose to also show items that are filling another table by clearing the check box.
b Select the filling item for the table and click OK.
5 Click OK to dismiss the Table Setup dialog and create the new table.
CAGE adds a table node to the tradeoff tree. Note you can still change the input for the table as follows. Double-click the new table in the list under

Tables In Tradeoff, or click to select the table (it is selected automatically if it is the only table in the tradeoff) and then click Change Filling Item
 context menu.

The Select Filling Item dialog appears where you can select inputs to fill the table, as described above.

6 Repeat this procedure for each new table you want to add. Each additional table in the tradeoff must have the same normalizers as the first table, so you do not have to select normalizer inputs and sizes repeatedly. For each new table you only have to enter the name and initial value.

## Adding Existing Tables

1 Add a table by selecting Tradeoff > Add Existing Tables or click in the toolbar.

A dialog appears where you can select from a list of tables in the current session.

2 Select a table and click OK. It may be helpful to first select the check box to only show suitable tables that can be added to the tradeoff.

## Displaying Models in Tradeoff

To display models when viewing tables in the tradeoff display,
1 Highlight the tradeoff node in the tree.
2 From the Available Models list, select the one you want to display.
Models that are filling a table are automatically displayed.
3 Click Add Model to Display List in the toolbar or $>$ in the Additional Display Models pane to move the selected model into the Display Models pane. To quickly add all available models to the display list, click the display button repeatedly and each successive model will be added.

4 Repeat steps 2 and 3 to add all the models you want to the display list.


## Removing a Model

1 In the Display Models list, select the model that you want to remove.
2 Click $\frac{+4}{}$ in the toolbar, or $<$ in the Display Models pane, to move the selected model into the Available Models pane.

3 Repeat until you have cleared all the appropriate models.
Once you have displayed all the models that you want to work with, you are ready to calibrate your tables.

## Calibrating Tables in a Tradeoff Calibration

Selecting a table node in the tree display enables you to view the models that you have displayed and calibrate that table.

To calibrate the tables,
1 Select the table that you want to calibrate.
2 Highlight one operating point from the table.
3 Set the values for other input variables.
For information, see "Setting Values of Other Variables" on page 5-13.
4 Determine the value of the desired operating point.
For instructions, see "Determining a Value at a Specific Operating Point" on page 5-15.

5 Click to apply this value to the lookup table.
This automatically adds the point to the extrapolation mask.
6 Repeat steps 2, 3, 4, and 5 at various operating points.
7 Extrapolate to fill the table by clicking in the toolbar.
For information, see "Filling the Table by Extrapolation" on page 4-30.

After you complete all these steps you can export your calibration. For information, see "Exporting Calibrations" on page 3-47.

## Table View in a Tradeoff Calibration



Notice that the graphs colored green indicate how the highlighted table will be filled:

- If a row of graphs is highlighted, the table is being filled by the indicated model evaluation (the value shown at the left of the row).
- If the column of graphs is green, the table is being filled by the indicated input variable (shown in the edit box below the column).

The next sections describe the following in detail:

- "Setting Values of Other Variables" on page 5-13
- "Determining a Value at a Specific Operating Point" on page 5-15


## Setting Values of Other Variables

Typically the models that you use to perform a tradeoff calibration have many inputs. When calibrating a table of just one input, you need to set values for the other inputs.


## Setting Values for Individual Operating Points

To set values for inputs at individual operating points,
1 Highlight the operating point in the lookup table.
2 Use the edit boxes or drag the red bars to specify the values of the other variables.

In the preceding example, the spark table is selected (the SPK graph is colored green). You have to specify the values of AFR (A) and EGR (E) to be used, for example:

1 Select the spark table node.
2 Click in the edit box for A and set its value to 14.3.
3 Click in the edit box for E and set its value to 0 .
The default values are the set points of variables, which you can edit in the Variable Dictionary.

## Setting Values for All Operating Points

For example, if you are using a tradeoff to calibrate a table for spark angle, you might want to set the initial values for tables of air/fuel ratio (AFR) and exhaust gas recycling (EGR).

To set constant values for all the operating points of one table,
1 Highlight the table in the tree display.
2 Select one operating point in the table.
3 Enter the desired value of the cell.
4 Right-click and select Extrapolation Mask > Add Selection.
This adds the cell to the extrapolation mask.
5 Click to extrapolate over the entire table.
This fills the table with the value of the one cell.

## Determining a Value at a Specific Operating Point



Performing a tradeoff calibration necessarily involves the comparison of two or more models. For example, in this case, the tradeoff allows a calibrator to check that a value of spark that gives peak torque also gives an acceptable value for the NOX flow model.

1 To select a value of an input, do one of the following:

- Drag the red line.
- Right-click a graph and select Find the minimum, maximum, or turning point of the model as appropriate (also in the toolbar and Inputs menu).
- Click the edit box under the graph as shown above and enter the required value.

2 Once you are satisfied with the value of your variable at this operating point, you apply this value to the table by doing one of the following:

- Press Ctrl+T.
- Click (Apply Table Filling Values) in the toolbar.
- Select Tables > Apply > Fill to Table.


## Right-Click Menu

Right-clicking a graph enables you to

- Find minimum of model output with respect to the input variable
- Find maximum of model output with respect to the input variable
- Find turning point of model with respect to the input variable

These first three options are also in the Inputs menu.

- Reset graph zooms (also in the View menu)

There are also toolbar buttons to find the minimum, maximum and turning point of the selected model graph.

## Using Zoom Controls on the Graphs

To zoom in on a particular region, shift-click or click with both mouse buttons simultaneously and drag to define the region as a rectangle.

To zoom out to the original graph, double-click the selected graph, or use the right-click Reset Graph Zooms option (also in the View menu).

Note Zooming on one graph adjusts other graphs to the same scale.

## Tradeoff Table Menus

## View Menu

Selecting the View menu offers you the following options:

## - Table History

This opens the History display. For information, see "Using the History Display" on page 3-16.

## - Configure Hidden Items

This opens a dialog box that allows you to show or hide models and input variables. Select or clear the check boxes to display or hide items. This is particularly useful if you are trading off a large number of models or models that have a large number of factors.

## - Display Confidence Intervals

When you select this, the graphs display the $99 \%$ confidence limits for the models.

## - Display Common Y Limits

Select this to toggle a common $y$-axis on and off for all the graphs. You can also press CTRL+Y as a shortcut to turn common Y limits on and off.

## - Display Constraints

Select this to toggle constraint displays on and off. Regions outside constraints are shown in yellow on the graphs, as elsewhere in the toolbox.

## - Graph Size

Select from the following options for number and size of graphs:

- Display All Graphs
- Small
- Medium
- Large
- Large Graph Headers

Select this to toggle graph header size. The smaller size can be useful when you need to display many models at once.

## - Reset Graph Zooms

Use this to reset if you have zoomed in on areas of interest on the graphs. Zoom in by shift-clicking (or clicking both buttons) and dragging. You can also reset the zooms by double-clicking, or by using the right-click context menu on the graphs.

## - Display Table Legend

Select this to toggle the table legend display on and off. You might want more display space for table cells once you know what the legend means. The table legend tells you how to interpret the table display:

- Cells with a tick contain saved values that you have applied from the tradeoff graphs (using the 'Apply table filling values' toolbar or menu option).
- Yellow cells are in the extrapolation mask.
- Blue cells are in a region mask.
- Yellow and blue cells with rounded corners are both in a region and the extrapolation mask.
- Cells with a padlock icon are locked.


## Tables Menu

## - Apply Fill to Table

Select this option to apply the values from the tradeoff graphs to the selected table cell. This option is also in the toolbar, and you can use the keyboard shortcut CTRL+T.

Note that the corresponding cell in all tables is filled with the appropriate input, not just the cell in the currently displayed table. For example if you have graphs for spark and EGR inputs, selecting Apply Fill to Table fills the spark table cell with the spark value in the graphs, and the EGR table cell with the EGR value.

- Extrapolation Mask - Also available in the toolbar and the context menu (by right-clicking a table cell). Use these options to add and remove cells from the mask for filling tables by extrapolation. Note that cells filled by applying values from the tradeoff graphs (using the Apply Fill To Table toolbar and menu option) are automatically added to the extrapolation mask.
- Add Selection
- Remove Selection
- Clear Mask
- Extrapolation Regions - Also available in the toolbar and the context menu (by right-clicking a table cell). Use these options to add and remove cells from regions. A region is an area that defines locally where to extrapolate before globally extrapolating over the entire table. Use regions to define high-priority areas for use when filling tables by extrapolation. See "Using Regions" on page 5-21.
- Add Selection
- Remove Selection
- Clear Regions
- Extrapolate - This option (also in the toolbar) fills the table by extrapolation using regions (to define locally where to extrapolate before globally extrapolating) and the cells defined in the extrapolation mask.
- Extrapolate (Ignore Regions) - This option fills the table by extrapolation only using cells in the extrapolation mask.
- Table Cell Locks - Also available in the context menu by right-clicking a table cell. Use these options to lock or unlock cells; locked cells are not changed by extrapolating.
- Lock Selection
- Unlock Selection
- Lock Entire Table
- Clear All Locks


## Inputs Menu

- Reset to Last Saved Values - This option resets all the graph input values to the last saved value. Also in the toolbar.
- Set to Table Value - This option sets the appropriate input value on the graphs to the value in the table.
The following three options are only enabled if a graph is selected (click to select, and a blue frame appears around the selected graph). They are also available in the right-click context menu on the graphs.
- Find Minimum of model vs input factor
- Find Maximum of model vs input factor
- Find Turning Point of model vs input factor
where model and input factor are the model and input factor displayed in the currently selected graph, for example, TQ_model vs Spark.
- Automated Tradeoff - Use this option once you have set up an optimization, to apply that optimization to the selected region of your tradeoff table. See "Automated Tradeoff" on page 6-87 for information.


## Tools Menu

- Calibration Manager - opens the Calibration Manager. See "Calibration Manager" on page 3-20.
- Surface Viewer - Opens the Surface Viewer. See Chapter 8, "Surface Viewer".


## Using Regions

A region is an area that defines locally where to extrapolate before globally extrapolating over the entire table.

For example, consider filling a large table that has twenty breakpoints for each normalizer by extrapolation. Two problems arise:

- To have meaningful results, you need to set values at a large number of operating points.
- To set values at a large number of operating points takes a long time.

To overcome this problem, you can
1 Define regions within the lookup table.
2 In each region, set the values of some operating points.
3 Click to fill the table by extrapolation.
Each region is filled by extrapolation in turn. Then the rest of the table is filled by extrapolation. The advantage of using regions is that you can have more meaningful results by setting values for a smaller number of operating points.


Cells are colored

- Yellow if they form part of the extrapolation mask
- Blue if they are part of a region
- Yellow and blue with rounded corners if they are part of the extrapolation mask and part of a region


## Defining a Region

1 Click and drag to highlight the rectangle of cells in your table.
2 To define the region, click $\square_{+}$in the toolbar, or right-click and select Extrapolation Regions > Add Selection, or select the menu option Tables > Extrapolation Regions > Add Selection.
The cells in the region are colored blue.

## Clearing a Region

1 Highlight the rectangle of cells in your table.
2 To clear the region, click ${ }^{\square}$ in the toolbar, or right-click and select Extrapolation Regions > Remove Selection, or select the menu option Tables > Extrapolation Regions > Remove Selection.

You can clear all regions at once by selecting Clear Regions from the Extrapolation Regions submenu.

## Multimodel Tradeoffs

There are two types of tradeoff that you can add to your session, a tradeoff of independent models, as described earlier (see "Performing a Tradeoff Calibration" on page 5-2), or a tradeoff of interconnected models (a multimodel tradeoff).

A multimodel tradeoff is a specially built collection of models from the Model Browser.

You can build a series of models so that each operating point has a model associated with it. In the Model Browser, you can export models for a multimodel tradeoff from the test plan node. The models must be two-stage and must have exactly two global inputs.

The procedure for calibrating by using a multimodel tradeoff follows:
1 Add the multimodel tradeoff. (See the following section, "Adding a Multimodel Tradeoff" on page 5-24.)

2 Calibrate the tables. (See "Calibrating Using a Multimodel Tradeoff" on page 5-27.)

3 Export your calibration. (See "Importing and Exporting Calibrations" on page 3-46.)

The multimodel is only defined for certain cells in the tradeoff tables. These are the operating points that were modeled using the Model Browser part of the toolbox. These cells have model icons in the table. At each of these operating points, you can use the model to trade off, and by doing this you can adjust the value in the table. The multimodel is not defined for all other cells in the table and so you cannot use models to tradeoff. You can edit these cells and they can be filled by extrapolation. You trade off values at each of the model operating points in exactly the same way as when using independent models, as described in "Determining a Value at a Specific Operating Point" on page $5-15$. When you have determined table values at each of the model operating points, you can fill the whole table by extrapolation by clicking 通。 See "Filling the Table by Extrapolation" on page 4-30.

## Adding a Multimodel Tradeoff

To add a multimodel tradeoff to your session,
1 Select File > New > Tradeoff. CAGE switches to the tradeoff view and creates a new empty tradeoff.

2 Select the new tradeoff in the tree, then select File > Import > Multimodel Tradeoff.

The file must have been exported from the MBC Model Browser using the Tradeoff button (only enabled for two-stage models with exactly two global inputs). See "Multimodel Tradeoffs" on page 5-23.

3 Select the correct file to import and click Open. This opens a dialog box.


4 In the left Model sites list, you can clear the check boxes for any models at operating points that you do not want to import.

Notice that the operating points are displayed graphically at the top. If an operating point is deselected, it is displayed as gray here, rather than blue.

CAGE will create tables for all the models and input variables, with breakpoints at all the model operating points. You can choose not to create
all the tables; click Select Tables to choose from the list which tables you want.

5 Choose the normalizers (axes) of the tables by using the $X$ - and $Y$-axis input drop-down menus.

6 You can adjust the number of breakpoints in the following ways:

- Leave the Automatic breakpoint settings radio button selected and edit the relative tolerances around the model sites. Use the tolerance edit boxes in the model setup pane. You can observe the effects of altering the tolerances on the number of breakpoint dotted lines drawn on the top graphic. Initially each model site has a breakpoint. If operating points are close together, you can increase the tolerances to decrease the number of breakpoints.

For example, if several close points may all have been intended to run at exactly the same point, you might want to adjust the tolerances until those model points (displayed as blue dots) only have one breakpoint line. The number of rows and columns that will be created is displayed in the edit boxes on the right.

- Alternatively you can select the Manual breakpoint settings radio button and enter the number of rows and columns in the edit boxes, and you can directly edit the values of the breakpoints.


## 7 Click OK.

When you click OK, CAGE creates all the tables for the multimodel tradeoff, with breakpoints at the values you have selected.

Note When you calibrate the tables, you can only use models to tradeoff at the operating points defined for the models. These cells have model icons in the table. You can edit other cells, but they have no models to tradeoff associated with them.

You can now calibrate your tables. See the next section, "Calibrating Using a Multimodel Tradeoff" on page 5-27.

## Calibrating Using a Multimodel Tradeoff

Each editable operating point in your tables has a model icon in the cell, like this example cell.

```
4602.722
```

These cells have a model defined at that point. You use the display of these models to help you trade off values at these points to fulfill your aims in exactly the same way as when using independent models in "ordinary" tradeoff mode, as described in "Determining a Value at a Specific Operating Point" on page 5-15.

1 Change input values by dragging the red lines on the graphs or by typing directly into the edit boxes above the graphs. Use the context menu, toolbar or Inputs menu to find the maximum, minimum, or turning point of a model if appropriate.

2 Look at the model evaluation values (to the left of each row of graphs) and the input variable values (in the edit boxes below the graphs) to see if they meet your requirements.

Remember that the green highlighted graphs indicate how the selected table is filled: if a row is green, the model evaluation value (to the left) fills the table at that operating point; if a column is green, the input variable value (in the edit box below) fills the table.

See the example following; the SPK column of graphs is green, so the value of SPK in the edit box is entered in the table when you click the Apply Table Filling Values button (点) 。


3 When you are satisfied with the tradeoff given by the value of your variable at this operating point, you apply this value to the table by pressing Ctrl+T, selecting Tables -> Apply Fill to Table, or clicking in the toolbar.

4 When you have determined table values at each of the model operating points, you can fill the whole table by extrapolation by clicking "Filling the Table by Extrapolation" on page 4-30.

You can then export your calibration; see "Importing and Exporting Calibrations" on page 3-46. An example multimodel tradeoff is shown following.


## Automated Tradeoff

You can use automated tradeoff to run an optimization routine and fill your tradeoff tables. Once you have set up an optimization you can run an automated tradeoff. As with any other tradeoff you need at least one table. You can apply an optimization to a cell or region of a tradeoff table and the tradeoff values found are used to fill the selected cells. You can then fill the entire table by extrapolation.

You must first set up an optimization to use automated tradeoff.
See "Automated Tradeoff" on page 6-87 in the Optimization section for instructions.

## Optimization

This section includes the following topics:
$\left.\left.\begin{array}{ll}\text { Using the Optimization View (p. 6-3) } & \begin{array}{l}\text { An introduction to setting up your } \\ \text { session for optimizations. }\end{array} \\ \text { Optimization Problems You Can } & \begin{array}{l}\text { Examples of the optimization } \\ \text { problems that can be solved in CAGE } \\ \text { and links to instructions for setting } \\ \text { up optimizations }\end{array} \\ \text { Solve with CAGE (p. 6-5) }\end{array} \quad \begin{array}{l}\text { Steps to set up point-by-point } \\ \text { optimizations with links to } \\ \text { instructions. }\end{array}\right] \begin{array}{l}\text { You use the Optimization Wizard } \\ \text { Setting Up Point-by-Point } \\ \text { Optimizations (p. 6-8) } \\ \text { Creating an Optimization (p. 6-9) } \\ \text { choosing your algorithm, algorithm } \\ \text { options, and free variables. You can } \\ \text { set up objectives and constraints } \\ \text { either in the wizard or from the main }\end{array}\right\}$
\(\left.$$
\begin{array}{ll}\text { Running Optimizations (p. 6-41) } & \begin{array}{l}\text { How to run optimizations, and } \\
\text { configure the Optimization } \\
\text { Parameters dialog box. }\end{array} \\
\text { Optimization Output View (p. 6-50) } & \begin{array}{l}\text { Using the optimization output views } \\
\text { to investigate your results and select } \\
\text { and export your preferred solutions. }\end{array} \\
\text { Automated Tradeoff (p. 6-87) } & \begin{array}{l}\text { How to apply an optimization to a } \\
\text { tradeoff table. }\end{array} \\
\text { User-Defined Optimization (p. 6-91) } & \begin{array}{l}\text { An overview of the process of } \\
\text { customizing the optimization } \\
\text { template to use your own }\end{array}
$$ <br>

optimization routines in CAGE.\end{array}\right\}\)| Optimization Function Reference |
| :--- |
| (p. 6-98) |
| Information on all the methods |
| available for writing your own |
| optimization functions. |

## Using the Optimization View

Optimization functionality is one of the CAGE processes. The Optimization button can be found in the left-hand Processes pane.

button.
Here you can set up and view optimizations. As with other CAGE processes, the left Optimization pane shows a tree hierarchy of your optimizations, and the right panes display details of the optimization selected in the tree. When you first open the Optimization view both panes are blank until you create an optimization.

As for other CAGE processes, you must set up your session for an optimization. For any optimization, you need one or more models. You can run an optimization at a single point, or you can supply a set of points to optimize. The steps required are

1 Import a model or models.
2 Set up a new optimization.

Optimization functionality in CAGE is described in the following sections:

- "Optimization Problems You Can Solve with CAGE" on page 6-5
- The steps for setting up and running optimizations are described in these sections:
- "Creating an Optimization" on page 6-9
- "Setting Up Point-by-Point Optimizations" on page 6-8
- "Setting Up Sum Optimizations" on page 6-32
- "Objectives and Constraints" on page 6-24
- "Running Optimizations" on page 6-41
- "Using the Optimization Parameters Dialog Box" on page 6-42
- "Optimization Output View" on page 6-50 describes using the views to analyze your results.
- After you set up an optimization, you can apply it to a region in a set of tradeoff tables. See "Automated Tradeoff" on page 6-87
- You can define your own optimization functions for use in CAGE. See "User-Defined Optimization" on page 6-91

There are tutorial examples to guide you through the optimization functionality. See "Tutorial: Optimization and Automated Tradeoff", and see the optimization sections in "Gasoline Case Study" and "Diesel Case Study", in the Getting Started documentation.

## Optimization Problems You Can Solve with CAGE

CAGE provides a flexible optimization environment in which many automotive optimization problems can be solved. These problems can be divided into two main groups:

- "Point-by-Point Optimization Problems" on page 6-5
- "Sum Optimization Problems" on page 6-6


## Point-by-Point Optimization Problems

In a point-by-point problem, a single optimization run can determine optimal control parameter values at a single operating point. To optimize control parameters over a set of operating points, an optimization can be run for each point.

Examples of point-by-point problems that CAGE can be used to solve are described below:

- Find the optimal spark timing (SPK), intake valve timing (INTCAM) and exhaust valve timing (EXHCAM) at each point of a lookup table whose axes are engine speed ( N ) and relative load (L).

Optimized values of the control parameters are determined by running the following optimization at each point of the lookup table:

Objective: Maximize engine torque, TQ = TQ(N, L, SPK, EXHCAM, INTCAM)

Constraints:

- Residual fraction $<=17 \%$ at each (N, L) operating point
- Exhaust temperature $<=1290^{\circ} \mathrm{C}$ at each (N, L) operating point
- Engine to be operated inside the operating envelope of the engine
- Find the optimal mass of fuel injected (F), rail pressure (P), pilot timing (PT) and main timing (MT) at each point of a lookup table whose axes are engine speed ( N ) and engine torque ( TQ ).

Optimized values of the control parameters are determined by running the following optimization at each point of the lookup table:

Objective: Minimize brake specific fuel consumption, $\operatorname{BSFC}=\operatorname{BSFC}(N, T Q)$
Constraints:

- Engine out NOx $<=0.001 \mathrm{~kg} / \mathrm{s}$ at each (N, TQ) operating point
- Engine out Soot emissions $<=0.0001 \mathrm{~kg} / \mathrm{s}$ at each (N, TQ) operating point
- Find the optimum spark timing (SPK) and exhaust gas recirculation (EGR) at each point of a set of operating points defined by engine speed (N), engine load (L) pairs. Optimized values of SPK and EGR are determined by running the following optimization at each point:

Objective: Maximize engine torque, TQ = TQ(N, L, SPK, EGR)
Constraints: Engine out NOx <= $400 \mathrm{~g} / \mathrm{hr}$ at each (N, L) operating point

- For a new engine, find out the optimal torque versus NOx emissions curve for this engine over the operating range of the engine. This is a multi-objective optimization, and CAGE Optimization contains an algorithm (NBI) to solve these problems.

For this example, the optimal torque-NOx curve is determined by solving the following optimization problem for optimal settings of spark timing (SPK) and exhaust gas recirculation (EGR):

Objectives:

- Maximize engine torque, TQ = TQ(N, L, SPK, EGR)
- Minimize engine out $\mathrm{NOx}=\mathrm{NOx}(\mathrm{N}, \mathrm{L}, \mathrm{SPK}, \mathrm{EGR})$

To find out more about solving these types of problems in CAGE, see "Setting Up Point-by-Point Optimizations" on page 6-8.

## Sum Optimization Problems

In a sum optimization, a single optimization run can determine the optimal value of control parameters at several operating points simultaneously. All the control parameters for the operating points are optimized by calling the algorithm once (there's only one call to foptcon per run for a sum optimization). This approach contrasts with a point-by-point optimization, which has to make a call to the algorithm for every point to find the optimal settings of the control parameters.

- Find the optimal spark timing (SPK), intake valve timing (INTCAM) and exhaust valve timing (EXHCAM) at each point of a look-up table whose axes are engine speed ( N ) and relative load (L).

Optimized values of the control parameters are determined by running the following optimization once:

Objective: Maximize weighted sum of engine torque, $\mathrm{TQ}=\mathrm{TQ}(\mathrm{N}, \mathrm{L}, \mathrm{SPK}$, EXHCAM, INTCAM) over the ( $\mathrm{N}, \mathrm{L}$ ) points of a look-up table.

Constraints:

- Difference in INTCAM between adjacent cells is no greater than $5^{\circ}$.
- Difference in EXHCAM between adjacent cells is no greater than $10^{\circ}$.
- At each table cell, residual fraction $<=17 \%$
- At each table cell, exhaust temperature $<=1290^{\circ} \mathrm{C}$
- Find the optimal start of injection (SOI), basefuelmass (BFM), fuel pressure (P), turbo position (TP) and lift of the EGR valve (EGR) at a set of mode points defined by engine speed (N), engine torque (TQ) pairs.

Optimized values of the control parameters are determined by running the following optimization once:

Objective: Maximize weighted sum of brake specific fuel consumption, BSFC = BSFC(SOI, BFM, P, TP, EGR, N, TQ) over the (N, TQ) mode points.

Constraints:

- Weighted sum of brake specific NOx must be less than a legislated maximum
- At each mode point, air fuel ratio must be greater than a specified minimum
- At each mode point, turbo speed must not exceed a specified maximum

To find out more about solving these types of problems in CAGE, see "Setting Up Sum Optimizations" on page 6-32.

## Setting Up Point-by-Point Optimizations

Use the following process to set up a point-by-point optimization:
1 Use the "Optimization Wizard" on page 6-9 to create your optimization.
It is optional whether you set up your objectives in the wizard or later in the Optimization view.

2 For simple model constraints it is optional whether you set them up in the wizard or later in the Optimization view. To apply other types of constraints (more flexible model constraints, linear, ellipsoid, 1-D table, 2-D table, and range) you must use the Optimization view. See "Constraint Editor" on page 6-27 for details of all these constraints.

3 Set variable values for the points where you want the optimization to run. See "Defining Variable Values" on page 6-18. You can enter values manually or by importing from data sets or the output of existing optimizations.

4 Run the optimization. See "Running Optimizations" on page 6-41.
5 View the results. See "Optimization Output View" on page 6-50).

## Creating an Optimization

To create a new optimization, select File > New > Optimization.
This takes you to the Optimization Wizard (described below), which leads you through the steps of choosing the optimization to run, specifying the number of variables to optimize over (unless this is predefined by the function), and linking the variables referenced in the optimization to CAGE variables.

## Optimization Wizard

You use the Optimization Wizard to:
1 Choose algorithm
2 Set up free variables, objectives, and constraints options - "Optimization Wizard Step 2" on page 6-11

3 Select free variables - "Optimization Wizard Step 3" on page 6-13
The last 3 steps you can do in the wizard or in the Optimization view:
4 Set up objectives - "Optimization Wizard Step 4" on page 6-14
5 Set up model constraints - "Optimization Wizard Step 5" on page 6-15
6 Set up data sets (user-defined optimizations only) - "Optimization Wizard Step 6" on page 6-16

Step 1. First you must choose your algorithm. The first screen of the Optimization Wizard is shown below.

Optimization Wizard

## Algorithm Selection

Select from the list the algorithm that you want the new optimization to use.


The first two algorithm choices in the list are standard routines you can use for constrained single and multiobjective optimization.

- foptcon is a single-objective optimization subject to constraints. This function uses the MATLAB fmincon algorithm from the Optimization Toolbox.
- NBI stands for Normal Boundary Intersection algorithm, which is multiobjective and can also be subject to constraints.

In many cases these standard routines are sufficient to allow you to solve your optimization problem. Sometimes, however, you might need to write a customized optimization algorithm; to do this you can use the supplied template to modify for your needs. Any optimization functions that you have checked into CAGE appear in this list. See "User-Defined Optimization" on page 6-91 for information. The Worked Example option is designed to show you how to use the modified template. For step-by-step instructions, see the optimization tutorial section "Worked Example Optimization" in the Getting Started documentation.

Note If you choose a user-defined optimization function at step 1, all choices in subsequent steps depend on the settings defined by that function. When writing user-defined optimizations you can choose to set predetermined algorithm options or allow the user to make selections on any subsequent screen of the Optimization Wizard.

## Optimization Wizard Step 2

Here you select algorithm options for numbers of free variables, objectives, and constraints. The optimization tries to find the best values of the free variables. The options available depend on your selected algorithm.

- If in step 1 you select the foptcon algorithm and click Next, you get the following choices:


The foptcon algorithm can only have a single objective, so this control is not enabled. Choose the number of free variables and constraints you require. You can also add constraints later.

- If in step 1 you select the algorithm NBI, and click Next, you see this:

Dptimization Wizard

## Algorithm Options

Algorithms may be able to use a variable number of items. Select the number of each item that you want to use in this optimization.

| Number of free variables: | $1 *$ |
| :---: | :---: |
| Number of objectives: | 2 - |
| Number of constraints: | 0 - |
| Number of operating point sets: | 0 |



NBI must have a minimum of two objectives, and you can choose as many free variables and constraints as you like. You can add constraints later if required.

Click Next to proceed to setting up free variables.

## Optimization Wizard Step 3

You must select variables to link with the free variables used in your optimization.


Use this screen to associate the variables from your CAGE session with the free variable(s) you want to use in the optimization. Select the correct pair in the right and left lists by clicking, then click the large button as indicated in the figure.

Once you have assigned your free variables here you can either click Next or Finish. This also applies to all later steps in the Optimization Wizard.

- If you click Next you proceed to further screens of the Optimization Wizard where you can set up objectives and constraints.
- If you click Finish you return to the Optimization view in CAGE. You can set up your objectives and constraints from the Optimization view instead of using the Optimization Wizard. You cannot run your optimization until objectives (and constraints if required) have been set up.


## Optimization Wizard Step 4

You can set up your objectives here or you can set them up at the Optimization view in CAGE. See "Objective Editor" on page 6-25.


Here you can select which models from your session you want to use for the optimization, and whether you want to maximize or minimize the model output. The foptcon algorithm is for single objectives, so you can only maximize or minimize one model. The NBI algorithm can evaluate multiple objectives. For example, you might want to maximize torque while minimizing NOX emissions. Remember you can also define constraints later, for example, using emissions requirements.

You can also include 'helper' models in your user-defined optimizations, so you can view other useful information to help you make optimization decisions (this is not enabled for NBI or foptcon).

- Click Next to proceed to setting up constraints.
- Click Finish to complete the Optimization Wizard and return to the Optimization view. Note you can only set up point objectives in the wizard, but you can also set up sum objectives in the main Optimization view. See "Objectives and Constraints" on page 6-24.


## Optimization Wizard Step 5

You can use models to define constraint regions that restrict free variables. If you want to use constraints you can select them here, or add them in the Optimization view in CAGE. You can also add other types of constraints in the Optimization view. See "Constraint Editor" on page 6-27.


Select a model for each constraint by selecting a CAGE model and a model constraint and clicking the button to match them up.

For each constraint enter a value in the edit box. Select the operator to define whether the optimization output should be constrained to be greater than or less than the value. The example shown is NOXFLOW_Model <= 250.

- Click Finish to complete the Optimization Wizard and return to the Optimization view.
- You can only click Next to proceed to setting up any data sets if required by your user-defined optimization.


## Optimization Wizard Step 6

If your user-defined optimization allows you to add a data set you can select it on step 6 of the Optimization Wizard. You can use data sets to evaluate models over a different set of operating points during an optimization run. As an example, you could run an optimization at the points (N1, L1), (N2, L2), but an important quantity to monitor and possibly act upon is, say, temperature at points (N3, L3), (N4, L4). You can monitor the temperature at these points by using data sets, to help you select optimization results. You can set up data sets in Step 6 of the wizard or in the Optimization view in CAGE (select Optimization > Edit Data Sets).

Data sets are not enabled for foptcon and NBI optimizations.
Click Finish to return to the Optimization view in CAGE. Your new optimization appears as a new node in the tree pane on the left, and the setup details appear on the right.

## Optimization View Toolbar

## 

Common tasks are available in the toolbar:

- Add Objective - Adds an objective to your optimization (if enabled; remember foptcon can only have a single objective). You must double-click the new objective to open the Objective Editor, select a model, and set whether to maximize or minimize. See "Objective Editor" on page 6-25.
- Add Constraint - Adds a constraint to your optimization. You must double-click the new constraint (in the list of constraints) to open the Constraint Editor and set up the constraint. See "Constraint Editor" on page 6-27
- Import from a data set, Import from output- You can populate the Variable Values panes by importing values - See "Defining Variable Values" on page 6-18.
- Set Up Optimization, Set Up and Run Optimization - Both these options open the Optimization Parameters dialog box, where you can change optimization settings such as tolerances and number of solutions. When
you close the dialog the settings are saved (and the optimization runs in the case of Set Up and Run). See "Using the Optimization Parameters Dialog Box" on page 6-42.
- Run Optimization - Starts the optimization. See "Running Optimizations" on page 6-41.


## Defining Variable Values

In the optimization view you can use the Variable Values panes to define a set of operating points for the optimization. You do not have to choose a set of operating points; if you do not, however, the optimization runs at a single point of your choosing (the set points of variables is the default).

Running the optimization requires the selected models to be evaluated (many times over) and hence values are required for all the model input factors. The default values for the fixed variables are their set points, as shown in the Fixed Variables pane. You chose one or more free variables, so the optimization chooses different values for those free variables in trying to find the best value of the objectives. The default initial value for a free variable is the set point, as shown in the Free Variables pane.

To define the set of operating points for the optimization, you can

- "Define Variables Manually" on page 6-18
- "Import from a Data Set" on page 6-19
- "Import from Optimization Output" on page 6-21


## Define Variables Manually

To define values manually:
1 In the Input Variable Values pane, increase the Number of runs. New rows appear for both fixed and free variables, all containing the default set point values of each variable. Each row defines an operating point for an optimization run.

2 Edit the values in the Fixed Variables pane to define the points where you want to run the optimization.

- You can copy and paste values from other parts of CAGE (existing optimizations or data sets etc.), or from the Help Browser or other documents.
- You can select Optimization > Import From Data Set if you have suitable variables to import.
- You can select Optimization > Import From Output if you have suitable optimization outputs.
An example is shown in the following figure.

| Fixed Variables |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Variable: | L | N | A | E |
| Number of values: | $1 \leqslant$ | $1 \div$ | $1 \div$ | $1 \div$ |
| 1 | 0.1 | 1000 | 12 | 5 |
| 2 | 0.8 | 1000 | 12 | 5 |
| 3 | 0.1 | 3000 | 12 | 5 |
| 4 | 0.8 | 3000 | 12 | 5 |
| 5 | 0.1 | 6000 | 12 | 5 |
| 6 | 0.8 | 6000 | 12 | 5 |

3 You can edit the values in the Free Variables pane in a similar way to define the starting values of the free variables if you want, or you can leave these at the default.

For foptcon optimizations you can specify a number of initial starting values per run, see "foptcon Optimization Parameters" on page 6-43.

If you wish to restrict the range of the free variables, you can select Optimization > Edit Free Variable Ranges. The default is the range of the variable as defined in the Variable Dictionary.

4 Use the right-click context menu to duplicate or delete runs, or select Fill All Runs to copy the selected run's values to all other runs.

The Number of Values controls are for sum optimizations. See "Setting Up Sum Optimizations" on page 6-32.

## Import from a Data Set

1 Select Optimization > Import from Data Set (or use the toolbar button) to define the operating points for an optimization from a data set, if you have suitable variables to import. The Import From Data Set dialog box appears.


2 Select a data set.
3 Select data set columns to import.
4 Choose whether you want a run per data set row, or each variable to have the same length as the number of data set rows. For information on altering the length of variables (for sum optimizations only), see "Using Variable Values Length Controls" on page 6-34.

5 Click OK to import the variable values.

## Import from Optimization Output

1 Select Optimization > Import from Output to import starting values from the output values of a previous optimization. The Import From Optimization Output dialog box appears.


2 Select the desired optimization output.

3 Select the columns from the output you want to import.
4 Choose the runs from the optimization output that you want to use. The Selection within output controls allow you to choose selected solutions, and/or select a subset of rows to import. If the number of values per run differs between current inputs and selected outputs, the inputs are altered to match.

- Select the option button All to import all runs.
- Select the option button Selection to import a subset of runs. You can enter a vector specifying the runs you want to import (e.g., 13 6:9), or click the button Select in Table to open a dialog box and select runs manually.
- Select the option button Feasible to filter the output by constraint values. You can optionally set the Tolerance by using the buttons or entering a value, then click the button Select in Table to open a dialog box to view and edit this selection.
If the number of runs of the selected output is different to the current input, you are prompted (as shown in the preceding figure) to select the check box Alter number of runs in optimization if required to alter the number of runs of the optimization to match the output. For example, if you are importing 3 variables to a 5 variable optimization, all 5 variables must share the same number of runs. You cannot click $\mathbf{O K}$ to import the runs if it is necessary to select this check box first.

If you click the button Select in Table you see the following dialog box.


Highlight cells in the table (Shift+click, Ctrl+click, or click and drag) to select runs to import.

If you chose to filter for feasibility, the table appears prefiltered with runs selected that met the required Tolerance. For example, if the Tolerance was set to 0.0001 , runs are selected where all constraint outputs were $<=0.0001$. You can enter an independent selection for the tolerance on this dialog box, and click the Select button to filter using this value.

If there are multiple solutions in the output you can browse them with the Solution controls.

When you are satisfied with the selected runs, click OK to return to the Import From Optimization Output dialog box. Click OK to import the runs.

## Objectives and Constraints

You can set up objectives and constraints from the main CAGE Optimization view, as well as within the Optimization Wizard.

You can perform the following tasks:

- Add, Edit, or Delete objectives from the right-click context menu and Optimization menu (if allowed by the algorithm-foptcon can only have a single objective).
- Add, Edit, Delete, or Disable constraints from the right-click context menu and Optimization menu. Use Disable to remove constraints without deleting them, and use Enable to reapply them.

Double-click to edit existing objectives and constraints in the Objectives or Constraints panes.

You can run two types of optimizations, point optimizations and sum optimizations. Point optimizations look for the optimal values of each objective function at each point of an operating point set. A sum optimization finds the optimal value of a weighted sum of each objective function. The weighted sum is taken over each point, and the weights can be edited. For an example, see the tutorial section "Sum Optimization" in the Getting Started documentation.

You need to use the Objective Editor and Constraint Editor to set up sum objectives and model sum constraints. You must do this to run weighted sum optimizations. You cannot set these up from the Optimization Wizard.

See the following topics:

- "Objective Editor" on page 6-25
- "Constraint Editor" on page 6-27

You can also set up linear, 1- and 2-D table, and ellipsoid constraints in the Constraint Editor, as for designs in the Model Browser part of the Model-Based Calibration Toolbox.

## Objective Editor

Double-click or right-click objectives to open the Edit Objectives dialog.


You can select Point objective or Sum objective from the Objective type drop-down menu. Use sum objectives only for weighted sum optimizations; otherwise, use point objectives.

## Point Objectives

The preceding example shows the point objective controls. Select which models from your session you want to use for the optimization, and whether you want to maximize or minimize the model output. The foptcon algorithm is for single objectives, so you can only maximize or minimize one model. The NBI algorithm can evaluate multiple objectives. For example, you might want to maximize torque while minimizing NOX emissions.

You can also include 'helper' models in your user-defined optimizations, so you can view other useful information to help you make optimization decisions (this is not enabled for NBI or foptcon).

These are the same options you can choose in the Optimization Wizard. See "Optimization Wizard Step 4" on page 6-14.

## Sum Objectives

For weighted sum optimizations, the objectives are typically sum objectives. See the following example.


As for point objectives, select which models from your session you want to use for the optimization, and whether you want to maximize or minimize the model output.

You can edit weights in the Optimization view, to make certain operating points more important, giving more flexibility to solutions for other points. The weights are applied to each solution to calculate the weighted sums. You can edit the weights in the Fixed Variables pane. This is the same process as selecting weights for the Weighted Pareto View. See "Weighted Objective Pareto Slice" on page 6-54.

In the Edit Objective dialog box, the Expected sum of weights is optional. However if this option is used (and set correctly), then it improves the performance of the optimization. When the expected sum is set correctly, it scales the objective sum onto a range that is commensurate with the other optimization objectives and constraints.

The Expected sum of weights is a normalization value per run-all weights are divided by this value, to try to make the normalized weights sum to 1 for each run. With this normalization, the objective sum should approximately vary on the same range as the other optimization objectives and constraints. For instance if you have two operating points per run, and the Expected sum of weights is 5 , you can set the weights in the Fixed Variables pane to 2 and 3 for each operating point respectively, to make the normalized weights sum to 1 . See "Using Variable Values Length Controls" on page 6-34 to set multiple operating points per run.

For a tutorial example of a sum optimization, see "Sum Optimization" in the Getting Started documentation.

## Constraint Editor

Select a Constraint type in the drop-down menu. The first four choices are the same as the following design constraint types:

- "Linear Constraints"
- "Ellipsoid Constraints"
- "1-D Table Constraints"
- "2-D Table Constraints"

These are the same constraints you can apply to designs in the Model Browser part of the Model-Based Calibration Toolbox.

In the context of optimization you can select constraint inputs on the additional Inputs tab. You can select any variable or model as an input into constraints. The default selects the free variables where possible. Models are treated as nonlinear functions, so if you choose to feed a model into a linear constraint it will make that constraint nonlinear. You are not able to access it as a linear constraint in user-defined optimization scripts.

For optimization constraints you can also select the following constraint types:

- "Model Constraints" on page 6-28
- "Range Constraints" on page 6-29
- "Sum Constraints" on page 6-30
- "Table Gradient Constraints" on page 6-30


## Model Constraints

To construct a model constraint:
1 Select an Input model in the left list.
2 You can use the Evaluate quantity drop-down list to choose Evaluation value, Boundary constraint, or PEV value (model prediction error variance) to define your constraint.

3 Choose the appropriate option button to either enter a value in the Constant edit box, or to select a CAGE item from the list of models or variables.

4 Select the Constraint type operator to define whether the optimization output should be constrained to be greater than or less than the constant or item value specified on the right.

5 Check the displayed Constraint description, and click OK.
The model constraint settings are shown in the following figure.


## Range Constraints

You can specify an upper and lower bound to constrain expressions (which can be variables, models or tables). You can specify bounds with constants, vectors, variables, models, or tables.

1 Select a CAGE item to constrain on the Bound Expression tab. Use the drop-down menu to switch between variables, models, or tables, and then select the item to constrain. For appropriate models you can also choose to constrain either the PEV or evaluation value.

2 On the Lower Bound tab, select an option button to choose whether to use a constant, vector, or CAGE item to specify the bound.

- For constants, enter a value.
- For vectors, you can enter the lower bound for each point in the Input Variable Values pane in the Optimization view after you close the Edit Constraint dialog box.
- For CAGE items, use the drop-down menu to switch between variables, models, or tables, and then select the item to specify the lower bound. For appropriate models you can also choose to use either the PEV or evaluation value.

3 Specify the upper bound on the Upper Bound tab in the same way as you specified the lower bound on the Lower Bound tab.

4 Check the displayed Constraint description, and click OK.
For a detailed explanation of range constraint outputs, see "Range Constraint Output" on page 6-64.

## Sum Constraints

Use these for weighted sum optimizations. Choose a model, constraint bound value and an operator.

You can also select an Expected sum of weights normalization value per run to improve the performance of the optimization. See the explanation under "Sum Objectives" on page 6-26.

You can have a mixture of point and sum constraints.
See the tutorial "Sum Optimization" in the Getting Started documentation for a step-by-step example, and for descriptions of optimization output specific to sum problems, see "Interpreting Sum Optimization Output" on page 6-68.

## Table Gradient Constraints

Table Gradient constraints allow you to constrain the gradient of a free variable over a grid of fixed variables. These constraints are most useful in 'sum' problems. Unless you are using a user-defined optimization, you should normally use a sum objective (and therefore runs normally have multiple values).

1 Select a free variable to constrain.
2 Specify one or two fixed variables, and a grid of points either manually or by selecting table axes.

3 Enter values in the edit boxes to specify the maximum change in the free variable per amount of fixed variable change between cells. For example, enter 5 and 1000 to specify 5 degrees maximum change in cam angle per 1000 RPM.

4 Check the displayed Constraint description, and click OK.
For a detailed explanation of table gradient outputs, see "Table Gradient Constraint Output" on page 6-74.

## Setting Up Sum Optimizations

CAGE can solve sum type optimizations. These optimizations find the optimal settings of control parameters at several operating points simultaneously. Sum optimizations are useful for solving drive cycle problems where the constraints have to be applied across the whole cycle, e.g. weighted engine out brake specific NOx $<=3 \mathrm{~g} / \mathrm{kWh}$.

To set up a sum optimization:
1 Use the first 3 steps of "Optimization Wizard" on page 6-9 to create your optimization, defining the algorithm, number of objectives and free variables.

2 For simple model constraints it is optional whether you set them up in the wizard or later in the Optimization view. To apply other types of constraints you must use the Optimization view. You can apply linear, ellipsoid, 1-D table, 2-D table, and range constraints, and some constraints are specific to sum optimizations-sum constraints and table gradient constraints.

See "Constraint Editor" on page 6-27 for details of all these constraints.
3 For a sum optimization, it is highly likely that the objectives are sum objectives. For sum objectives you must configure your objectives in the Optimization view, not in the optimization wizard. To configure the objectives to be sum objectives, follow the instructions in "Sum Objectives" on page 6-26.

4 Set variable values for the points where you want the optimization to run. See "Defining Variable Values" on page 6-18. You can enter values manually, or by importing from data sets or the output of existing optimizations.

For sum optimizations you must also use the length controls when defining the variable values. See "Using Variable Values Length Controls" on page 6-34.

5 Run the optimization. See "Running Optimizations" on page 6-41.

6 View the results (see "Optimization Output View" on page 6-50). For descriptions of optimization output specific to sum problems, see "Interpreting Sum Optimization Output" on page 6-68.

## Example Sum Optimization

The following sections describe the controls and outputs for sum optimizations using the following example problem for illustration.

Say you have created models for torque (TQ), residual fraction (RESIDFRAC) and exhaust temperature (EXTEMP) for a gasoline engine.

The inputs to these models are

- Spark advance, S
- Intake cam timing, INT
- Exhaust cam timing, EXH
- Engine speed, N
- Relative load, L

You need to set up an optimization to calculate optimal settings of S, INT and EXH for the following operating points:

| $\mathbf{N}$ | $\mathbf{L}$ |
| :--- | :--- |
| 1000 | 0.3 |
| 1100 | 0.2 |
| 1250 | 0.31 |
| 1500 | 0.25 |
| 1625 | 0.18 |

The objective for this optimization is:
Maximize the weighted sum of TQ over the operating points.
The constraints for this optimization are:

- Constraint 1: EXTEMP <= $1290^{\circ} \mathrm{C}$ at each operating point
- Constraint 2: RESIDFRAC <= 17\% at each operating point
- Constraint 3: Change in INT is no more than $5.5^{\circ}$ per 500 rpm change in N and $5.5^{\circ}$ per 0.1 change in L , evaluated over a 3 -by- $3(\mathrm{~N}, \mathrm{~L})$ table.
- Constraint 4: Change in EXH is no more than $5.5^{\circ}$ per 500 rpm change in N and $5.5^{\circ}$ per 0.1 change in L , evaluated over a 3 -by- $3(\mathrm{~N}, \mathrm{~L})$ table.

You can use the foptcon algorithm in CAGE to solve this problem.
This example is used to explain the controls and outputs in the following sections, "Using Variable Values Length Controls" on page 6-34 and "Interpreting Sum Optimization Output" on page 6-68.

## What Is a Run?

Sum type optimizations determine optimal settings of operating points simultaneously. Thus, one call to the algorithm determines the optimal settings of the control parameters at each operating point.

Each call to the optimization algorithm is known in CAGE as a run. The number of runs that CAGE will perform is indicated in the Number of runs control in the Input Variable Values pane. See the next section, "Using Variable Values Length Controls" on page 6-34.

See "Algorithm Restrictions" on page 6-38 for details on the optimization algorithm restrictions in CAGE.

## Using Variable Values Length Controls

You use the Input Variable Values pane to set variable values for the points where you want the optimization to run. (See "Defining Variable Values" on page 6-18). You can enter values manually or by importing from data sets or the output of existing optimizations.

For sum optimizations you must also use the Number of Values length controls when defining the variable values.

At the optimization node the Input Variable Values pane has Number of Values controls for each free and fixed variable. Use these controls to increase the number of operating points per optimization run. If you leave all
the Number of Values set to one, each row in the values panes represents one optimization run. See "What Is a Run?" on page 6-34.

- You can edit the Number of Values directly, or you can select Optimization > Set Variable Length to change all variable lengths at once.
- You can quickly toggle between N runs of one point and a single run of N points (which can be used as a drive cycle for sum optimization problems) using the Optimization menu items Convert to Single Run and Convert to Multiple Runs. You can also use the Number of Values controls to define your sum optimization runs.

If you increase the Number of Values of a fixed or free variable, then the number of operating points within each run increases, as shown in the following example.

| Free Variables |  |  |  |  | Fixed Variables |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Variable: |  | S | EXH | $\mathbb{N T}$ | Variable: |  | Objective... | N | L |
|  | er of | $5 \div$ | $5 \div$ | $5 \div$ |  |  | $5 \div$ | 5* | $5 \div$ |
| 1 | (1) | 15.117 | 22.414 | 39.778 | 1 | (1) | 1 | 1000 | 0.3 |
|  | (2) | 13.745 | 29.173 | 34.534 |  | (2) | 1 | 1100 | 0.2 |
|  | (3) | 17.6 | 36.74 | 45.575 |  | (3) | 1 | 1250 | 0.31 |
|  | (4) | 22.034 | 24.4 | 43.411 |  | (4) | 1 | 1500 | 0.25 |
|  | (5) | 20.561 | 33.945 | 39.514 |  | (5) | 1 | 1625 | 0.18 |

The input variable values are configured for the example problem, showing a single run (left column under Number of Values shows 1) of five operating points (as shown in the right column under Number of Values). The optimizer simultaneously finds the optimal settings of S, EXH and INT at all the operating points, starting at the initial values shown in the Free Variables table for each point.

The index of each operating point is indicated by the number in brackets in the right column under Number of Values, for example the third operating point is $\mathrm{N}=1250, \mathrm{~L}=0.31$.

When objectives or constraints require weights or bounds you can enter them in the Input Variable Values pane. In the example problem, the objective requires specified weights for the weighted sum of torque, so the column Objective1_weights appears in the Fixed Variables pane, where you can
enter weights for each point. For an example see "Setting Weights for the Sum Objective and Constraint" in the diesel case study.

You can also run a sum optimization over different sets of operating points. Consider the following example, an optimization of the weighted sum of fuel consumption over two different drive cycles.

| Input Variable Values |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Number of runs: |  | Vector display format: |  |  | Expanded vertically |  |  |  |  |
| Free Variables |  |  |  |  | Fixed Variables |  |  |  |  |
| Variable: |  | S | EXH | INT | Variable: |  | Objective... | N | L |
| $\begin{gathered} \text { Num } \\ \text { va } \end{gathered}$ | er of tes: | $5 *$ | 5 - | $5 \div$ | $\underset{\text { ve }}{\text { Num }}$ | er of es: | 5 | 5* | $5 \div$ |
| 1 | (1) | 15.117 | 22.414 | 39.778 | 1 | (1) | 1 | 1000 | 0.3 |
|  | (2) | 13.745 | 29.173 | 34.534 |  | (2) | 1 | 1100 | 0.2 |
|  | (3) | 17.6 | 36.74 | 45.575 |  | (3) | 1 | 1250 | 0.31 |
|  | (4) | 22.034 | 24.4 | 43.411 |  | (4) | 1 | 1500 | 0.25 |
|  | (5) | 20.561 | 33.945 | 39.514 |  | (5) | 1 | 1625 | 0.18 |
| 2 | (1) | 25 | 22.5 | 22.5 | 2 | (1) | 1 | 5000 | 0.55 |
|  | (2) | 25 | 22.5 | 22.5 |  | (2) | 1 | 5214 | 0.5 |
|  | (3) | 25 | 22.5 | 22.5 |  | (3) | 1 | 5564 | 0.6 |
|  | (4) | 25 | 22.5 | 22.5 |  | (4) | 1 | 5847 | 0.64 |
|  | (5) | 25 | 22.5 | 22.5 |  | (5) | 1 | 6000 | 0.7 |

The preceding figure shows an optimization that runs twice (Number of runs has been set to 2, and the left column under Number of Values shows 2 runs). Each run contains five operating points (as shown in brackets in the right column under Number of Values).

The optimization algorithm will be called twice (two runs). In the first run, optimal settings of S, EXH and INT will be simultaneously calculated for each point in the first drive cycle, as shown in the following table.

| $\mathbf{N}$ | $\mathbf{L}$ |
| :--- | :--- |
| 1000 | 0.3 |
| 1100 | 0.2 |
| 1250 | 0.31 |
| 1500 | 0.25 |
| 1625 | 0.18 |

In the second run, optimal settings of S, EXH and INT will be calculated for each point in the second drive cycle, as shown in the following table.

| $\mathbf{N}$ | $\mathbf{L}$ |
| :--- | :--- |
| 5000 | 0.55 |
| 5214 | 0.5 |
| 5564 | 0.6 |
| 5847 | 0.64 |
| 6000 | 0.7 |

In the previous examples, the number of values for each variable is identical. It is also possible to specify a mixture of scalars and vectors for each variable, as shown in the following example.


The Number of Values controls are independent for each variable. In the preceding figure:

- $S$ Number of Values $=1$
- EXH Number of Values $=5$
- INT Number of Values = 1

In this case, the single initial value of $S$ is used for every drive cycle point in the optimization, and similarly for INT (and the optimizer will return a single value for $S$ and INT for the run).

## Algorithm Restrictions

Each run of a CAGE Optimization makes a call to the algorithm you have chosen to use. This algorithm needs to evaluate the objectives and constraints (probably several times) to allow it to determine the optimal settings of the free variables. Optimization algorithms typically have restrictions on the number of objective and constraint outputs they can handle. The following table details the restrictions on the two algorithms provided in CAGE.

| Algorithm Name | Objectives | Constraints |
| :--- | :--- | :--- |
| Foptcon | One output | Any number of outputs |
| NBI | Two or more outputs | Any number of outputs |

When each objective and constraint is evaluated during a run, the number of outputs it returns depends on the maximum number of values of all of its inputs. The following table details the number of outputs each objective type returns as a function of the maximum number of values of all of its inputs.

| Objective <br> Type | Maximum <br> Number of <br> Values of All <br> Inputs to the <br> Objective | Number of <br> Outputs | Reason |
| :--- | :--- | :--- | :--- |
| Point | N | N | A point objective is evaluated <br> at each operating point within <br> a run, and all the values are <br> returned. |
| Sum | N | One | A sum objective evaluates a <br> model at every operating point <br> and returns one value, which is <br> the weighted sum of the model <br> evaluations. |

Similarly, the following table details the number of outputs each constraint type returns as a function of the maximum number of values of all of its inputs.

| Constraint Type | Maximum <br> Number of Values of All Inputs to the Constraint | Number of Outputs | Reason |
| :---: | :---: | :---: | :---: |
| Linear | N | N | These constraints are evaluated at every operating point within a run, and all values are returned. |
| Ellipsoid | N | N |  |
| 1D Table | N | N |  |
| 2D Table | N | N |  |
| Model | N | N |  |
| Range | N | $0, \mathrm{~N}$ or 2 N | A range constraint evaluates an expression at each operating point within a run. The constraint returns two values for each point, the distance from the lower and upper bound. In this case 2 N outputs are returned. If one of the bounds is infinite, then only the distance to the finite bound is returned for each point, and N outputs are returned. If both bounds are infinite then 0 outputs will be returned. |
| Sum | N | 1 | A sum constraint evaluates a model at every operating point and returns the difference between the weighted sum of the model and a bound. |
| Table | N | $>=8$ <br> (dependent on settings) | A table gradient constraint constrains the gradient of a free variable over a grid. The number of outputs returned depends on the dimensions of the grid. |

You can use these three tables to check whether the problem set up satisfies the algorithm restrictions. As an example, the following table checks whether the example problem (detailed in "Example Sum Optimization" on page 6-33) satisfies the restriction of the algorithm chosen to solve it, foptcon.

| Objective | Maximum Number <br> of Values of All <br> Inputs | Number of Outputs |
| :--- | :--- | :--- |
| Weighted sum of TQ <br> over the drive cycle <br> points | 5 | 1 (using the Objective <br> table) |


| Constraint | Maximum Number of Values of All Inputs | Number of Outputs |
| :---: | :---: | :---: |
| EXTEMP $<=1290^{\circ} \mathrm{C}$ at each drive cycle point | 5 | 5 (using the Constraint table) |
| RESIDFRAC <= $17 \%$ at each drive cycle point | 5 | 5 (using the Constraint table) |
| Change in INT is no more than $5.5^{\circ}$ per 500 rpm and $5.5^{\circ}$ per 0.1 change in $L$ | 5 | 24 (this is the number of table gradient constraint outputs generated from a 3-by-3 table) |
| Change in EXH is no more than $5.5^{\circ}$ per 500 rpm and $5.5^{\circ}$ per 0.1 change in L | 5 | 24 (this is the number of table gradient constraint outputs generated from a 3-by-3 table) |

Thus, the example problem has 1 objective output and 58 constraint outputs. This satisfies the restrictions of the foptcon algorithm and so the algorithm can be used.

## Running Optimizations

When you click Finish to complete the Optimization Wizard, you return to the Optimization view in CAGE. Your new optimization appears as a new node in the tree pane on the left, and the setup details appear on the right. An example follows:


If your optimization is ready to run you can click Run Optimization in the toolbar to proceed. You may want to define variable values before running the optimization. If you need to set up any objectives or constraints Run will not be enabled. If your optimization is ready to run you can also click Set Up and Run Optimization if you want to change algorithm-specific settings such as number of required solutions and tolerances for termination.
－If you click Set Up and Run Optimization，you can change settings in the Optimization Parameters dialog box．Then when you click OK the optimization process begins．See＂Using the Optimization Parameters Dialog Box＂on page 6－42．
－If you click Run Optimization instead，you do not see the optimization settings，but go straight to running the optimization．

You will see a progress bar as the optimization proceeds．When it is finished， a new Output node appears under your Optimization node in the tree and the view automatically switches to this node where you can analyze the results． An example tree is shown in the following figure．See＂Optimization Output View＂on page 6－50．

## Optimization

$\square$－IN Optimization
昫 Optimization＿Output
－${ }^{20}$ Optimization＿1
罗习 Optimization＿1＿Output

## Using the Optimization Parameters Dialog Box

The settings in the Optimization Parameters dialog box are algorithm specific．
See the following topics：
－＂foptcon Optimization Parameters＂on page 6－43
－＂NBI Optimization Parameters＂on page 6－44
If you edit these settings and later want to return to the defaults，select Optimization＞Reset Parameters．If you add parameters to user－defined optimization scripts，you may need to use this reset option to make all new parameters appear in the dialog box．

See also＂Scale Optimization＂on page 6－48．

## foptcon Optimization Parameters

The foptcon optimization algorithm in CAGE uses the MATLAB fmincon algorithm from the Optimization Toolbox. foptcon wraps up the fmincon function so that you can use the function for maximizing as well as minimizing. For more information, see the fmincon reference page in the Optimization Toolbox documentation, fmincon.


- Display - choose none, iter, or final. This setting determines the level of diagnostic information displayed in the MATLAB workspace.
- none - No information is displayed.
- iter - Displays statistical information every iteration.
- final - Displays statistical information at the end of the optimization.
- Maximum iterations - Choose a positive integer.

Maximum number of iterations allowed

- Maximum function evaluations - Choose a positive integer.

Maximum number of function evaluations allowed

- Variable tolerance - Choose a positive scalar value.

Termination tolerance on the free variables

- Function tolerance - Choose a positive scalar value.

Termination tolerance on the function value

- Constraint tolerance - Choose a positive scalar value.

Termination tolerance on the constraint violation

- Minimum/maximum change in variables for gradient

Choose a positive scalar to control the input step size that is taken when gradients are being calculated. The default settings should work for the majority of problems.

- Number of start points - Choose a positive integer, N. (N-1) start points per run are chosen using a latin hypercube design to cover the space, in addition to the starting value specified in the Input Variable Values pane.
- Run from feasible start points only - Select this option to terminate all runs that start with an initial value that does not satisfy the constraints. If this condition is not met this is reported in Output message, in the Solution Information pane of the Optimization Output view.
- Interface version - This option is only enabled when a user-defined optimization script does not specify a version to use. Some existing user-defined optimization scripts may require setting the interface version as 2 or 3 , according to the toolbox version. Version 3 is preferable, but may not work with all old scripts. See setRunInterfaceVersion for details.


## NBI Optimization Parameters

The example following shows the NBI options in the Optimization Parameters dialog box.


## Background on the NBI (Normal Boundary Intersection Algorithm)

To understand the options for the NBI algorithm, some limited understanding of the algorithm is required. For more information on the NBI algorithm, see the NBI home page at the following URL:
http://www.caam.rice.edu/~indra/NBIhomepage.html
The NBI algorithm is performed in two steps. The first step is to find the global extrema of each objective individually. This is called the shadow minima problem, and is a single-objective problem for each objective function.

The MATLAB routine fmincon is used to find these extrema. Once these extrema are found, they can be plotted against each other. For example, consider an NBI optimization that simultaneously maximizes TQ and minimizes NOX emissions. A plot of the extrema against each other might resemble the following.


The second step is to find the "best" set of tradeoff solutions between your objectives. To do this, the NBI algorithm spaces Npts start points in the ( $\mathrm{n}-1$ ) hypersurface, S , that connects the shadow extrema. In the above example, $S$ is the straight line that connects the points $N$ and $T$. For each of the Npts points on S , the algorithm tries to maximize the distance along the normal away from this surface (this distance is labeled $L$ in the following figure). This is called the NBI subproblem. For each of the points, the NBI subproblem is a single-objective problem and the algorithm uses the MATLAB fmincon routine to solve it. This is illustrated below for the TQ-NOX example.


The figure above shows spacing of the points between the extrema along the ( $n-1$ ) surface. The algorithm tries to maximize the distance $L$ along the normal away from the surface. The following figure shows the final solution found by the NBI algorithm.


## NBI Options

- Tradeoff points per objective pair ( Np )

The number of tradeoff solutions between your objectives that you want to find, Npts, is determined by the following formula:

$$
N p t s=\left(\frac{n+N p-2}{N p-1}\right)
$$

where

- $N p$ is the number of points per objective pair.
- n is the number of objective functions.

Note the following:

- For problems with two objectives ( $\mathrm{n}=2$ ),

$$
N p t s=N p
$$

- For problems with three objectives ( $\mathrm{n}=3$ ),

$$
N p t s=\frac{N p(N p+1)}{2}
$$

## - Shadow minima options and NBI subproblem options

As the NBI algorithm uses the MATLAB fmincon algorithm to solve the shadow minima problem and the NBI subproblems, the options available are similar to those for the foptcon library function. For more information on these options, see the previous section, "foptcon Optimization Parameters" on page 6-43.

## Scale Optimization

The Optimization menu contains the option to Scale Optimization Items - Select this to toggle scaling on and off. When you select scaling on, objective and constraint evaluations are (approximately) scaled onto the range [-11]. With scaling off, when you run the optimization the objective and constraint evaluations return their raw numbers.

Try running your optimization with scaling off, which is the default setting, to see if it converges to a satisfactory solution (check the output flags and the
contour view). If your optimization solution is unsatisfactory, check to see if the objective and constraint functions have vastly different scales. In this case, try turning scaling on, because these optimization problems may benefit from objective and constraint evaluations being scaled to a common scale.

The output view always shows the solutions in raw, unscaled values, whether or not you use scaling to evaluate the problem.

## Optimization Output View

When you have run an optimization an Output node appears in the optimization tree and the Optimization Output views appear. Use the toolbar buttons to determine what is displayed in the table and the graph views. The first default view is the Solution Slice table and the Objective Slice Graphs.

Use these toolbar buttons or the View menu to select the following Table Views:

## 

- "Solution Slice" on page 6-51
- "Pareto Slice" on page 6-53
- "Weighted Objective Pareto Slice" on page 6-54
- "Selected Solution Slice" on page 6-57

Use these toolbar buttons to select the following Graph Views:

## 붕 日国

- "Objective Slice Graphs" on page 6-58
- "Objective Contour Plot" on page 6-59
- "Pareto Front Graphs" on page 6-60
- "Constraint Slice Graphs" on page 6-61
- "Constraint Summary Table" on page 6-63

You can split and add these views as in the Design, Data and Boundary Editors - use the right-click context menu, the View menu, or the buttons in the view title bars.

## 

The last four toolbar buttons are also in the Solution menu:

- Select solution - This option is for multiobjective optimization, used for choosing your preferred solution for each operating point. See "Selected Solution Slice" on page 6-57.
- Edit pareto weights - This option is used for evaluating weighted sums. See "Weighted Objective Pareto Slice" on page 6-54.
- Export to data set - This option exports the table visible in the current view only to a new data set (the name of the data set is taken from the name of the optimization node).
- Fill tables using optimal solutions - This option opens the Table Filling From Optimization Results Wizard. See "Filling Tables from Optimization Results" on page 6-81
- The Solution menu also has Retain Output (also in the context menu when you right-click an optimization output node). If you select this option, the output node is retained, so if you rerun the optimization you get additional output nodes.

Check the Solution Information pane for details such as the Output message for the selected solution. In this pane you can see, for example, if an foptcon optimization run terminated because no feasible start point was found.

Some features of the output node are specific to sum optimizations. See "Interpreting Sum Optimization Output" on page 6-68.

## Solution Slice

The Solution Slice view (click ) shows a table with one solution at all operating points and all runs.

The following example shows a Solution Slice table display.

| $\square$ | 4 |  | Current run |  | Curr | ent solutio | ก: 1 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Optimization Output Values |  |  |  |  |  |  |  |
| Vector display format: Expanded horizontally |  |  |  |  |  |  |  |
| Variable: | S | EXH | INT | N | L | Objective1 | Constrai... |
| 1 | 23.964 | 37.883 | 36.64 | 1000 | 0.3 | 36.241 | -326.177 |
| 2 | 25.914 | 21.227 | - 22.301 | 2000 | 0.3 | 38.142 | -175.611 |
| 3 | 33.118 | 10.027 | 20.076 | 3000 | 0.3 | 38.842 | -86.935 |
| 4 | 40.35 | 5.004 | - 20.007 | 4000 | 0.3 | 37.255 | -34.19 |
| 5 | 40.373 | 8.732 | 250 | 5000 | 0.3 | 34.93 | -2.283 |
| 6 | 26.23 | -5 | - $-8.804 \mathrm{e}-3$ | 4000 | 0.5 | 92.207 | -39.538 |
| 7 | 12.97 | 34.22 | 233.295 | 1000 | 0.5 | 89.165 | -263.537 |
| 8 | 15.336 | 30.54 | 4 28.554 | 1500 | 0.5 | 90.559 | -206.294 |
| 9 | 16.562 | 20.904 | 20.843 | 2000 | 0.5 | 91.747 | -145.287 |
| 10 | 22.173 | -5 | 5 -5 | 3000 | 0.5 | 93.149 | -82.167 |
| 11 | 26.23 | -5 | - $8.804 \mathrm{e}-3$ | 4000 | 0.5 | 92.207 | -39.538 |
| 12 | 30.869 | -2.669 | 21.539 | 5000 | 0.5 | 88.013 | -7.579 |
| 13 | 18.046 | 3.147 | 7.537 | 2500 | 0.6 | 118.737 | -83.429 |
| 14 | 22.341 | -4.938 | - -4.596 | 3500 | 0.6 | 119.712 | -63.818 |
| 15 | 23.622 | -5 | - -4.247 | 4500 | 0.7 | 143.181 | -19.45 |

The Solution Slice view shows a table of one solution at all operating points and all runs in the problem. For single-objective optimizations there is only one solution per operating point, so the Solution Slice is the only useful view. For multiobjective optimizations with more than one solution per run you can scroll through the solutions using the arrows or edit box at the top.

The table shows the selected solution at all operating points. The Optimization Output Values pane shows the fixed variable settings, the optimal free variable settings, and the evaluation of objectives and constraints at the optimal free variable settings.

Note If you export the output to a data set (using the toolbar button) it is the current table that is exported.

Click in the table to make the graph views (objective slice, constraint slice and pareto front) display the selected operating point.

- The "Objective Slice Graphs" on page 6-58 show the objective functions at the operating point selected in the table, with the solution value in orange.
- If you have constraints you can also choose to display the "Constraint Slice Graphs" on page 6-61. These show the constraint functions at the selected operating point with the solution value in orange.
- If you are viewing a multiobjective optimization you can also choose to display the "Pareto Front Graphs" on page $6-60$ which show the available solutions with the current selection highlighted in red.
- You can also display the "Constraint Summary Table" on page 6-63 which details the distance to each constraint edge for the selected operating point in the table. This can be useful to see at a glance if a solution met all the constraints. If there are many constraints it can be time-consuming to use the constraint graphs to verify this.

Note that before you run an NBI optimization you can specify how many solutions you want the optimization to find, using the Set Up and Run Optimization toolbar button.

For information on selecting best solutions at each operating point for subsequent export to a data set, see "Selected Solution Slice" on page 6-57.

## Pareto Slice

The Pareto Slice table view (click $\frac{+}{\top}$ ) is for multiobjective optimization where there is more than one solution at each run. The Pareto Slice shows a table of all solutions at one run; you can scroll through the runs using the arrows or edit box at the top.

Note that before you run an NBI optimization you can specify how many solutions you want the optimization to find, using the Set Up and Run Optimization toolbar button.

| R | 4 |  | Current run: | 4 | Current solution: |  | 7 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Optimization Output Values |  |  |  |  |  |  |  |  |
| Vector display format: Expanded horizontally |  |  |  |  |  |  |  |  |
| Variable: | SPK | N | L | A | E | Objective1 | Objective2 | Constraint1 |
| 1 | -3.877e-3 | 3000 | 0.8 | 12 | 5 | 71.38 | 24.138 | -225.862 |
| 2 | 1.488 | 3000 | 0.8 | 12 | 5 | 74.251 | 25.035 | -224.965 |
| 3 | 3.059 | 3000 | 0.8 | 12 | 5 | 77.01 | 26.015 | -223.985 |
| 4 | 4.721 | 3000 | 0.8 | 12 | 5 | 79.635 | 27.094 | -222.906 |
| 5 | 6.492 | 3000 | 0.8 | 12 | 5 | 82.098 | 28.293 | -221.707 |
| 6 | 8.395 | 3000 | 0.8 | 12 | 5 | 84.362 | 29.64 | -220.36 |
| 7 | 10.462 | 3000 | 0.8 | 12 | 5 | 86.371 | 31.177 | -218.823 |
| 8 | 12.74 | 3000 | 0.8 | 12 | 5 | 88.044 | 32.963 | -217.037 |
| 9 | 15.307 | 3000 | 0.8 | 12 | 5 | 89.247 | 35.097 | -214.903 |
| 10 | 18.298 | 3000 | 0.8 | 12 | 5 | 89.738 | 37.76 | -212.24 |

You can also display "Pareto Front Graphs" on page 6-60 (click ) which show the available solutions with the current selection highlighted in red.

Use the pareto front graphs and "Objective Slice Graphs" on page 6-58 to select the best solution for the run. If you have constraints you can also use the "Constraint Slice Graphs" on page 6-61 and "Constraint Summary Table" on page 6-63 to help you decide which solution to choose for each run.

When you have decided which solution you want to use for the currently selected run you can select it as best by clicking Select Solution ( 鯂) in the toolbar. You cannot select solutions until you enable the Selected Solutions view. See "Selected Solution Slice" on page 6-57. You can also select best solutions in the Solution Slice view, see "Solution Slice" on page 6-51.

## Weighted Objective Pareto Slice

The Weighted Objective Pareto Slice view (click $\#$ ) shows a weighted sum Pareto solution. This is a weighted sum of the objective values over all runs for each solution. For a single objective optimization there is a single cell - the sum of the objective across all runs.

In the following multiobjective example, the value in the Objective 1 column in the first row shows the sum of the solution 1 values of the first objective across all runs. The second row shows the sum of solution 2 Objective 1
values across all runs, and so on for all ten solutions in this case. This can be useful, for example, for evaluating total emissions across a drive cycle. The default weights are unity (1) for each run.

|  | 4 | 1 | Current run: | <none> | Current solution: | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Optimization Output Values |  |  |  |  |  |  |
| Vector display format: Expanded horizontally $\square$ |  |  |  |  |  |  |
| Variable: | Objective1 | Objective2 |  |  |  |  |
| 1 | 587.802 | 5847.758 |  |  |  |  |
| 2 | 587.804 | 5847.766 |  |  |  |  |
| 3 | 587.806 | 5847.774 |  |  |  |  |
| 4 | 587.807 | 5847.781 |  |  |  |  |
| 5 | 587.809 | 5847.789 |  |  |  |  |
| 6 | 587.811 | 5847.797 |  |  |  |  |
| 7 | 587.813 | 5847.804 |  |  |  |  |
| 8 | 587.815 | 5847.812 |  |  |  |  |
| 9 | 587.817 | 5847.82 |  |  |  |  |
| 10 | 587.818 | 5847.828 |  |  |  |  |

You can change the weights; for example, if you need a weighted sum of emissions over a drive cycle, you might want to give a higher weight to the value at idle speed. You can alter weights by clicking Edit Pareto Weights ( Ill ) in the toolbar. The Pareto Weights Editor appears.


Here you can select objectives to sum, and select weights for any run by clicking and editing, as shown in the example above. The same weights are applied to each solution to calculate the weighted sums. Click OK to apply new weights, and the weighted sums are recalculated.

You can also specify weights with a MATLAB vector or any column in the optimization output by selecting the other radio buttons. If you select Data column you can also specify which solution; for example, you could choose to use the values of spark from solution 5 at each operating point as weights. Click Table Entry again, and you can then view and edit these new values.

Note Weights applied in the Weighted Pareto View do not alter the results of your optimization as seen in other views. You can use the weighted sums to investigate your results only. You need to perform a sum optimization if you want to optimize using weighted operating points.

## Selected Solution Slice

In a multiobjective optimization, there is more than one possible optimal solution at each run. You can use the Selected Solutions view to collect and export those solutions you have decided are optimal at each run.

Once you have enabled the Selected Solution view, you can use the plots in the Pareto Front Graphs view and Solution Slice table view to help you select best solutions for each run. These solutions are saved in the Selected Solutions view. You can then export your chosen optimization output for each point from the Selected Solutions view, or use your optimization output to fill tables.

1 You cannot select best solutions until you have enabled the Selected Solutions view. Do this by selecting Solution -> Selected Solution -> Initialize.

2 A dialog called Create Selected Solution appears. The default 1 initializes the first solution for each run as the selected solution. You can edit the solution number here if you want. For example if you select 4 , solution number 4 is initialized as the best solution for every run. When you click OK, the toolbar buttons for the Selected Solutions view and Select Solution are enabled.


3 Once you have enabled the Selected Solutions view, you can use the table views (Solution Slice and Pareto Slice) and the plots in the graphs (Objective Slice, Pareto Front, and Constraint Slice graphs) to help you select best solution for each run.
a Click in the tables to select a point to display in the graphs until you can decide which solution you want for a point.
b Click Select Solution ( ${ }^{\text {鳃 }}$ ) in the toolbar to select the current solution as best.
Repeat until you have selected solutions for all points.

These solutions are saved in the Selected Solutions view. This view collects all your selected solutions together in one place. For example, you might want to select solution 7 for the first run, and solution 6 for the second, and so on. You can then use your chosen optimization output for each point to fill tables, or choose the Export to Data Set ${ }^{\text {囲 toolbar and Solution menu option. See }}$ "Filling Tables from Optimization Results" on page 6-81.

An example of the Selected Solutions view is shown. It looks similar to the Solution Slice view, except the solution controls at the top are not enabled. You cannot change solution number here. The solution chosen as best (in the other views) for the currently selected run is displayed in the grayed out edit box.

| Solution: $4 \longdiv { 3 }$ |  |  | Current run: Current solution: | $\begin{aligned} & 4 \\ & 3 \end{aligned}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Optimization Output Values |  |  |  |  |  |  |  |
| Vector display format: Expanded horizontally |  |  |  |  |  |  |  |
| Variable: | S | N | L | EXH | INT | Objective1 | Objective2 |
| Length: | $1 \div$ | $1 *$ | 1- | 1* | $1 \leqslant$ | 1- | 1* |
| 1 | 24.996 | 1000 | 0.3 | 22.5 | 22.5 | 32.198 | 993.746 |
| 2 | 33.17 | 2000 | 0.3 | 22.5 | 22.5 | 37.873 | 1104.683 |
| 3 | 48.993 | 3000 | 0.3 | 22.5 | 22.5 | 38.217 | 1180.428 |
| 4 | 50.739 | 4000 | 0.3 | 22.5 | 22.5 | 36.18 | 1249.649 |
| 5 | 34.757 | 5000 | 0.3 | 22.5 | 22.5 | 31.664 | 1279.681 |
| 6 | 34.821 | 4000 | 0.5 | 22.5 | 22.5 | 90.017 | 1242.291 |
| 7 | 16.887 | 1000 | 0.5 | 22.5 | 22.5 | 86.365 | 1035.18 |
| 8 | 24.988 | 1500 | 0.5 | 22.5 | 22.5 | 86.969 | 1084.412 |

## Objective Slice Graphs

The objective slice graphs are displayed by default for optimization output views, or you can select $\nabla_{\text {in }}$ the toolbar.


The objective slice graphs show the objective functions at the point selected in the table, with the solution value in orange. Whether the table is displaying a solution slice or pareto slice, the cell you select in the table is always displayed in the graphs. The objective graphs show cross section plots of the objective function against each free variable in the problem.

The yellow areas show a region outside a constraint (such as a boundary constraint exported from the Model Browser part of the Model-Based Calibration Toolbox, or any other optimization constraint). All constraint regions in optimization displays (as in the rest of the toolbox) are shown in yellow.

Use the right-click context menu to toggle constraint display and alter graph size.

## Objective Contour Plot

The Objective Contour Plot (click ©) shows the contours of the objective against any pair of control parameters, at the run selected in the table, with the solution value at the centre of the orange cross-hairs. Yellow areas show a region outside a constraint (see the following figure). This view can be useful for exploring objective functions-a visual way to help avoid local minima.


Select parameters to plot in the drop-down lists, and if you have more than one objective you can select from the Objective drop-down list.

Use the right-click context menu to toggle constraint display, contour labels, and colorbar, and control other options such as number and placing of contour levels.

## Pareto Front Graphs

The Pareto Front Graphs (click $\square_{\text {) }}$ are for multiobjective optimization where there is more than one solution at each run. The Pareto Front graphs show the available solutions for the selected run with the current selection highlighted in red. Click in the tables or graphs to select solutions. The selected solution is displayed in all other graphs (objective and constraint).

Before you run an NBI optimization you can specify how many solutions you want the optimization to find, using the Set Up and Run Optimization toolbar button to access the Optimization Parameters dialog box.


You can use the Pareto Front graphs in combination with the table views (Solution Slice and Pareto Slice) and the other plots in the graphs (Objective Slice and Constraint Slice graphs) to help you select best solutions for each run. You can collect these solutions together in the "Selected Solution Slice" on page 6-57.

## Constraint Slice Graphs

The Constraint Slice graphs (click ) show the constraint functions at the selected operating point with the solution value in orange. Click in the tables to select solutions to display. Yellow areas show a region outside a constraint.


This example shows the constraint EXTEMP $\leq 1290^{\circ} \mathrm{C}$.
The constraint graphs (the blue lines) show how the Left Value of each output of a constraint (in this case, the EXTEMP model) depends on the free variables in the optimization (in this case S, EXH and INT). The Left Value is compared with a plot of the Right Value output (in this case, $1290^{\circ} \mathrm{C}$ ) on the same axes.

The red horizontal line denotes the Right Value (i.e., the upper bound on EXTEMP) which in this case is $1290^{\circ} \mathrm{C}$ ). Because this value is an upper bound, the yellow region above the red line shows where the constraint is infeasible. The vertical orange lines show the optimal values of the free variables; the intersection of these with the blue lines is marked with a blue triangle on the Constraint1 axis-this intersection is the Left Value ( $1290^{\circ} \mathrm{C}$ ) at the optimal settings. These are the Left and Right values in the Constraint Summary table for Constraint1. See "Constraint Summary Table" on page 6-63.

Use the right-click context menu to alter graph size.
See also "Range Constraint Output" on page 6-64 for an explanation of range constraint graphs, and "Constraint Graphs" on page 6-72 for specific sum optimization features, such as a table gradient constraints.

## Constraint Summary Table

The Constraint Summary Table (click each constraint edge for the selected solution in the table. This view can be useful to see at a glance if a solution met all the constraints. If there are many constraints it can be time-consuming to use the constraint graphs for verification. If you are using equality constraints or tight table gradient constraints, the graphs can appear entirely yellow and you can only see whether a feasible solution has been found by looking at the Constraint Summary Table.

| Constraint Summary |  |  |  | 甘 中 $\times$ |
| :---: | :---: | :---: | :---: | :---: |
| Name | Description | Constraint Edge Distance | Left Value | Right Value |
| $\square$ Constraint1 | EXTEMP(S, N, L, EXH, INT) $<=1290$ | $6.63058 \mathrm{e}-008$ | 1290 | 1290 |
| $\square$ Constraint2 | RESIDFRAC(S, N, L, EXH, INT) $<=17$ | 7.77719 | 9.22281 | 17 |
| $\square$ Constraint3 | Boundary constraint of BTQ $(S, N, L, E X H, ~ I N T)$ | 0.651531 | -0.651531 | 0 |
|  |  |  |  |  |

Constraint edge distances greater than zero appear in red. These results should be checked as they may show the optimization failed to find a solution within the constraint, or they may be within tolerance (very close to zero). Constraint edge distances less than zero are within the constraint and shown in black.

Constraints are evaluated as inequalities, e.g., Constraint1, as shown in the preceding figure, is EXTEMP $\leq 1290^{\circ}$ C. The Left Value shows the left hand side of the inequality at the optimal settings of the free variables (in this case, the output of the constraint model (EXTEMP), which is $1290^{\circ} \mathrm{C}$ ). The Right Value shows the right hand side of the inequality (in this case, the upper bound, $1290^{\circ} \mathrm{C}$ ). The constraint edge distance is the difference between the Left and Right values.

For additional information on working with constraints, see the following topics:

- "Range Constraint Output" on page 6-64 for an explanation of range constraints in the summary table.
- "Constraint Summary" on page 6-73 for specific sum optimization features, such as table gradient constraint outputs.


## Range Constraint Output

The range constraint output is best explained using an example problem.
Control parameters or free variables: S, EXH, INT
Fixed variables: N, L
Objective: Maximize TQ(S, EXH, INT, N, L) at the fixed values shown in the following table.

| Run | $\mathbf{N}$ | $\mathbf{L}$ |
| :--- | :--- | :--- |
| 1 | 3000 | 0.5 |
| 2 | 4000 | 0.6 |

Constraint: Restrict $S$ between an upper and lower bound shown in the following table.:

| Run | $\mathbf{N}$ | $\mathbf{L}$ | Min S | Max S |
| :--- | :--- | :--- | :--- | :--- |
| 1 | 3000 | 0.5 | 20 | 30 |
| 2 | 4000 | 0.6 | 30 | 40 |

When the optimization is run the optimizer returns the following optimal values of S, EXH and INT, as the following table shows.

| Run | $\mathbf{N}$ | $\mathbf{L}$ | Optimal S | Optimal <br> EXH | Optimal INT |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 3000 | 0.5 | 21.33 | 8.593 | 29.839 |
| 2 | 4000 | 0.6 | 30 | 5 | 7.767 |

Range constraints implement the following expression:
Lower Bound $(\mathrm{LB}) \leq$ Expression $\leq$ Upper Bound (UB)
In CAGE, this expression is implemented as two upper-bound constraints, namely:

$$
\left[\begin{array}{l}
\text { RangeConLeft(1) } \\
\text { RangeConLeft(2) }
\end{array}\right]=\left[\begin{array}{c}
- \text { Expression } \\
\text { Expression }
\end{array}\right] \leq\left[\begin{array}{c}
-L B \\
U B
\end{array}\right]=\left[\begin{array}{l}
\text { RangeConRight }(1) \\
\text { RangeConRight }(2)
\end{array}\right]
$$

A range constraint returns two values at each operating point within a run, as shown in the following expression:

$$
\left[\begin{array}{l}
\text { RangeConOut }(1) \\
\text { RangeConOut }(2)
\end{array}\right]=\left[\begin{array}{c}
- \text { Expression }+L B \\
\text { Expression }-U B
\end{array}\right]
$$

The two values that the range constraint returns are the distance from the lower bound, RangeConOut(1), and the distance from the upper bound, RangeConOut(2), respectively.

The constraint in the example problem is
$\mathrm{LB}(\mathrm{N}, \mathrm{L}) \leq \mathrm{S} \leq \mathrm{UB}(\mathrm{N}, \mathrm{L})$
CAGE implements this constraint as

$$
\left[\begin{array}{c}
-S \\
S
\end{array}\right] \leq\left[\begin{array}{c}
-L B(N, L) \\
U B(N, L)
\end{array}\right]
$$

and returns the following two values at each operating point within a run to the optimizer (in this point-by-point example there is only one point per run):
$\left[\begin{array}{l}\text { RangeConOut }(1) \\ \text { RangeConOut }(2)\end{array}\right]=\left[\begin{array}{c}-S+L B(N, L) \\ S-U B(N, L)\end{array}\right]$

| Optimization Output Values |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Vector display format: Expanded vertically |  |  |  |  |  |  |  |  |  |  |
| Variable: |  | S | EXH | INT |  | L | S_LowerBound | S_UpperBound | Objective1 | Constraint1 |
| Number of values: |  | 1 | 1* | 1* | 1* | $1 \div$ | $1 *$ | $1 *$ | $1 \stackrel{1}{*}$ | $2 \div$ |
| 1 | (1) | 21.33 | 8.597 | 29.832 | 3000 | 0.5 | 20 | 30 | 92.467 | -1.33 |
|  | (2) |  |  |  |  |  |  |  |  | -8.67 |
| 2 | (1) | 30 | -5 | 7.767 | 4000 | 0.6 | 30 | 40 | 118.285 | 0 |
|  | (2) |  |  |  |  |  |  |  |  | -10 |

The Optimization Output Values pane shows the fixed variable settings, the optimal free variable settings, and the evaluation of objectives and constraints at the optimal free variable settings. In this example, the output of the range constraint at the optimal free variable settings is shown in the Constraint1
column. For each operating point in a run, two values are returned from the range constraint.

Looking at the first run:
Optimal S value $=21.33^{\circ}$
To calculate the distances returned from the range constraint:
Distance from lower bound: RangeConOut(1) $=21.33^{\circ}+20^{\circ}=-1.33^{\circ}$
Distance from upper bound: RangeConOut(2) $=21.33^{\circ}-30^{\circ}=-8.67^{\circ}$
These are the values shown in the Constraint1 column. Remember that negative constraint values mean that the constraint is feasible. The same values appear in the Constraint Summary Table for the selected run, but here absolute values appear in the Constraint Edge Distance column, as shown in the following figure.

| Constraint Summary |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Name | Description | Constraint Edge Distance | Left Value | Right Value |
| $\triangle$ Constraint1(1) | S_LowerBound <= S <= S_UpperBound | 1.33021 | -21.3302 | 20 |
| $\triangle$ Constraint1(2) | S_LowerBound <= S <= S_UpperBound | 8.66979 | 21.3302 | 30 |
|  |  |  |  |  |

The Constraint Edge Distance gives a measure of the distance to the constraint boundary for each constraint output. If the Left Value > Right Value for any of the constraint outputs, the constraint edge distance is colored red. This color coding means that this constraint distance should be checked to see if the constraint is feasible at that point (it may be within tolerance, or it may be infeasible).


The Objective Graphs show cross-section plots of the objective function against each free variable in the problem. The left plot is a plot of the objective function against S, with EXH and INT at their optimal values, for the second run. The range constraint for the second operating point ( $30 \leq S \leq 40$ ) can be seen; within the constraint region is white, and all other regions outside the constraint are yellow.


The constraint graphs for a range constraint shows how the Left Value of each output of a range constraint depends on the free variables in the optimization. The Left Value is compared with a plot of the Right Value output on the same axes. This comparison is illustrated for the example problem at the second run, as shown in the top left graph.

Constraint1(1) is the first Left Value of the range constraint, RangeConLeft(1), for the first run in the example problem. The top-left graph shows a blue line, which is a plot of RangeConLeft(1) against S (the constrained variable) with all other free variables set to their optimal values. The red horizontal line denotes the Right Value (RangeConRight(1), i.e., the upper bound on S ) which in this case is $-20^{\circ}$. Because this value is an upper bound, the yellow region above the red line shows where the table gradient constraint is infeasible. The vertical orange line shows the optimal value of S ; the intersection of this line with the blue line is marked with a blue triangle on the Constraint1(1) axis-the triangle marks the Left Value ( $-21.3^{\circ}$ ) at the optimal settings. These are the Left and Right values in the Constraint Summary table for Constraint1(1).

Constraint1(2) is the second Left Value of the range constraint, RangeConLeft(2), for the first run in the example problem. The bottom left graph shows a blue line plot of RangeConLeft(2) against $S$ with all other free variables set to their optimal values. The horizontal red line denotes the Right Value (RangeConRight(2)) which in this case is $30^{\circ}$. Because this value is an upper bound, the yellow region above the red line denotes where the table gradient constraint is infeasible. The vertical orange line shows the optimal value of S; the intersection of this with the blue line is marked with a blue triangle on the Constraint1(2) axis-the triangle marks the Left Value ( $21.3^{\circ}$ ) at the optimal settings. These are the Left and Right values in the Constraint Summary table for Constraint1(2).

In this example, the range constraint does not depend on EXH or INT, so the constraint graphs against these variables are blank.

## Interpreting Sum Optimization Output

Some features of the output node are specific to sum optimizations. Using the Example Problem (see "Example Sum Optimization" on page 6-33) for reference these features are described in the following sections:

- "Operating Point Indices" on page 6-69
- "Optimization Output Values Table" on page 6-70
- "Objective Graphs" on page 6-71
- "Objective Contour Plot" on page 6-72
- "Constraint Graphs" on page 6-72
- "Constraint Summary" on page 6-73
- "Table Gradient Constraint Output" on page 6-74


## Operating Point Indices

As in the Input Variable Values pane in the Optimization view, in the output view, the index of the operating point within a run is denoted by the number in brackets. The following figures provide examples.

| Optimization Output Values |  |  |  |
| :---: | :---: | :---: | :---: |
| Vector display format: |  |  | xp |
| Variable: |  | S |  |
| Number of values: |  | $5 \stackrel{\square}{\square}$ | $\Gamma$ |
| 1 | (1) | 15.112 |  |
|  | (2) | 17.859 |  |


| FreeVariableValues |  |  |
| :--- | :--- | :--- |
| $\mathrm{S}(1)$ | 15.1122816206 | $\Delta$ |
| $\mathrm{~S}(2)$ | 17.8594565528 |  |
| $\mathrm{~S}(3)$ | 18.4487986985 |  |
| $\mathrm{~S}(4)$ | 23.0664558695 |  |
| $\mathrm{~S}(5)$ | 27.1807926264 |  |
| $\mathrm{EXH}(1)$ | 22.3159450349 |  |



In the Optimization Output Values table, the index of the operating point within the run is shown in brackets. In the Free Variable Values table and graphical displays, the input variable at the i-th operating point within a run is denoted by InputVariableName(i), for example, $\mathrm{S}(4)$ is the spark value at the 4 th operating point, $\operatorname{EXH}(1)$ is the value of exhaust valve timing at the first operating point.

## Optimization Output Values Table

Features of the Optimization Output Values table are labeled in the following figure.


## Key to Optimization Output Values Table

- A: The run index - Index into the set of operating points that is being displayed.
- B: The quantity index.
- For fixed and free variables this index corresponds to the index of the operating point within the run.
- For objectives this corresponds to the index of the output for the specific labelled objective.
- For constraints this corresponds to the index of the output for the specific labelled constraint.
- C: Optimal Free Variable Settings - The optimal settings in this case of S, EXH and INT at each operating point in the run. For example, the optimal settings of S, EXH and INT at the third operating point in this run 1 are $\mathrm{S}=18.565^{\circ}$, $\mathrm{EXH}=24.801^{\circ}$, $\mathrm{INT}=41.214^{\circ}$
- D: Fixed Variable Settings - These settings define the operating points for the run and other fixed variables (such as weights) required for objectives and constraints. These values were set up before the optimization was run.

For information on the set up of these values, see "Using Variable Values Length Controls" on page 6-34.

- E: Optimal objective outputs - The optimal values of any objective outputs are displayed here, e.g., the optimized value of the weighted sum of TQ ( 115.002 Nm ) in this case.
- F,G: Constraint outputs at optimized control parameter settings - The value of constraint outputs are displayed here. For the example problem, the model constraint outputs are displayed in the section labeled F. Note that the number of constraint outputs matches the number of operating points. The table gradient constraint outputs are displayed in the section labeled G. The number of values returned by the table gradient constraint is dependent on the internal settings of that constraint. For more information on the number of values returned by objectives and constraints, see "Algorithm Restrictions" on page 6-38.


## Objective Graphs

The objective graphs for sum objective problems show the objective cross section plots as in the point-by-point case. However, plots are now displayed against each control parameter at each point in the set of operating points within each run. In the following figure, the weighted sum of TQ is plotted against the spark values at the first four operating points in run 1.


## Objective Contour Plot

The objective contour plot for sum objective problems shows the contours of the objective as in the point-by-point case. However, plots can now be displayed against any pair of control parameters chosen from all the control parameters at each point in the set of operating points within each run. In the following figure, a contour plot of the weighted sum of TQ is plotted against the value of exhaust valve timing for the third operating point, $\operatorname{EXH}(3)$ and the value of intake valve timing for the fourth operating point, INT (4).
Objective Contours

## Constraint Graphs

The constraint graphs for sum objective problems show the cross section plots of the left hand side of the constraints as in the point-by-point case. However, in the sum case there are several more inputs and outputs that can be plotted. Specifically, each constraint can return several outputs (see "Algorithm Restrictions" on page 6-38 for more detail) and these can be displayed against each control parameter at each point in the set of operating points within each run.


In the example problem, the exhaust temperature and residual fraction constraints have 5 outputs, one for each operating point. In the graphs shown, one output of the exhaust temperature and residual fraction constraints is displayed against four free variables. Specifically, the exhaust temperature model evaluated at the fifth operating point in run 1 (Constraint1(5)) and the residual fraction model evaluated at the first operating point in run 1 (Constraint2(1)) is plotted against the values of exhaust valve timing at operating points 4 and $5(E X H(4)$ and EXH (5)) plus the values of intake valve timing at operating points 1 and 2 (INT(1) and INT(2)).

See also "Table Gradient Constraint Output" on page 6-74.

## Constraint Summary

The constraint summary for sum optimizations shows a summary of all the constraint outputs for each constraint at the optimized control parameter settings. Part of the constraint summary table for the Example problem is shown in the following figure.

| Constraint Summary |  |  |  | \#虫 $\times$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Name | Description | Constraint Edge Distance | Left Value | Right Value | - |
| $\triangle$ Constraint1(1) | EXTEMP(S, N, L, EXH, INT $)<=1290$ | 153.321 | 1136.68 | 1290 |  |
| - Constraint1(2) | EXTEMP(S, N, L, EXH, INT $)<=1290$ | 184.163 | 1105.84 | 1290 |  |
| $\square$ Constraint1(3) | EXTEMP(S, N, L, EXH, INT $)<=1290$ | 151.336 | 1138.66 | 1290 |  |
| $\square$ Constraint1(4) | EXTEMP(S, N, L, EXH, INT $)<=1290$ | 162.578 | 1127.42 | 1290 |  |
| $\square$ Constraint1(5) | EXTEMP(S, N, L, EXH, INT $)<=1290$ | 165.434 | 1124.57 | 1290 |  |
| Constraint2(1) | RESIDFRAC(S, N, L, EXH, INT) <= 17 | $2.96633 \mathrm{e}-008$ | 17 | 17 |  |
| - Constraint2(2) | RESIDFRAC(S, N, L, EXH, INT $)<=17$ | $3.19401 \mathrm{e}-008$ | 17 | 17 |  |
| $\square$ Constraint2(3) | RESIDFRAC $(S, N, L, E X H, I N T)<=17$ | $4.80789 \mathrm{e}-011$ | 17 | 17 |  |
| - Constraint2(4) | RESIDFRACL $(S, N, L, E X H, I N T)<=17$ | 0.954605 | 16.0454 | 17 |  |
| $\square$ Constraint2(5) | RESIDFRAC(S, N, L, EXH, INT) < $=17$ | $9.01228 \mathrm{e}-009$ | 17 | 17 |  |
| $\square$ Constraint3(1) | Gradient constraint of INT over (N,L) | 0.00663488 | 0.00436512 | 0.011 |  |
| Constraint3(2) | Gradient constraint of INT over (N,L) | 0.0067411 | 0.0042589 | 0.011 |  |
| $\square$ Constraint3(3) | Gradient constraint of INT over (N,L) | 0.00701456 | 0.00398544 | 0.011 |  |
| Constraint3(4) | Gradient constraint of INT over (N,L) | 0.00712369 | 0.00387631 | 0.011 |  |
| Constraint3(5) | Gradient constraint of INT over (N,L) | 0.00692299 | 0.00407701 | 0.011 |  |
| $\square$ Constraint3(6) | Gradient constraint of INT over (N,L) | 0.00708754 | 0.00391246 | 0.011 |  |
| C Constraint3(7) | Gradient constraint of INT over (N,L) | 0.0153651 | 0.00436512 | -0.011 |  |
| Constraint3(8) | Gradient constraint of INT over (N,L) | 0.0152589 | 0.0042589 | -0.011 |  |
| Constraint3(9) | Gradient constraint of INT over (N,L) | 0.0149854 | 0.00398544 | -0.011 | - |

Three of the four constraints in the example problem are shown, Constraints 1,2 and 3 .

A summary of the first constraint, EXTEMP $<=1290^{\circ} \mathrm{C}$ at each operating point (Constraint1), is shown in the first five rows of the table. In this case, each of the rows corresponds to an evaluation of the constraint at each operating point within the run. For example, Constraint1(2) details an evaluation of EXTEMP $<=1290^{\circ} \mathrm{C}$ at the second operating point in the set of operating points in the run.

Part of the summary for the first table gradient (Constraint3) is shown. For a detailed explanation of table gradient outputs, see the next section, "Table Gradient Constraint Output" on page 6-74.

## Table Gradient Constraint Output

The table gradient constraint output is best explained using an example problem.

Control parameters/free variables: SPK, EXH, INT
Fixed variables: N, L
Objective: Maximize Weighted sum of TQ(SPK, EXH, INT, N, L) over the points shown in the following table (with unit weights at each point):

| $\mathbf{N}$ | $\mathbf{L}$ |
| :--- | :--- |
| 3000 | 0.5 |
| 3000 | 0.6 |
| 4000 | 0.5 |
| 4000 | 0.6 |

Table Gradient Constraint: Maximum change in EXH is bounded by the following specifications:

- No more than $5^{\circ}$ per 1000 rpm change in N
- No more than $4^{\circ}$ per 0.1 change in L
- Over the following 2-by-2 table: N breakpoints $=$ [3000 4000]; L breakpoints $=\left[\begin{array}{ll}0.5 & 0.6\end{array}\right]$

In this case, the optimization operating points are the same as the selected table breakpoints for the table gradient constraint, but these are not necessarily always the same.

When the optimization has run, the following optimal values of EXH are returned from the optimizer, as shown in the following tables.

| $\mathbf{N} / \mathbf{L}$ | $\mathbf{L}(\mathbf{1})$ | $\mathbf{L}(\mathbf{2})$ |
| :--- | :--- | :--- |
| $\mathbf{N}(\mathbf{1})$ | $\operatorname{EXH}(1)$ | $\operatorname{EXH}(2)$ |
| $\mathbf{N}(\mathbf{2})$ | $\operatorname{EXH}(3)$ | $\operatorname{EXH}(4)$ |

The values for all these items are shown in the following table.

| $\mathbf{N} / \mathbf{L}$ | $\mathbf{0 . 5}$ | $\mathbf{0 . 6}$ |
| :--- | :--- | :--- |
| $\mathbf{3 0 0 0}$ | 2.225 | 0 |
| $\mathbf{4 0 0 0}$ | -2.775 | -5 |

Table gradient constraints calculate the gradient between the values of specified free variable at the specified table points specified by the constraint. In the example problem, the table gradient constraint returns a set of constraint values as follows.

The table gradient constraint takes the values of EXH from the optimizer, and then determines the value of EXH at the grid points defined in the table gradient constraint. In this case, those grid points are the same, so this is identical to the preceding table. In cases where the grid points in the optimization do not match those in the table gradient constraint, a radial basis function interpolant is used to estimate the constrained variable on the table gradient grid points.

The table gradient constraint takes the grid of EXH values and calculates row and column gradients. Row gradients in the direction of increasing $\mathrm{N}, \mathrm{rg}^{\text {inc }}$, are calculated on the grid as follows:
$r g_{1}^{i n c}=(\operatorname{EXH}(3)-\operatorname{EXH}(1)) /(\mathrm{N}(2)-\mathrm{N}(1))$
$=(-2.775-2.225) / 1000$
$=-0.005$
$r g_{2}{ }^{\text {inc }}=(\operatorname{EXH}(4)-\mathrm{EXH}(2)) /(\mathrm{N}(2)-\mathrm{N}(1))$
$=(-5-0) / 1000$
$=-0.005$
The table gradient constraint restricts the row and column gradients in each direction. Row gradients in the direction of decreasing $\mathrm{N}, r g^{d e c}$, are calculated on the grid as follows:
$r g_{1}{ }^{\text {dec }}=-r g_{1}{ }^{\text {inc }}=0.005$
$r g_{2}{ }^{\text {dec }}=-r g_{2}{ }^{\text {inc }}=0.005$
Column gradients in the direction of increasing $\mathrm{L}, c g^{i n c}$, are calculated on the grid as follows:
$c g_{1}^{\text {inc }}=(\mathrm{EXH}(2)-\mathrm{EXH}(1)) /(\mathrm{L}(2)-\mathrm{L}(1))$
$=(0-2.225) / 0.1$
$=-22.25$
$c g_{2}{ }^{\text {inc }}=(\mathrm{EXH}(4)-\mathrm{EXH}(3)) /(\mathrm{L}(2)-\mathrm{L}(1))$
$=(-5-(-2.775)) / 0.1$
$=-22.25$
Similarly, column gradients in the direction of decreasing $\mathrm{N}, r g^{d e c}$, are calculated on the grid as follows:
$c g_{1}{ }^{\text {dec }}=-c g_{1}{ }_{1}^{\text {inc }}=22.25$
$c g_{2}{ }^{\text {dec }}=-c g_{2}{ }^{\text {inc }}=22.25$
The table gradient constraint implements the following:
$\left[\begin{array}{l}r g_{1}{ }^{\text {inc }} \\ r g_{2}{ }^{i n c} \\ r g_{1}{ }^{\text {dec }} \\ r g_{1}{ }^{\text {iec }} \\ \operatorname{cg}_{1}{ }_{1}{ }^{i n c} \\ c g_{2}{ }^{i n c} \\ c g_{1}{ }^{\text {dec }} \\ c g_{1}{ }^{\text {dec }}\end{array}\right] \leq\left[\begin{array}{c}5 / 1000 \\ 5 / 1000 \\ 5 / 1000 \\ 5 / 1000 \\ 4 / 0.1 \\ 4 / 0.1 \\ 4 / 0.1 \\ 4 / 0.1\end{array}\right]$

This equation can be rewritten as Left Value <= Right Value. The left and right values from these calculations are displayed in the Constraint Summary table, as shown in the following figure.

| Constraint Summary |  |  |  | ㅂ\|由 $\times$ |
| :---: | :---: | :---: | :---: | :---: |
| Name | Description | Constraint Edge Distance | Left Value | Right Value |
| $\triangle$ Constraint4(1) | Gradient constraint of EXH over ( $\mathrm{N}, \mathrm{L}$ ) | 0.01 | -0.005 | 0.005 |
| $\triangle$ Constraint(2) | Gradient constraint of EXH over (N,L) | 0.01 | -0.005 | 0.005 |
| Constraint(3) | Gradient constraint of EXH over (N,L) | $8.88178 \mathrm{e}-019$ | 0.005 | 0.005 |
| $\triangle$ Constraint4(4) | Gradient constraint of EXH over (N,L) | $3.14627 \mathrm{e}-009$ | 0.005 | 0.005 |
| $\triangle$ Constraint4(5) | Gradient constraint of EXH over (N,L) | 62.2504 | -22.2504 | 40 |
| $\triangle$ Constraint(6) | Gradient constraint of EXH over (N,L) | 62.2504 | -22.2504 | 40 |
| $\triangle$ Constraint(7) | Gradient constraint of EXH over (N,L) | 17.7496 | 22.2504 | 40 |
| Constraint(8) | Gradient constraint of EXH over (N,L) | 17.7496 | 22.2504 | 40 |

The column of numbers under Left Value shows the row and column gradient results calculated previously, i.e.:

$$
\left[\begin{array}{l}
r g_{1}{ }^{\text {inc }} \\
r g_{2}{ }^{i n c} \\
r g_{1}{ }^{d e c} \\
r g_{1}{ }^{d e c} \\
\operatorname{cg}_{1}{ }^{i n c} \\
\text { cg }_{2}{ }^{\text {inc }} \\
c g_{1}{ }^{d e c} \\
c g_{1}{ }^{d e c}
\end{array}\right]=\left[\begin{array}{c}
-0.005 \\
-0.005 \\
0.005 \\
0.005 \\
-22.25 \\
-22.25 \\
22.25 \\
22.25
\end{array}\right]
$$

The column of numbers under Right Value shows the maximum gradient (the upper bound) allowed by the constraint, i.e.:

$$
\left[\begin{array}{c}
5 / 1000 \\
5 / 1000 \\
5 / 1000 \\
5 / 1000 \\
4 / 0.1 \\
4 / 01 \\
4 / 01 \\
4 / 01
\end{array}\right]=\left[\begin{array}{c}
0.005 \\
0.005 \\
0.005 \\
0.005 \\
40 \\
40 \\
40 \\
40
\end{array}\right]
$$

In each row the Left Value must be smaller than the Right Value to meet the constraint.

The Constraint Edge Distance is equal to the absolute value of (Left Value minus Right Value) and gives a measure of the distance to the constraint boundary for each constraint output. If the Left Value > Right Value for any of the constraint outputs, the constraint edge distance is colored red. This color coding indicates that this constraint distance should be checked to see if the constraint is feasible at that point. It may be infeasible, or it may be within the tolerance.

The Constraint Edge Distance values are calculated as follows from Left Value minus Right Value.

$$
\left[\begin{array}{l}
r g_{1}{ }^{i n c} \\
r g_{2}{ }^{i n c} \\
r g_{1}{ }^{d e c} \\
r g_{1}{ }^{d e c} \\
\text { gg }_{1}{ }^{i n c} \\
c g_{2}{ }^{i n c} \\
c g_{1}{ }^{d e c} \\
c g_{1}{ }^{d e c}
\end{array}\right]-\left[\begin{array}{c}
5 / 1000 \\
5 / 1000 \\
5 / 1000 \\
5 / 1000 \\
4 / 0.1 \\
4 / 01 \\
4 / 01 \\
4 / 01
\end{array}\right]=\left[\begin{array}{c}
-0.005 \\
-0.005 \\
0.005 \\
0.005 \\
-22.25 \\
-22.25 \\
22.25 \\
22.25
\end{array}\right]-\left[\begin{array}{c}
0.005 \\
0.005 \\
0.005 \\
0.005 \\
40 \\
40 \\
40 \\
40
\end{array}\right]=\left[\begin{array}{c}
-0.01 \\
-0.01 \\
0 \\
0 \\
-62.25 \\
-62.25 \\
-17.75 \\
-17.75
\end{array}\right]
$$

These Constraint Edge Distance values are also shown in the Optimization Output Values table, but here they are signed-negative constraint values mean the constraint is feasible. In the following figure, these values appearin the Constraint4 column. The Optimization Output Values pane also shows the fixed variable settings, the optimal free variable settings, and the evaluation of objectives and constraints at the optimal free settings.


The constraint graphs for a table gradient constraint show how the Left Value of each output of a table gradient constraint depends on the free variables in the optimization. These graphs for the example problem appear in the following figure.


The Left Value is compared with a plot of the Right Value output on the same axes. This comparison is illustrated for the table gradient example problem. Consider the top-left graph in the figure shown. Constraint4(1) in figure 2 is the first Left Value ( $r g_{1}{ }^{\text {inc }}$ ) of the table gradient constraint in the example problem. Recall that this can be written as
$r g_{1}^{i n c}=(\mathrm{EXH}(3)-\mathrm{EXH}(1)) /(\mathrm{N}(2)-\mathrm{N}(1))$
The top left graph shows a plot of $r g_{1}{ }^{i n c}$ against EXH(1) with all other free variables set to their optimal values, i.e.,
$r g_{1}^{\text {inc }}=(2.775-\mathrm{EXH}(1)) / 1000$
which is the blue line shown in the top left graph. The horizontal red line shows the Right Value (i.e., the upper bound on $r g_{1}^{i n c}$ ). Because this value is an upper bound on the allowable gradient, the yellow region above the line shows where the table gradient constraint is infeasible. The vertical orange line shows the optimal value of the free variable, EXH(1). The blue marker on the Constraint4(1) axis marks the Left Value (the value of $r g_{1}^{i n c}$ ) at the intersection of the optimal $\operatorname{EXH}(1)$ value and the blue line.

The graph of Constraint4(1) against EXH(2) shows a flat line. The flat line indicates that there is no dependence of $r g_{1}^{i n c}$ on $\operatorname{EXH}(2)$, as it is calculated as $(\operatorname{EXH}(3)-\operatorname{EXH}(1)) /(\mathrm{N}(2)-\mathrm{N}(1))$.

The other constraint graphs can be analyzed in a similar way.

Note If you are using table gradient constraints the solution may appear infeasible upon inspection of the objective and constraint graphs (the graphs may appear to be entirely yellow). There are cases when the solution is actually feasible in this case. This appearance of infeasibility often arises in sum problems which have tight table gradient constraints. In such cases, you should check the Solution Information pane and the Constraint Summary Table to check whether a feasible solution has been found.

## Filling Tables from Optimization Results

There are two methods for filling tables with optimization results.
1 At the Optimization_Output node, select Solution > Fill Tables, or click the toolbar button

The Table Filling wizard appears.
2 Select the tables to fill, and click the button to add them to the list of tables to be filled. Click Next.

3 For each table to be filled, select the correct variable or model output from the list of optimization results and click the button to match them, as shown in this example.


In a single objective optimization there is only one solution for each operating point so by default you will fill the table with solution 1 . In a multiobjective optimization there is more than one solution per point. You can select a solution number to use for every point, or you can select the other radio button to use your Selected Solution for each point. To collect your preferred solutions you must first use the "Selected Solution Slice" on page 6-57.

## 4 Select a Fill Method.

- Extrapolate Fill - uses the optimization results to fill the whole table by extrapolation.
- Direct Fill - fills only those table cells whose breakpoints exactly match the optimization points.
- Custom Fill - you can write your own table filling algorithm and use the file browser to select it. See "Custom Fill Function Structure" on page 6-84.

5 Exclude infeasible solutions - select this check box to include only optimization results that meet the constraints. This does not depend on the exit status of the optimization (exit flag), only a check to see if constraints are met. To view the exit flag and algorithm termination messages check the Solution Information pane in the Optimization Output view.

6 Add to extrapolation mask - when this check box is selected, filled table cells are added to the extrapolation mask.

If you use the wizard to repeatedly fill a table any existing extrapolation mask is added to. As an example, consider filling multiple zones of a table using results from different optimizations. All zones are cumulatively added to the mask. If there is overlap with previous fills cells are overwritten unless they are locked. Note that locked cells are never altered by table filling.

7 Click Finish to fill the tables.
You will see a dialog reporting successful table filling. Switch to the Tables view to examine the tables.

The other method of filling tables with optimization output uses Data Sets.
1 From the Optimization_Output optimization output node, click Export to


2 Go to the Data Sets view (click the Data Sets button in the Data Objects pane) to see that the table of optimization results is contained in the new data set. The new data set takes the name of the optimization and the suffix identifies that which solution number you exported from the optimization view.

You can now use this data set (or any optimization results) to fill tables, as you can with any data set.

3 Select the data set and click (Fill Table From Data Set) in the toolbar.
4 Clear the check box to Show table history after fill.
5 Choose to fill a table with the desired optimization output by selecting them in the two lists, then click the button Fill Table at the bottom right.

6 Right-click the display and select Surface to see the filled table surface and the optimization output values.

## See also

- "Tutorial: Filling Tables from Data" in the Getting Started documentation for more details on using data sets to fill tables.


## Custom Fill Function Structure

It can be useful to create your own function to fill tables from the results of an optimization, for example to implement alternative fill methods, smoothing strategies, or to customize output.

The input/output structure of a custom fill function resembles that of the MATLAB interpolation routines INTERP1 and INTERP2. To see the structure of the function it is best to look at an example:

1 Locate and open the file griddataTableFill.m in the mbctraining directory.

2 Type the following at the command line to open the example:

```
edit griddataTableFill
```

There are instructions for using this example in the optimization tutorial, "Using a Custom Fill Routine to Fill Tables", in the Getting Started documentation. This function is an example of a function that will fill 2-D tables from optimization results.

All 2-D custom fill functions must take the following six inputs, which will be supplied to it by CAGE when the function is called:

| Input | Description <br> col <br> row |
| :--- | :--- |
| Column coordinate of optimization results <br> $(N F-$ by -1$)$ |  |
|  | Row coordinate of optimization results <br> $(N F-b y-1)$ |


| Input | Description |
| :---: | :---: |
| filldata | Optimized results at (row, col) points (NF-by-1) |
| colaxis | Column breakpoints of table to be filled ( 1 -by-NCOL) |
| rowaxis | Row breakpoints of table to be filled (NROW-by-1) |
| currtabdata | Existing table values of table to be filled (NROW-by-NCOL) |

The function must pass three output arguments back to CAGE, to allow CAGE to fill the table:

| Output | Description |
| :--- | :--- |
| ok | Boolean flag to indicate success of the table <br> fill (TRUE or FALSE) |
| tabval | New table values of table to be filled <br> (NROW-by-NCOL) |
| fillmask | Logical matrix to indicate cells to be added <br> to the extrapolation mask as a consequence <br> of the table being filled (NROW-by -NCOL) |

In the above specifications:

- NF is the number of points from the optimization results that will be used to fill your tables
- NCOL is the number of column breakpoints in the table
- NROW is the number of row breakpoints in the table

Note that your function should handle the cases when the table fill is successful or not. In griddataTableFill, this is handled using the try-catch construct around the call to griddata. If griddata should fail, then the ok flag is set to false and the function returns.

## Custom Fill Function for 1-D Tables

You can also write custom fill functions to fill 1-D tables. In this case the input and output specifications are as follows:

| Input | Description |
| :--- | :--- |
| row | Row coordinate of optimization results (NF-by-1) |
| filldata | Optimized results at (row, col) points (NF-by-1) |
| rowaxis | Row breakpoints of table to be filled (NROW-by-1) |
| currtabdata | Existing table values of table to be filled (NROW-by-1) |
| Output | Description |
| ok | Boolean flag to indicate success of the table fill (TRUE or <br> FALSE) |
| tabval | New table values of table to be filled (NROW-by-1) <br> fillmaskLogical matrix to indicate cells to be added to the <br> extrapolation mask as a consequence of the table being <br> filled (NROW-by-1) |

## Automated Tradeoff

You can use automated tradeoff to run an optimization routine and fill your tradeoff tables. Once you have set up an optimization and a tradeoff, you can run an automated tradeoff. As with any other tradeoff you need at least one table. You can apply an optimization to a cell or region of a tradeoff table, or the whole table, and the tradeoff values found are used to fill the selected cells. If only filling selected cells you can then fill the entire table by extrapolation.

There is an example automated tradeoff in the optimization tutorial chapter, "Tutorial: Optimization and Automated Tradeoff" in the Getting Started documentation.

## Using Automated Tradeoff

1 You need a CAGE session with some models and a tradeoff containing some tables.

- See Chapter 5, "Tradeoff Calibrations" for instructions on setting up a tradeoff. You could use the tradeoff tutorial to generate a suitable example session.

You also need to set up an optimization before you can run an automated tradeoff. Objectives and constraints must be set up.

- For an example work through the step-by-step tutorial to set up some optimizations and then apply them to a tradeoff table. See "Tutorial: Optimization and Automated Tradeoff" in the Getting Started documentation.

2 Go to the tradeoff table you want to automate. You can select some table cells to apply the optimization to, or use the whole table, or fill only previously saved tradeoff points. Note that if you define a large region with many cells or a whole table it can take a long time to complete the optimization. You can select individual cells, or click and drag to select a rectangle of cells. The selected cells do not have to be adjacent. Try a small region (say up to six cells) to begin with. Right-click selected cells and select Extrapolation Regions -> Add Selection or use the toolbar button (to add selection to extrapolation regions).

# 3 To apply optimization: click $\downarrow \downarrow$ in the toolbar, or select Inputs -> Automated Tradeoff. 

- A dialog appears that allows an appropriate (defined below) optimization to be selected from the current project.

Note You must set up an optimization to run before you can perform an automated tradeoff. You do this in the Optimization view. See also "Setting Up Point-by-Point Optimizations" on page 6-8.

The set of cells in the region you have selected becomes the operating point set for the optimization. The cell/region breakpoint values are used to replace the fixed variable values in the selected optimization. Note that the existing fixed variable values are reset to their previous state at the end of the automated tradeoff.

If previous tradeoff values have been applied to a cell, those values are used for free variable initial values and non-table-axis fixed variables; otherwise the set points are used.

4 The optimization is run as if you were clicking Run from the Optimization view. See "Running Optimizations" on page 6-41.

Results are placed in the tradeoff object, that is, values for the tables involving the free variables or values for the tables for constraint or objective models. If the routine applied gives more than one solution, for example, an NBI optimization, then a solution which tries to trade off all objectives is placed in the tradeoff tables. Every cell in the defined region is filled.

5 The cells of the region become part of the extrapolation mask (as if apply point has been applied); so if you want you can then click Extrapolate in the toolbar to fill the rest of the table from your optimized automated tradeoff.


## What Are Appropriate Optimizations?

The list of all optimizations in the project is filtered. To be eligible for selection,

- The optimization must be ready to run (toolbar button enabled).
- The variables in the axes of the tradeoff tables must not be free variables in the optimization. For example, if one of the axes is speed, then speed cannot be a free variable.
- The fixed variables must be a subset of the variables in the axes of the tradeoff tables. For example, if the optimization requires variables Speed and Load, then these must be the axes variables in the tradeoff table.
- The optimization must either have N runs with all variables of length 1 , or a single run with all variables of length N .


## Multimodel Tradeoff

For a multimodel tradeoff, things work slightly differently. The multimodel is only defined for certain cells in the tradeoff tables. These are the operating
points that were modeled using the Model Browser part of the toolbox. Such cells are marked with a model icon as shown in the example, and you should select these for running the automated tradeoff. You can select any region, but the optimization can only find values for the operating points defined by the multimodel.


## User-Defined Optimization

User-defined optimizations are described in the following sections:

- "Implementing Your Optimization Algorithm in CAGE" on page 6-91 describes how to customize the optimization template to use your optimization routines in CAGE.
- There is a step-by-step guide to using the example provided to help you understand how to modify the template file to use your own optimization functions. See the optimization tutorial section"Worked Example Optimization" in the Getting Started documentation.

In many cases the standard routines supplied for constrained single and multiobjective optimization (foptcon and NBI) are sufficient to allow you to solve your optimization problem. Sometimes, however, you need to write a customized optimization algorithm. This can be useful in many situations, for example,

- For an expert to capture an optimization process to solve a particular problem, for example, determination of optimal spark angle and exhaust gas recirculation rate on a port-fuel injection engine
- To implement an alternative optimization algorithm to those supplied
- To implement a complex constraint or objective that is only possible through writing M-code
- To produce custom output graphics

User-defined optimization functions in CAGE allow advanced users to write their own optimization routines that can access current CAGE data. In order to access the user function from CAGE, you must register the M-file with CAGE and place it on the MATLAB path. It is crucial that this function conforms to the template specified. The following sections describe this process.

## Implementing Your Optimization Algorithm in CAGE

At some point a CAGE optimization function calls on an algorithm to optimize the objective functions over the free variables. You can implement the algorithm in the CAGE optimization function as an external M-file. Use
the template file as a basis for your optimization function. The best way to understand how to alter the template file to implement your own optimization algorithms is to compare it with the worked example, as described in the optimization tutorial.

- See the following optimization tutorial sections in the Getting Started documentation:
- "Worked Example Optimization" describes the process of using the worked example
- "Creating an Optimization from Your Own Algorithm" describes in detail the steps necessary to use an example optimization algorithm in CAGE
- "About the Worked Example Optimization Algorithm" on page 6-94
examines the coding involved in implementing an external optimizer in a CAGE optimization M-file
- "Checking User-Defined Optimizations into CAGE" on page 6-96 explains how to check in your optimization function so you can use it in CAGE


## Optimization Function Structure

The optimization function M-files have two sections. To compare these sections in the worked example with the template file on which it is based:

1 Locate and open the file mbcoStemplate in the mbctraining directory
2 Type the following at the command line to open the example:

```
edit mbcOSworkedexample
```

The two sections are the Options section and Evaluate section.
1 The Options function section contains the settings that define your optimization. Here you can set up these attributes:

- Name
- Description
- Free variables
- Objective functions
- Constraints
- Helper data sets
- Optimization parameters

CAGE interacts with the cgoptimoptions object, where all these settings are stored.

See "Methods of cgoptimoptions" on page 6-98 for information about setting up the options section.

If you leave the cgoptimoptions function unchanged, your optimization function must be able to support the default options. That is, your optimization will have:

- One objective
- Any number of constraints (selected by the user in CAGE )

2 The Evaluate function section contains your optimization routine. CAGE calls this section when the Run button is clicked.

Place your optimization routine under this section, interacting with CAGE (obtaining inputs and sending outputs) via the cgoptimstore object. Your optimization must conform to the following syntax:

```
optimstore = <Your_Optimization> (optimstore)
```

where <Your_Optimization> is the name of your optimization function.
Any subfunctions called by your optimization routine should also be placed at the bottom of this section.

See "Methods of cgoptimstore" on page 6-100.

Note Be careful not to overwrite the worked example and template files when you are trying them out - save them under a new name when you make changes.

There is a step-by-step guide describing how to modify the template using the worked example optimization function in the optimization tutorial. See "Worked Example Optimization" in the Getting Started documentation.

## About the Worked Example Optimization Algorithm

mbcweoptimizer is an example of a user-specified optimization that solves the following problem:
max TQ over (AFR, SPK).

- [bestafr, bestspk] = mbcweoptimizer(TQ) finds a maximum (bestafr, bestspk) to the function TQ.

TQ must be a function (or a function handle) that depends on [AFR, SPK, any other variables] only. The function must depend on the variables in that order. This routine does no variable matching.

- [bestafr, bestspk]=mbcweoptimizer(TQ, afrrng, spkrng) finds a maximum (bestafr,bestspk) to the function TQ.
afrrng and spkrng are 1-by-2 row vectors containing search ranges for those variables.
- [bestafr, bestspk]=mbcweoptimizer(TQ, afrrng, spkrng, res) finds a maximum (bestafr,bestspk) to the function TQ.

This optimization is performed over a res-by-res grid of (AFR, SPK) values. If res is not specified, the default grid resolution is 25 .

- [bestafr, bestspk]=mbcweoptimizer(TQ, afrrng, spkrng, res, optimstore) finds a maximum (bestafr,bestspk) to the function TQ within a CAGE optimization function.
optimstore is passed to this function when it is called from the Evaluate section subroutine of your optimization function. In this case, TQ must be a function handle that takes the inputs AFR, SPK, and OPTIMSTORE, in that order. Any other inputs for the TQ model will be set by CAGE.
- [bestafr, bestspk] = mbcweoptimizer(TQ, afrrng, spkrng, res, optimstore, P1, P2, ...) passes extra scalar arguments (in order) to the torque model when it is evaluated. In this case, the optimstore input is ignored.


## The Structure of the Worked Example

The best way to understand how to implement an external optimizer in a CAGE optimization function is to study the details of the example.

- To view the whole worked example M-file, at the command line, type

```
edit mbcOSworkedexample
```

The following code section is taken from the Evaluate section of the worked example file as an example.

```
* For every fixed point, find the optimum (afr, spk) using
* the mbcweoptimizer routine you have written
[bestafr, bestspk] = mbcweoptimizer (0i_evalTQ, [minA今FR, maxAFR], ...
    [minSPK, maxSPK], res, optimstore);
* Set the best values calculated for the free variable(s) into the output data set
optimstore = setFreevariables(optimstore, [bestafr, bestspk]);
* Return some information about the optimization
OUTPUT.Algorithm = 'Brute force search';
OUTPUT.Resolution = res;
* Set all information in the optimstore, and leave ....
optimstore = setExitStatus(optimstore, 1, 'Optimization Completed');
optimstore = setOutput (optimstore, OUTPUT);
```

The code fragment above is in the i_Evaluate subfunction. This subfunction is called once for each run of the script. The line of code labeled A above calls the worked example optimization algorithm external to the optimization function. As with functions in the Optimization Toolbox, the first argument to the call to the optimizer is a function handle that evaluates the objectives at a given input point. We recommend you place the function pointed at by the function handle in the optimization file. If you do not place them in the same file you must make sure the evaluate function M-file is on the MATLAB path. As an example, the optimization evaluation function in the worked example optimization is shown in the code fragment following.

```
function y = i_evalTQ(afr, spk, optimstore)
# = evaluate(optimstore, [afr, spk]);
    B
```

The first two inputs to this function are the torque (in this case) model inputs. The final input is the optimstore object, where information about the optimization is stored. To evaluate the objective, the evaluate method from the optimstore object is used. In the above example, the line of code referenced by B evaluates the torque model in the worked example at the (afr, $s p k$ ) input points. The values of ( $\mathrm{N}, \mathrm{L}$ ) at the current run are used in the evaluation of the torque model. CAGE retrieves these values from optimstore when the torque model is evaluated.

The two subfunctions presented above are an example of how to implement an external optimizer in a CAGE optimization M-file.

See also the optimization tutorial section"Creating an Optimization from Your Own Algorithm" in the Getting Started documentation, which describes in detail the steps involved in incorporating an example algorithm into a CAGE optimization M-file.

## Checking User-Defined Optimizations into CAGE

When you have modified the template to create your own optimization function, you must check it into the Model-Based Calibration Toolbox in order to use the function in CAGE. Once you have checked in your optimization function it appears in the Optimization Wizard. See "Optimization Wizard" on page 6-9.

To check a user-defined optimization into CAGE,

## 1 Select File -> Preferences.

2 Click the Optimization tab and click Add... to browse to your M-file. Select the file and click Open. This registers the optimization function with CAGE. You need to do this when you customize your own optimizations.


The example shows the worked example function, which is already registered with CAGE for use in the optimization tutorial.

3 You can click Test to check that the optimization function is correctly set up. This is a very useful function when you use your own functions; if anything is incorrectly set up the test results tell you where to start correcting your function.

You can see an example of this by saving a copy of the worked example file and changing one of the variable names (such as afr) to a number. Try to check this altered function into CAGE and the Test button will return an informative error specifying the line you have altered.

4 Click OK to dismiss the CAGE Preferences dialog and return to the CAGE browser.

Registered optimizations appear in the Optimization Wizard when you set up a new optimization.

## Optimization Function Reference

Following are the reference pages for all the functions you can use in user-defined optimizations. See the following tables for a list of available functions by category:

- "Methods of cgoptimoptions" on page 6-98
- "Methods of cgoptimstore" on page 6-100


## Methods of cgoptimoptions

You use these functions to set up all your optimization settings in the Options section of the file. You can set up any or all of these seven attributes:

- Name
- Description
- Free variables
- Objective functions
- Constraints
- Helper data sets
- Optimization parameters

The following methods are available:
addFreeVariable
addLinearConstraint
addModelConstraint
addObjective
addOperatingPointSet
addParameter
getConstraints

Add free variable to optimization Add linear constraint to optimization Add model constraint to optimization Add objective to optimization Add operating point set to optimization

Add parameter to optimization
Return information about all optimization constraints

| getConstraintsMode | Return current usage of constraints |
| :--- | :--- |
| getDescription | Get current description for <br> optimization function |
| getEnabled | Get current enabled status for <br> optimization |
| getFreeVariables | Return optimization free variable <br> labels |
| getFreeVariablesMode | Return current usage of free <br> variables |
| getLinearConstraints | Get linear constraint placeholder <br> information |
| getModelConstraints | Get model constraint placeholder <br> information |
| getName | Get current name label for <br> optimization function |
| getNonlcon | Get nonlinear constraint information <br> Return information about <br> optimization objectives |
| getObjectives | Return current usage of objective <br> functions |
| getObjectivesMode | Return information about <br> optimization operating point |
| getOperatingPointSets | sets |
| geturn current usage of operating |  |

removeObjective<br>removeOperatingPointSet<br>removeParameter<br>setConstraintsMode<br>setDescription<br>setEnabled<br>setFreeVariablesMode<br>setName<br>setObjectivesMode<br>setOperatingPointsMode<br>setRunInterfaceVersion

## Methods of cgoptimstore

The following methods are available:

| evaluate | Evaluate optimization objectives and <br> constraints |
| :--- | :--- |
| evaluateConstraint | Evaluate optimization constraints |
| evaluateNonlcon | Evaluate optimization nonlinear <br> constraints |
| evaluateObjective | Evaluate optimization objectives |
| get | Get optimization properties |

```
getA
getB
getDataset
getFreeVariables
getInitFreeVal
getLB
getLcon
getNumNonlcon
getNumNonlconLabels
getNumObjectiveLabels
getNumObjectives
getNumRowsInDataset
getObjectives
getObjectiveType
getOptimOptions
getOutputInfo
getParam
getStopState
getUB
gridEvaluate
```

Get linear inequality constraint matrix.

Get linear inequality constraint target values.

Retrieve data from data set
Get optimal values of free variables
Get initial free values for optimization

Get free variable lower bounds
Return linear constraint labels
Return number of nonlinear constraints per label

Return number of nonlinear constraint labels

Return number of objective labels
Return number of objectives per label

Get number of rows in optimization data set

Return objective labels for optimization

Return objective type
Retrieve optimization options object
Get output information for optimization

Get optimization parameter
Current stop state for optimization
Get free variable upper bounds
Grid evaluation of optimization objectives and constraints

| gridPevEvaluate | Grid evaluation of prediction error <br> variance (PEV) |
| :--- | :--- |
| isScalarFreeVariables | Return whether all free variables <br> are scalars |
| nEvaluate | Natural evaluation of optimization <br> objectives and constraints <br> Natural evaluation of optimization <br> constraints |
| nEvaluateConstraint | Natural evaluation of optimization <br> nonlinear constraints |
| nEvaluateNonlcon | Natural evaluation of optimization <br> objectives <br> Create/alter optimization OPTIONS <br> structure |
| nEvaluateObjective | Evaluate prediction error variance <br> (PEV) |
| pevEvaluate | Set exit status information for <br> optimization |
| setExitStatus | Set optimal values of free variables |
| setFreeVariables | Set diagnostic information for <br> optimization |
| setOutput | Set output information for <br> optimization |
| setOutputInfo | Set current stop state for <br> optimization |
| setStopState |  |

## Functions - Alphabetical List

## addFreeVariable

## Purpose

Add free variable to optimization
Syntax options = addfreeVariable (options, label)

Description
A method of cgoptimoptions. Adds a placeholder for a free variable to the optimization. The string label is used to refer to the variable in CAGE.

See Also setFreeVariablesMode, getFreeVariablesMode, getFreeVariables, removeFreeVariable

## Purpose Add linear constraint to optimization

```
Syntax
options = addLinearConstraint(options, label, A, B)
```

Description A method of cgoptimoptions. Adds a placeholder for a linear constraint to the optimization. The string label is used to refer to the constraint in the CAGE GUI. Linear constraints can be written in the form

$$
A(1) X(1)+A(2) X(2)+\ldots+A(n) X(n)<=b
$$

where $X(i)$ is the $i^{\text {th }}$ free variable, $A$ is a vector of coefficients, and $b$ is a scalar bound.

## Examples

```
% Add SPK and EGR variables to an optimization
opt = addFreeVariable(opt, 'SPK');
opt = addFreeVariable(opt, 'EGR');
% Add a linear constraint such that 3*SPK - 2*EGR <= 30
opt = addLinearConstraint(opt, 'newCon', [3 -2], 30);
```

See Also
getLinearConstraints, addModelConstraint, setConstraintsMode, removeConstraint

## addModelConstraint

| Purpose | Add model constraint to optimization |
| :--- | :--- |
| Syntax | options=addModelConstraint (options, label, boundtype, bound ) |
| Description | A method of cgoptimoptions. Adds a placeholder for a model constraint <br> to the optimization. The string label is used to refer to the constraint <br> in CAGE. <br> boundtype can be set either to the string 'greaterthan ' or 'lessthan ' <br> bound must be a scalar real. |
|  | If boundtype = 'greaterthan', the model constraint takes the following <br> form: <br> CAGE model >= bound |
|  | Similarly, if boundtype = 'lessthan', the model constraint takes the <br> form |
| CAGE model <= bound |  |

## Purpose Add objective to optimization

```
Syntax options = addObjective(options, label, typestr)
```

Description A method of cgoptimoptions. Adds a placeholder for an objective function to the optimization. The string label is used to refer to the constraint in CAGE.
typestr can take one of four values, 'max', 'min', 'min/max', or 'helper'.

## Examples

```
opt = addObjective(opt, 'newObj', 'max')
```

Adds an objective function labeled newObj to the optimization and indicates that it is to be maximized.

```
opt = addObjective(opt, 'newObj', 'min/max')
```

Adds an objective function labeled newObj to the optimization and indicates that the user should be allowed to choose whether it is minimized or maximized from CAGE.

```
opt = addObjective(opt, 'newObj2', 'helper')
```

Adds an objective function labeled newObj2 to the optimization. The string 'helper' indicates that the function is used as part of the determination of the cost function but is not directly minimized or maximized.

See Also getObjectives, setObjectivesMode, getObjectivesMode, removeObjective

## addOperatingPointSet

Purpose Add operating point set to optimization
Syntax options = addOperatingPointSet(options, label, vars)

Description A method of cgoptimoptions. Adds a placeholder for an additional operating point set to the optimization.
The string label is used to refer to the constraint in CAGE. vars is a ( $1-$ by $-N$ ) cell array of strings where $N>=1$. Each element of vars is a label for a CAGE variable that must appear in the operating point set that the user chooses.

See Also

getOperatingPointSets, setOperatingPointsMode, getOperatingPointsMode, removeOperatingPointSet

## Purpose

Add parameter to optimization

```
Syntax
```

```
options = addParameter(options, label, typestr, value)
```

```
options = addParameter(options, label, typestr, value)
```

Description
A method of cgoptimoptions. Adds a parameter to the optimization. The string label is used to refer to the parameter. The string typestr takes one of 'number', 'list', or 'boolean'. A default value for the parameter must be supplied in value. The form of value must be one of the following:

| typestr | Value |
| :--- | :--- |
| 'number' | Scalar, real number |
| 'list' | Cell array of strings, one for each <br> list member |
| 'boolean' | True or false |
| options = addParameter (options, label, typestr, value, <br> displayName) allows a more descriptive label to be used for the <br> parameter in the CAGE Optimization Parameters GUI. Note that you <br> still must refer to the parameter by label in the 'Evaluate' section of <br> your script. |  |

## See Also

## Purpose Evaluate optimization objectives and constraints

```
Syntax \(\quad Y=\) evaluate (optimstore, \(X\) )
```

Description A method of cgoptimstore.
Evaluate optimization objectives and constraints.
$Y=$ evaluate (optimstore, $X$ ) evaluates all of the optimization objectives and constraints at the free variable values X . X is a (NPoints-by-NFreeVar) matrix where NPoints is the number of points to be evaluated and NFreeVar is the number of free variables in the optimization.

## Examples

```
Y = evaluate(optimstore, X, itemnames)
```

evaluates the objectives and constraints specified in the cell array of strings, itemnames, at the free variable values X . The values of the objectives and constraints are returned in Y , which is of size (NPoints-by-NItems) where NItems is the number of objectives and constraints listed in itemnames. Note that the evaluation of Y is scaled onto [-1 1].

```
Y = evaluate(optimstore, X, itemnames, datasetname)
```

evaluates the specified objectives and constraints at the operating points in the data set specified by the string datasetname. X must be a (Nrows-by-NfreeVar) matrix, where Nrows is the number of rows in the data set.

```
Y = evaluate(optimstore, X, itemnames, datasetname, rowind)
```

evaluates the specified objectives and constraints at the points of datasetname given by rowind. X must be a (NRows-by-NFreeVar) matrix where NRows is the length of ROWIND. ROWIND must be a list of integer indices in the range [1 NumRowsInDataset]. Y is a (Nrows-by-NItems) matrix.

See Also nEvaluate, pevEvaluate

## evaluateConstraint

| Purpose | Evaluate optimization constraints |
| :--- | :--- |
| Syntax | $Y=$ evaluateconstraint (optimstore, $X$ ) | Description | A method of cgoptimstore. |
| :--- |
| $Y=$$Y$ evaluateconstraint (optimstore, $X)$ evaluates all of the <br> optimization constraints at the free variable values $X$. $X$ must be a <br> (NPoints -by - NFreeVar) matrix where NPoints is the number of points <br> to be evaluated and NFreevar is the number of free variables in the <br> optimization. The values of the constraints are returned in $Y$, which is of <br> size (NPoints - by -NItems) where NItems is the number of constraints <br> in the optimization. The evaluation of $Y$ is scaled approximately onto <br> [-1 1]. Negative values of $Y$ imply $X$ is feasible. |

## Examples

See Also evaluateObjective, evaluateNonlcon

| Purpose | Evaluate optimization nonlinear constraints |
| :---: | :---: |
| Syntax | [varargout] = evaluateNonlcon(optimstore, X, ItemNames) |
| Description | Evaluate optimization nonlinear constraints. A method of cgoptimstore. |
|  | $Y=$ evaluateNonlcon(optimstore, $X$ ) evaluates all of the nonlinear constraints in the optimization at the free variable values $X$. $X$ must be a (NPoints-by-NFreeVar) matrix where NPoints is the number of points to be evaluated and NFreeVar is the number of free variables in the optimization. The evaluation of $Y$ is scaled onto [-1 1]. |
|  | $Y=$ evaluateNonlcon(optimstore, X, ItemNames) evaluates the nonlinear constraints specified in the cell array of strings, ItemNames, at the free variable values $X$. The values of the nonlinear constraints are returned in Y , which is of size (NPoints-by-NItems) where NItems is the number of nonlinear constraints listed in ItemNames. |
|  | [ $\mathrm{Y}, \mathrm{YG}$ ] = evaluateNonlcon(optimstore, X, ItemNames) also evaluates the gradient of the specified constraints in YG (if ItemNames is not specified, then the gradient of all constraints is returned). YG is of size NFreeVar-by-NItems-by-NPoints, where NFreeVar is the number of free variables in the optimization. |

See Also evaluateObjective

## evaluateObjective

Purpose Evaluate optimization objectives
Syntax varargout = evaluateObjective(optimstore, X, ItemNames)
Description Evaluate optimization objectives. A method of cgoptimstore.
Y = evaluateObjective(optimstore, X) evaluates all of theoptimization objectives at the free variable values $X$. $X$ must be a(NPoints-by-NFreeVar) matrix where NPoints is the number of pointsto be evaluated and NFreeVar is the number of free variables in theoptimization. The values of the objectives are returned in Y , which is ofsize (NPoints-by-NItems) where NItems is the number of objectives inthe optimization. The evaluation of $Y$ is scaled onto [-1 1].
Y = evaluateObjective(optimstore, X, ItemNames) evaluatesthe objectives specified in the cell array of strings, ItemNames, at thefree variable values $X$. The values of the objectives are returned in $Y$,which is of size (NPoints-by-NItems) where NItems is the numberof objectives listed in ItemNames.
[Y, YG] = evaluateObjective(optimstore, X, ItemNames) also evaluates the gradient of the specified objectives in YG (if ItemNames is not specified, then the gradient of all objectives is returned). YG is of size NFreeVar-by-NItems-by-NPoints, where NFreeVar is the number of free variables in the optimization.

See Also evaluateNonicon

## Purpose Get optimization properties

Syntax $\quad V=$ get (optimstore, 'PropertyName')

Description Returns the value of the specified property in the optimization. A method of cgoptimstore.
get (optimstore) displays all property names and a description of each property for the OPTIMSTORE object.

S = get(optimstore) returns a structure where each field name is the name of a property of OPTIMSTORE and each field contains the description of that property.

Note This method is obsolete. Use the GETXXX methods instead.

See Also See also cgoptimstore/GETXXX, for example getA, getB, etc.

Purpose Get linear inequality constraint matrix.
Syntax
A = getA(optimstore)

Description
Get the linear inequality constraint matrix. A method of cgoptimstore. $\mathrm{A}=$ getA(optimstore) returns the linear inequality constraint matrix used in the optimization. A is a (NLINCON-by-NFreeVar) matrix where NFreeVar is the number of free variables in the optimization and NLINCON is the number of linear inequality constraints.

## See Also <br> getB

Purpose Get linear inequality constraint target values.
Syntax B = getB(optimstore)
Description Get the linear inequality constraint target values. A method ofcgoptimstore.$B=$ getB(optimstore) returns the linear inequality constraint targetvalues used in the optimization. B is a (NLINCON-by-1) column vectorwhere NLINCON is the number of linear inequality constraints.
See Also ..... get $A$

## getConstraints

Purpose Return information about all optimization constraints
Syntax coninfo = getConstraints (obj)

Description Return information about all optimization constraints. A method of cgoptimoptions.
coninfo = getConstraints(options) returns a structure array of information regarding the optimization constraint functions. coninfo(i).label contains the label for the i-th constraint. A string defining the type of the $i$-th constraint is stored in coninfo(i).typestr. The constraint parameters are stored in coninfo(i). pars.

## See Also

addModelConstraint, addLinearConstraint
Purpose Return current usage of constraints
Syntax mode = getConstraintsMode(options)
Description Returns a string describing how the optimization makes constraints available to the user. mode will be one of 'any ' or 'fixed '.
See Also setConstraintsMode

## getDataset

Purpose Retrieve data from data set

```
Syntax \(\quad V=\) getDataset (optimstore, datasetName, inputNames)
```

Description Returns required data from a named data set. A method of cgoptimstore.

PTS = getDataset(optimstore, datasetName) returns all the data from the specified helper data set. If the data set cannot be found, data is returned as empty.

PTS = getDataset(optimstore, datasetName, inputNames) returns data from the specified helper data set. Data is retrieved for the columns of the data set with names that match those in inputNames. If the dataset cannot be found, data is returned as empty.

## Examples

```
V = getdataset(optimstore, 'myDS', {'speed', 'afr'})
```

returns a NPTS by 2 matrix, V .
NPTS is the number of rows in the operating point set labelled 'myDS', $V(:, 1)$ is the data for the variable labelled 'speed ', $V(:, 2)$ is the data for the variable labelled ' afr '.

## See Also addOperatingPointSet

## getDescription

## Purpose Get current description for optimization function

Syntax desc = getDescription(options)

Description A method of cgoptimoptions. Returns the description, desc, of the user-defined optimization function.

See Also setDescription

## getEnabled

Purpose Get current enabled status for optimization
Syntax en=getEnabled(options)

Description A method of cgoptimoptions. Returns whether this user-defined optimization is available to be run. en is set to true or false. When an optimization is disabled, the user can still register it with CAGE but is not allowed to create new optimizations using it.

See Also setEnabled

## Purpose Get optimal values of free variables

```
Syntax
data = getFreeVariables(obj)
```

Description A method of cgoptimstore. Get the optimal values of the free variables. Results = getFreeVariables(obj) returns the matrix of optimal values that has been set for the free variables. Results is a NSOL by NFREEVAR matrix containing many solutions for the optimal values of the free variables. NSOL is the number of solutions and NFREEVAR is the number of free variables.

See Also setFreeVariables

Purpose Return optimization free variable labels
Syntax labels=getFreeVariables(options)

Description A method of cgoptimoptions. Returns the current placeholder labels for the free variables in the optimization. The labels are returned in a (1-by-NFreeVar) cell array, labels, where NFreeVar is the number of free variables that have been added to the optimization.

See Also
addFreeVariable, setFreeVariablesMode, getFreeVariablesMode

# Purpose Return current usage of free variables 

Syntax mode= getFreeVariablesMode(options)

Description A method of cgoptimoptions. Returns a string describing how the optimization makes free variables available to the user. mode is set to any or fixed.

See Also setFreeVariablesMode

## getInitFreeVal

Purpose Get initial free values for optimization
Syntax $\quad x 0=$ getInitFreeVal (cos)

Description Get the initial free values for the optimization. A method of cgoptimstore.
x0 = getInitFreeVal(optimstore) returns the initial values of the free variables used in the optimization. X0 is a ( $1-$ by -NFreeVar) matrix where NFreeVar is the number of free variables in the optimization.

See Also<br>setFreeVariablesMode

## Purpose <br> Get free variable lower bounds

Syntax LB = getLB(optimstore)

Description
Get the free variable lower bounds. A method of cgoptimstore.
LB = getLB(optimstore) returns the free variable lower bounds used in the optimization. LB is a ( $1-$ by-NFreeVar) vector where NFreeVar is the number of free variables in the optimization.

See Also
getUB

Purpose Return linear constraint labels
Syntax conLabels = getLcon(optimstore)

Description Return the linear constraint labels. A method of cgoptimstore. conLabels $=$ getLcon(optimstore) returns the labels for the linear constraints in the optimization. These labels are those found in the CAGE GUI for the optimization linear constraints.

See Also
getObjectives, getNumNonlcon

Purpose Get linear constraint placeholder information
Synfax out = getLinearConstraints(options)

Description A method of cgoptimoptions. Returns a structure array of information regarding the linear constraints in the optimization. The structure has three fields: label, A, and b. See the help for addLinearConstraint for more information on these fields.

See Also
addLinearConstraint, setConstraintsMode

## getModelConstraints

Purpose Get model constraint placeholder information
Syntax out = getModelConstraints (options)
Description A method of cgoptimoptions. Returns a structure array of information regarding the model constraints in the optimization. The structure has three fields: label, boundtype, and bound. See the help for addModelConstraint for more information on these fields.

See Also addModelConstraint, setConstraintsMode
Purpose Get current name label for optimization function
Syntax name=getName(options)
Description A method of cgoptimoptions. Returns the current name label, name, for the user-defined optimization function.
See Also ..... setName

Purpose Get nonlinear constraint information
Syntax out = getNonlCon(obj)

Description Get nonlinear constraint information. A method of cgoptimoptions. out $=$ getNonlinearConstraints(options) returns a structure array of information regarding the nonlinear constraints in the optimization. The structure has three fields: label, type and pars. The label field contains the label used for the constraint in the CAGE GUI. The typestr field contains constraint type selected by the user. The pars field contains any parameters associated with the constraint.

## See Also

getModelConstraints, getLinearConstraints

| Purpose | Return number of nonlinear constraints per label |
| :--- | :--- |
| Syntax | ncon $=$ getNumNonlcon(optimstore) <br> ncon $=$ getNumNonlcon(optimstore, conLabels) |

Description Return the number of nonlinear constraints per label. A method of cgoptimstore.
ncon $=$ getNumNonlcon(optimstore) returns the number of constraints that will be returned from an evaluation of each labelled constraint. For example, consider an optimization that has a sum constraint over a set of points, S , and a point constraint to be evaluated at each member of $S$. NCON will return [1r], where $r$ is the number of points in S.
ncon = getNumNonlcon(optimstore, conLabels) returns the number of constraints type for the defined constraints.

See Also getConstraints, getNumNonlconLabels

## getNumNonlconLabels

Purpose Return number of nonlinear constraint labels
Syntax numlab = getNumNonlconLabels(optimstore)

Description Returns the number of nonlinear constraint labels in the optimization. A method of cgoptimstore.

See Also getNumObjectiveLabels

Purpose Return number of objective labels
Syntax numlab = getNumObjectiveLabels(optimstore)

Description $\quad \begin{aligned} & \text { Returns the number of objective labels in the optimization. A method of } \\ & \text { cgoptimstore. }\end{aligned}$ cgoptimstore.

See Also getNumNonlconLabels

## getNumObjectives

Purpose Return number of objectives per label

```
Syntax
nobj = getNumObjectives(optimstore)
nobj = getNumObjectives(optimstore, objlabels)
```

Description Return the number of objectives per label. A method of cgoptimstore. nobj = getNumObjectives(optimstore) returns the number of objectives that will be returned from an evaluation of each objective label. For example, consider an optimization that has a sum objective over a set of points, $S$, and a point objective to be evaluated at each member of S . nobj will return [ 1 r ], where r is the number of points in S .
nobj = getNumObjectives(optimstore, objlabels) returns the number of objectives that will be returned for the defined objective labels.

## See Also

getObjectives; getObjectiveType

## getNumRowsInDataset

Purpose Get number of rows in optimization data set
Syntax npts = getNumrowsInDataset(optimstore, datasetName)

Description Returns the number of rows in the named data set. A method of cgoptimstore.

## getObjectives

Purpose Return objective labels for optimization
Syntax objLabels = getObjectives(optimstore)

Description A method of cgoptimstore. Returns the labels for the objective functions in optimization. These labels are those found in the CAGE GUI for the optimization objectives.

See Also getLcon

## Purpose Return information about optimization objectives

Syntax objinfo=getObjectives(options)

Description A method of cgoptimoptions. Returns a structure array of information regarding the optimization objective functions. objinfo(i).label contains the label for the $i^{\text {th }}$ objective. A string defining the type of the $\mathrm{i}^{\text {th }}$ objective (max, min, min/max, or helper) is stored in objinfo(i).type.

See Also addObjective, setObjectivesMode, getObjectivesMode

## getObjectivesMode

Purpose Return current usage of objective functions

```
Syntax mode = getObjectivesMode(options)
```

Description A method of cgoptimoptions. Returns a string describing how the optimization makes objectives available to the user. mode will be one of 'multiple', 'any', or 'fixed'.

See Also setObjectivesMode

## getOperatingPointSets

## Purpose <br> Return information about optimization operating point sets

Syntax getOperatingPointSets(options)

Description A method of cgoptimoptions. Returns a structure array of information regarding the optimization operating point sets. The structure has two fields, label and vars. See the help for addOperatingPointSet for more information on these fields.

See Also
addOperatingPointSet, setOperatingPointsMode, getOperatingPointsMode

## getOperatingPointsMode

Purpose Return current usage of operating point sets
Syntax mode=getOperatingPointsMode(options)

Description A method of cgoptimoptions. Returns a string describing how the optimization makes operating point sets available to the user. mode will be one of 'default', 'fixed', or 'any'.

See Also setOperatingPointsMode

## Purpose Return objective type

Syntax
objType = getObjectiveType(optimstore)
objType = getObjectiveType(optimstore, objLabels)

Description Return the objective type. A method of cgoptimstore.
objType = getObjectiveType(optimstore) returns the objective type of all the objectives in the optimization. A 1-by-NOBJ cell array is returned, each element being 'min', 'max' or 'helper'.
objType = getObjectiveType(optimstore, objLabels) returns the objective type for the defined objectives.

See Also
getObjectives

## getOptimOptions

Purpose Retrieve optimization options object
Syntax options = getOptimOptions(optimstore)

Description A method of cgoptimstore. Returns the optimization configuration object. Information about the optimization set up can be retrieved from this object.

## Purpose Get output information for optimization

```
Syntax [exitflag, msg, stats] = getOutputInfo(cos)
```

Description Get output information for the optimization. A method of cgoptimstore.
[exitflag, termMsg] = getOutputInfo(optimstore) returns diagnostic output information from optimstore. exitflag indicates the success (exitflag $>0$ ) or failure (exitflag <=0) of the current optimization run. exitflag may also give some indication why the optimization terminated. Any termination message set by the optimization can be retrieved from termMsg.
[exitflag, termMsg, output] = getOutputInfo(optimstore) returns in addition a structure of algorithm-specific information in output. For output to be non-empty, the user must create it in their algorithm. See the worked example and tutorial for more information on how to create output structures.

## getParam

Purpose Get optimization parameter

```
Syntax
property_value = getParam(obj, propertyname)
```

Description $\quad \begin{aligned} & \text { Get optimization parameter. A method of cgoptimstore. } \\ & \\ & V=\text { getParam(optimstore, 'Parameter_name') returns the value } \\ & \text { of the specified parameter in the optimization. These optimization } \\ & \text { parameters must be set up in the Options section of the user-defined } \\ & \text { script. }\end{aligned}$
See Also addParameter
See the example file mbcOSworkedexample, used in the optimization tutorial "Worked Example Optimization".

| Purpose | Return information about optimization parameters |
| :--- | :--- |
| Syntax | getParameters (options) |
| Description | A method of cgoptimoptions. Returns a structure array containing <br> information about the parameters that are defined for the optimization. <br> Parameter information is returned in a structure with fields label, <br> typestr, value, and displayname. See the help for addParameter for <br> more information on these fields. |
| See Also | addParameter, getParam |

Purpose Get preferred interface to provide evaluation function

```
Syntax ver = getRunInterfaceVersion(obj)
```

Description Get the preferred interface to provide the evaluation function. A method of cgoptimoptions.
ver = getRunInterfaceVersion(options) returns the Model-Based Calibration Toolbox Version that is emulated when the optimization function's evaluate option is called. If ver is set to 2 , the interface provided by the Model-Based Calibration Toolbox Version 2 is activated. If ver is set to 3 , the new interface, which the Model-Based Calibration Toolbox Version 3 defines, is used.

See Also<br>setRunInterfaceVersion

## getStopState

## Purpose Current stop state for optimization

Syntax stop= getStopState(opt)

Description A method of cgoptimstore. stop= getStopState(optimstore) returns the current stop state for the optimization. The stop state could be set by the Stop button on the Running Optimization progress bar or via a call to setStopState within a script.

See Also setStopState

## getUB

Purpose Get free variable upper bounds
Syntax $\quad U B=\operatorname{getUB}($ optimstore $)$

Description A method of cgoptimstore. Returns the free variable upper bounds used in the optimization. UB is a ( $1-\mathrm{by}-\mathrm{NFreeVar}$ ) vector where NFreeVar is the number of free variables in the optimization.

See Also getLB

## Purpose

Grid evaluation of optimization objectives and constraints
Syntax
Y = gridEvaluate(optimstore, X)
Y = gridEvaluate(optimstore, X, objconname)
Y = gridEvaluate(optimstore, X, objconname, datasetname)
Y = gridEvaluate(optimstore, X, objconname, datasetname, rowind)

## Description

## Examples

A method of cgoptimstore.
Y = gridEvaluate (optimstore, X) evaluates all the objectives and constraints at the points X for the current run. This call produces identical results to the equivalent call to cgoptimstore/evaluate.

Y = gridEvaluate(optimstore, X, objconname) evaluates the objectives/constraints specified in the cell array objconname as described above.

Y = gridEvaluate(optimstore, X, objconname, datasetname) evaluates all the objectives and constraints at all combinations of the points in datasetname with $X$. The return matrix, $Y$, is of size $\operatorname{SIZE}(X, 1)-$ by - (NOBJ+NCON) - by -NPTS, where NOBJ is the number of objectives, NCON is the number of constraints and NPTS is the number of rows in P. Further, Y(I, J, K) is the value of the J-th objective/constraint at $X(I,:)$ and $P(K,:) . \quad Y$ is scaled on [-1 1 ].

Objectives: 01, 02

Constraints : C1, C2
Primary data set:

| A | B |
| :--- | :--- |
| 4 | 5 |
| 1 | 3 |

Free variables:

## gridEvaluate

| X1 | X2 | X3 |
| :--- | :--- | :--- |
| 2 | 4 | 8 |
| 1 | 9 | 3 |
| 6 | 2 | 7 |
| $X$ |  |  |

In this case, the following command

```
Y = gridEvaluate(optimstore, X)
```

evaluates objectives and constraints at the following points:

| A | B | $\mathbf{X 1}$ | $\mathbf{X 2}$ | $\mathbf{X 3}$ |
| :--- | :--- | :--- | :--- | :--- |
| 4 | 5 | 2 | 4 | 8 |
| 4 | 5 | 1 | 9 | 3 |
| 4 | 5 | 6 | 2 | 7 |
| 1 | 3 | 2 | 4 | 8 |
| 1 | 3 | 1 | 9 | 3 |
| 1 | 3 | 6 | 2 | 7 |

Y is a 3-by-4-by-2 matrix where
$\mathrm{Y}(:, 1,1)=$ Values of 01 at $\mathrm{A}=4, \mathrm{~B}=5$
$\mathrm{Y}(:, 2,1)=$ Values of 02 at $\mathrm{A}=4, \mathrm{~B}=5$
$\mathrm{Y}(:, 3,1)=$ Values of C 1 at $\mathrm{A}=4, \mathrm{~B}=5$
$\mathrm{Y}(:, 4,1)=$ Values of C 2 at $\mathrm{A}=4, \mathrm{~B}=5$
$\mathrm{Y}(:, 1,2)=$ Values of 01 at $\mathrm{A}=1, \mathrm{~B}=3$
$\mathrm{Y}(:, 2,2)=$ Values of 02 at $\mathrm{A}=1, \mathrm{~B}=3$

## gridEvaluate

```
Y(:, 3,2) = Values of C1 at A = 1, B = 3
Y(:,4,2)= Values of C2 at A = 1, B = 3
    Y = gridEvaluate(optimstore, X, objconname, datasetname, rowind)
```

evaluates the specified objectives/constraints at the points of datasetname given by rowind as described above. $Y$ is a length(rowind) by length(objconname) by npts matrix.

See Also evaluate

## gridPevEvaluate

Purpose Grid evaluation of prediction error variance (PEV)

```
Syntax
[y, ysums] = gridpevevaluate(optimstore, X)
Y = gridpevevaluate(optimstore, X, objconname)
Y = gridpevevaluate(optimstore, X, objconname, datasetname)
Y = gridpevevaluate(optimstore, X, objconname, datasetname, rowind)
```


## Description

See Also pevevaluate

## Purpose Return whether all free variables are scalars

```
Syntax stat = isScalarFreeVariables(optimstore)
```

Description Return whether all the free variables are scalars. A method of cgoptimstore.
stat = isScalarFreeVariables(optimstore) returns TRUE if all the free variables are scalars and FALSE otherwise.

## nEvaluate

## Purpose Natural evaluation of optimization objectives and constraints

## Syntax

[y, ysums] = nEvaluate(optimstore, x)
Y = nEvaluate(optimstore, $x$, itemNames)
$Y=n E v a l u a t e(o p t i m s t o r e, ~ x, ~ i t e m N a m e s, ~ d a t a s e t N a m e) ~$
$Y=n E v a l u a t e(o p t i m s t o r e, ~ x, ~ i t e m N a m e s, ~ d a t a s e t N a m e, ~ r o w i n d) ~$

[^0]| Purpose | Natural evaluation of optimization constraints |
| :---: | :---: |
| Syntax | $Y=$ nEvaluateConstraint(optimstore, $x$ ) <br> $Y=$ nEvaluateConstraint(optimstore, $x$, itemNames) |
| Description | A method of cgoptimstore. |
|  |  optimization constraints at the free variable values x . X must be a (NPoints-by-NFreeVar) matrix where NPoints is the number of points to be evaluated and NFreeVar is the number of free variables in the optimization. The raw values of the constraints are returned in Y , which is of size (NPoints-by-NItems) where NItems is the number of constraints in the optimization. |
|  | $\mathrm{Y}=$ nEvaluateConstraint(optimstore, X , itemNames) evaluates the constraints specified in the cell array of strings, itemNames, at the free variable values $X$. The raw values of the constraints are returned in Y , which is of size (NPoints-by-NItems) where NItems is the number of constraints listed in itemNames. |
| See Also | evaluateObjective, evaluateNonlcon |

## nEvaluateNonlcon

```
Purpose Natural evaluation of optimization nonlinear constraints
Syntax \(\quad y=n E v a l u a t e N o n l c o n(o p t i m s t o r e, ~ x) ~\)
Y = nEvaluateNonlcon(optimstore, x, itemNames)
```

Description Natural evaluation of optimization nonlinear constraints. A method of cgoptimstore.
 optimization nonlinear constraints at the free variable values $X$. $X$ must be a (NPoints-by-NFreeVar) matrix where NPoints is the number of points to be evaluated and NFreeVar is the number of free variables in the optimization. The raw values of the constraints are returned in $Y$, which is of size (NPoints-by-NItems) where NItems is the number of nonlinear constraints in the optimization.
 nonlinear constraints specified in the cell array of strings, itemNames, at the free variable values $X$. The raw values of the constraints are returned in $Y$, which is of size (NPoints-by-NItems) where NItems is the number of nonlinear constraints listed in itemNames.

See Also evaluateObjective; evaluateNonlcon
Purpose Natural evaluation of optimization objectives
Syntax y = nEvaluateObjective(optimstore, x)
Y = nEvaluateObjective(optimstore, x, itemNames)
Description

Natural evaluation of optimization objectives. A method of cgoptimstore.
 optimization objectives at the free variable values $X$. $X$ must be a (NPoints-by-NFreeVar) matrix where NPoints is the number of points to be evaluated and NFreeVar is the number of free variables in the optimization. The raw values of the objectives are returned in Y , which is of size (NPoints-by-NItems) where NItems is the number of objectives in the optimization.
$Y=n E v a l u a t e O b j e c t i v e(o p t i m s t o r e, ~ x, ~ i t e m N a m e s) ~ e v a l u a t e s ~ t h e ~$ objectives specified in the cell array of strings, itemNames, at the free variable values $X$. The raw values of the objectives are returned in $Y$, which is of size (NPoints-by-NItems) where NItems is the number of objectives listed in itemNames.
See Also
evaluateObjective; evaluateNonlcon

Purpose Create/alter optimization OPTIONS structure

Syntax $\quad$| options $=$ optimset (optimstore) |
| :--- |
| options $=$ optimset (optimfunction, optimstore) |
| options $=$ optimset(optimfunction, optimstore) |
| options $=$ optimset( $\ldots$, 'param1', value1, $\ldots$ ) |

Description Create/alter optimization OPTIONS structure. A method of cgoptimstore.
options = optimset(optimstore) creates an optimization options structure that can be used with Optimization Toolbox functions. with the named parameters altered with the specified values. Any parameters specified in the optimization that match (by name) those in the default options structure are copied into options.
options = optimset(oldopts, optimstore) creates a copy of oldopts and copies matching parameters from the optimization into it.
options = optimset(optimfunction, optimstore) creates an options structure with all the parameter names and default values relevant to the optimization function named in optimfunction and then copies matching parameters from the optimization into it.
options $=$ optimset(..., 'param1', value1,...) sets the additional named parameters to the specified values.

## See Also <br> getParam

## Purpose Evaluate prediction error variance (PEV)

$$
\text { Syntax } \quad Y=\text { pevEvaluate (optimstore, } X \text { ) }
$$

## Description Warning

The evaluation of PEV is no longer supported in cgoptimstore and this method will return PEV values of zero (as detailed below) if called.

A method of cgoptimstore.

```
Y = pevEvaluate(optimstore, X, itemnames)
```

returns PEV values of zero for objectives/constraints at the free variable values X . X is a (NPoints-by-NFreeVar) matrix where NPoints is the number of points to be evaluated and NFreeVar is the number of free variables in the optimization.

```
Y = pevevaluate(optimstore, X, objconname, datasetname)
```

returns PEV values of zero for the objectives/constraints at the operating points in the data set specified by the string datasetname.

```
Y = pevevaluate(optimstore, X, objconname, datasetname, rowind)
```

returns PEV values of zero for the specified objectives/constraints at the points of datasetname given by rowind. X must be a (NRows-by-NFreeVar) matrix where NRows is the length of rowind. rowind must be a list of integer indices in the range [ 1 NumRowsInDataset].Y is a (Nrows-by-NItems) matrix.

See Also

## removeConstraint

Purpose Remove constraint from optimization
Syntax obj = removeConstraint (obj, sLabel)

Description Remove a constraint from the optimization. A method of cgoptimoptions.
obj = removeConstraint(options, label) removes the placeholder for the constraint referred to by the string label.

See Also getModelConstraints, getLinearConstraints, addModelConstraint, addLinearConstraint

# Purpose Remove free variable from optimization 

Syntax
obj = removeFreeVariable(obj, sLabel)

Description Remove a free variable from the optimization. A method of cgoptimoptions.<br>options = removeFreeVariable(options, label) removes the placeholder for the free variable referred to by the string label.

See Also
getFreeVariables, addFreeVariable

## removeObjective

Purpose Remove objective from optimization
Syntax obj = removeObjective(obj, sLabel)

Description Remove an objective from the optimization. A method of cgoptimoptions.
options = removeObjective(options, label) removes the placeholder for the objective referred to by the string label.

See Also
getObjectives, addObjective

Purpose
Remove operating point set from optimization
Syntax

Description

See Also

## removeParameter

Purpose Remove parameter from optimization
Syntax obj = removeParameter(obj, sLabel)
Description Remove a parameter from the optimization. A method of cgoptimoptions.Removes the placeholder for the parameter referred to by the stringlabel.
See Also getParameters, addParameter

| Purpose | Set how optimization constraints are to be used |
| :--- | :--- |
| Syntax | options=setConstraintsMode (options, modestr) |

Description A method of cgoptimoptions. Sets the mode that governs how the user can set up constraints for the optimization in CAGE.
When modestr = any, the user can add any number of constraints.
When modestr = fixed, the user can only edit the constraints that are added by the user-defined optimization function.

See Also getConstraintsMode, addModelConstraint, addLinearConstraint

## setDescription

Purpose Provide description for optimization function
Syntax options=setDescription(options, desc)
Description A method of cgoptimoptions. Sets the description for the optimization object to be the string desc.

See Also getDescription

## Purpose Set enabled status for optimization function

```
Syntax options = setEnabled(options, status)
```

Description A method of cgoptimoptions. Sets the optimization function enabled status. status must be true or false. When an optimization is disabled, you can still register it with CAGE but are not allowed to create new optimizations using it.

See Also getEnabled

## setExitStatus

Purpose Set exit status information for optimization
Syntax optimstore = setExitStatus(optimstore, exitflag, termmsg)

Description Set exit status information for the optimization. A method of cgoptimstore.
optimstore = setExitStatus(optimstore, exitflag, termmsg) sets termination status information in the optimstore. exitflag is an integer which determines whether the optimization has terminated successfully. A value of exitflag $>0$ indicates success, and exitflag $<=0$ indicates failure. In any event, a termination message can be passed back to the optimization through termmsg.

## See Also

See the example file mbcOSworkedexample, used in the optimization tutorial "Worked Example Optimization".

Purpose Set optimal values of free variables
Syntax OUT = setFreeVariables(optimstore, results)
Description Sets the optimal values of the free variables, as returned by the optimization, into the optimstore. A method of cgoptimstore.
results is a npts by nfreevar matrix containing the optimal values of the free variables. nsol is the number of solutions and nfreevar is the number of free variables.

Note This function must be called at the end of the optimization for the optimal values to be stored.

See Also getFreeVariables

## setFreeVariablesMode

Purpose Set how optimization free variables are used

```
Syntax options = setFreeVariablesMode(options, modestr)
```

Description A method of cgoptimoptions. Sets the mode that governs how the user is allowed to set up free variables for the optimization in the CAGE GUI.
When modestr = 'any', the user is allowed to add any number of free variables.

When modestr = 'fixed', the user is only allowed to use the number of free variables that are added by the user-defined optimization function.

## See Also

getFreeVariablesMode, addFreeVariable

## Purpose Provide name label for optimization function

Syntax options = setName(options, name)
Description A method of cgoptimoptions. Sets the name label for the optimization object to be the string name.

See Also getName

## setObjectivesMode

## Purpose Set how optimization objective functions are used

```
Syntax options = setObjectivesMode(options, modestr)
```

Description A method of cgoptimoptions. Sets the mode that governs whether the user is allowed to set up objectives for the optimization in the CAGE GUI.

When modestr = 'any', the user is allowed to add any number of objectives.

When modestr = 'fixed', the user is only allowed to edit the objectives that are added by the user-defined optimization function.

When modestr = 'multiple', the user is only allowed to run the optimization if he or she has defined two or more objectives.

See Also getObjectivesMode, addObjective

## setOperatingPointsMode

| Purpose | Set how optimization operating point sets are used |
| :--- | :--- |
| Syntax | options $=$ setOperatingPointsMode (options, modestr) |

Description
A method of cgoptimoptions. Sets the mode that governs how the user is allowed to set up operating point sets for the optimization in CAGE.
When modestr = 'any ', the user is allowed to add any number of operating point sets.

When modestr = 'default', the user is allowed to optionally define a single operating point set to run the optimization over.

When modestr = 'fixed', the number of operating point sets required can be fixed by the optimization function and the user is not allowed to add or remove any using the CAGE GUI.

See Also getOperatingPointsMode, addOperatingPointSet

Purpose Set diagnostic information for optimization

```
Syntax optimstore = setOutput(optimstore, OUTPUT)
```

Description Set diagnostic information for the optimization. A method of cgoptimstore.
optimstore $=$ setOutput(optimstore, OUTPUT) sets diagnostic information for the optimization in optimstore. Any diagnostic information is passed to optimstore through the structure, OUTPUT. See the worked example for an example of creating an OUTPUT structure.

## See Also <br> See the example file mbcOSworkedexample, used in the optimization tutorial "Worked Example Optimization".

## Purpose Set output information for optimization

```
Syntax
optimstore = setOutputInfo (optimstore, exitflag, termmsg, output)
```

Description Sets output information for the optimization in optimstore. A method of cgoptimstore.

The following information is set:

- exitflag: integer value status flag indicating why the optimization has terminated. exitflag $>0$ implies that the optimization has terminated successfully.
- termmsg: Message that is displayed at termination of algorithm. Normally used for error messages.
- output: Structure of algorithm statistics for the optimization.

Note This method is obsolete. Use cgoptimstore/setExitStatus and cgoptimstore/setOutput instead.

## See Also

```
setExitStatus, setOutput
```


## setRunInterfaceVersion

## Purpose Get preferred interface to provide evaluation function

```
Syntax obj = setRunInterfaceVersion(obj, ver)
```

Description Set the preferred interface to provide the evaluation function. A method of cgoptimoptions.

Sets the Model-Based Calibration Toolbox Version that is emulated when the optimization function's evaluate option is called. If ver is set to 2 , the interface provided by the Model-Based Calibration Toolbox Version 2 is activated. If ver is set to 3 , the new interface, which the Model-Based Calibration Toolbox Version 3 defines, will be used.

The interface version that the current version of Model-Based Calibration Toolbox runs is superior in its capabilities, however it does contains some backwards incompatibilities with the interface used in version 2. You can use this function in old Model-Based Calibration Toolbox optimization files that fail to work with the newer interface.

[^1]
## Purpose Set current stop state for optimization <br> Syntax setStopState (opt, stop)

Description
Set current stop state for optimization. A method of cgoptimstore.
stop $=$ setStopState(optimstore, stop) sets the current stop state (TRUE or FALSE) for the optimization. Note that this command does not stop an optimization, the optimization script must do this.

See Also getStopState

## Data Sets

This section includes the following topics:

| Data Sets Views (p. 7-2) | How to use the Data Sets views. |
| :--- | :--- |
| Setting Up Data Sets (p. 7-4) | How to set up data sets by importing <br> experimental data, importing data <br> from tables, specifying factors <br> manually, and creating a factor from <br> the error between factors. |
| Viewing Data in a Table (p. 7-11) | How to use the data table view. |
| Plotting Outputs (p. 7-13) | How to use the plot view. |
| Using Color to Display Information | How to use color plots and restrict the <br> color to display factor information. |
| (p. 7-16) | How to link factors. |
| Linking Factors in a Data Set |  |
| (p. 7-20) | How to assign columns of data to <br> input factors, for example, in order <br> to compare experimental data with <br> tables or models. |
| Assigning Columns of Data (p. 7-22) |  |
| Manipulating Models in Data Set | How to change models from input to <br> output factors. |
| View (p. 7-23) | How to fill tables from data, <br> including creating rules. |
| Filling Tables from Experimental |  |
| Data (p. 7-24) |  |

## Data Sets Views

The Data Set view has these main functions:

- Validating calibrations with experimental data
- Filling tables by reference to a set of experimental data
- Constructing operating point sets for running optimizations
- Investigating optimization results and using them to fill tables

For worked examples about data sets, see the Getting Started tutorials.
Data Sets consists of four views. These views display different aspects of the data set. Each view is accessible from the View menu or by clicking the appropriate button on the toolbar.


## - Factor Information

List of all available project expressions, which can be added to the data set for display and evaluation.

- View Data

Displays the data in a table. Individual entries can be altered. Columns of data can be assigned to CAGE expressions.

## - Plot Outputs

Displays models and features evaluated at the data points (of the data set).

## - Fill Table from Data Set

This mode allows you to fill tables by reference to experimental data.


## Setting Up Data Sets

The Data Sets view displays the strategies, tables, and models, etc., as a list of factors in the default Data Set Factors view. You can also display the same factors as columns in a grid, with all factors displayed as columns in the list, by selecting the View Data toolbar button ( $\mathrm{Tl}_{\text {) }}$ ). The data set works over a grid of values, which is not necessarily the same as the normalizers of any included tables in the data set.

You have to set the input factors and their values to define the grid in the data set. You can do this in one of three ways:

- Import experimental data. (See "Importing Experimental Data" on page 7-4.)
- Import the values from a table in your CAGE session. (See "Importing Data from a Table in Your Session" on page 7-6.)
- Specify the factors and their values manually. (See "Specifying the Factors Manually" on page 7-7.)

The next sections describe each of these in detail.

## Importing Experimental Data

You can import experimental data to a data set, either to validate a calibration or to use it as the basis for a calibration.

You can import data that is stored in the following formats:

- Microsoft Excel spreadsheets
- Comma-separated value files
- MAT-files


## Importing from Excel or Comma-Separated Value

When you import data from either a Microsoft Excel spreadsheet or from a comma-separated value file, you must ensure that the data is organized in the following manner:

- The first column can either be row markers (text) or entries (numbers).
- The first row can either be column headers (text) or entries (numbers).
- All the other row and column entries must be numbers.


## Importing from MAT-files

When you import from a MAT-file, you must ensure that the file contains numbers only, that is, a double array.

To import experimental data,

## 1 Select File -> Import -> Data.

2 In the file browser, select the correct file to import.

## This opens the Data Set Import Wizard.

3 Discard any columns of data you do not want to import by selecting the column and clicking the button shown.

## $x$

4 Click Next.
The following screen asks you to associate variables in your project with data columns in the data.

5 Highlight the variable in the Project Assignments column and the corresponding data column in the Data Column, then click the assign button, shown.


6 Repeat step 5 until you are satisfied that you have associated all the variables and data columns. Any unassigned data columns are treated as output factors.


7 Click Finish to close the dialog box.
This imports your data into the data set. When you have imported your data, you can view your data set.

## Importing Data from a Table in Your Session

To import data from a table,

## 1 Select Data -> Import -> Import from Table.

If your data set is not empty, a dialog box asks whether you want to Fill the data set from the table or Overwrite the data set from the table. Select Fill to use the table values to fill the factors in your data set. Select

Overwrite to disregard all factors in your data set and fill the data set with the input and output factors from the table. A dialog box opens.

2 Select the correct table from your session to import and click OK.
When you have imported your data, you are ready to view the data set.

## Specifying the Factors Manually

1 Select the Data Set view by clicking the large Data Sets button in the Data Objects pane.

2 Add a data set to the project by selecting File -> New -> Data Set.
3 Select the factors. (See "Selecting the Factors" on page 7-7.)
4 Build the grid. (See "Manually Setting Values of the Input Variables" on page 7-9.)
Once you have completed these steps you can view the data set.
This section describes

- "Selecting the Factors" on page 7-7
- "Manually Setting Values of the Input Variables" on page 7-9


## Selecting the Factors

Clicking the Factors View button in the toolbar ( 原 ) . This displays two list boxes.

- The upper list shows all factors within the data set. You can sort factors by clicking the column headings.
- The lower list shows CAGE project expressions.


You can use this view to add factors to or remove factors from the data set.
To add a factor to a data set,

- Right-click a factor and select Add to Data Set from the context menu.
- Alternatively, select the factor or factors that you want to add to the data set from the list in the lower Project Expressions pane, then select Data $>$ Factors > Add to Data Set.

To make multiple selections, use the standard Shift+click or Ctrl+click.
To remove a factor from a data set,
1 Select the factor or factors that you want to remove from the data set.

2 Right-click and select Remove from Data Set, or select the menu item Data -> Factors -> Remove From Data Set.

Note Links between the two lists are always preserved, so clicking load in the upper list also selects load in the lower list. In other words, you can copy or remove from either list and the relevant results appear in both.

## Manually Setting Values of the Input Variables

## Clicking the Build Grid toolbar button ( $⿻$ () or selecting Data -> Build Grid

 enables you to set the values of the input variables for the data set.To build a full factorial grid,

## 1 Select Data -> Build Grid.

2 Select the factor that you want to define a grid for.
3 Set the grid for the factor.
To set a grid of $5,10,15,20,25,30$, input the following: 5:5:30, where the first number is the minimum, the second is the step size, and the last number is the maximum value.

4 Check the size of the data set in the pane. The current size reported at the bottom of the dialog is the size if you click Cancel to leave the data set unchanged. The projected size is created if you click OK. In the following example, the projected size of 45 you can see is obtained by multiplying the number of points for each factor with a grid (in this case, $3 * 5 * 3$ ).

5 Select the next factor that you want to define a grid for.
6 When you have set the grids for all the factors, click OK.


## Creating a Factor from the Error Between Factors

To create a factor that is the difference between two other factors,
1 Highlight the two factors, using Ctrl+click or Shift+click.
2 Select Create Error from the right-click menu on either column head.
This creates a new factor that is the difference between the two other factors.

## Viewing Data in a Table

Click the View Data button（ ${ }^{(\mathbb{T}}$ ）in the toolbar or select View－＞Data to display the data in tabular form and a list of the current items in the project．

Note that this view is only enabled if you have a grid of points at which to evaluate and display the models and variables．This grid is not necessarily derived from the normalizers of any tables included in the data set．You can set the grid by importing experimental or table data，or by using the Build Grid toolbar button（母）．See＂Setting Up Data Sets＂on page 7－4．

|  |  | Inputs to the selected column，colored cream |  |  | Input that is not an input to the selected column |  | Selected column |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 禺口 | 淢 load | 军－atr | 淢 spk | nmeas | tameas | ［7）Torque：Model | 7 Torque：Strategy |
| 1 | 2235 | 0.549 | 9.5 | 0.1 | 2247 | 66.7 | 71.666 | 66.079 |
| 2 | 3591 | 0.454 | 13.2 | 0.1 | 3613 | 54.1 | 47.163 | 46.89 |
| 3 | 4946 | 0.651 | 12 | 0.1 | 4974 | 73.7 | 47.573 | 79.256 |
| 4 | 881 | 0.648 | 11.9 | 5.7 | 881 | 75.8 | 99.23 | 80.21 |
| 5 | 2234 | 0.441 | 13.3 | 0.1 | 2247 | 55.9 | 51.256 | 45.15 ． |
| 6 | 3591 | 0.747 | 10.9 | 0.1 | 3612 | 90 | 92.837 | 105．586 |
| 7 | 4947 | 0.541 | 9.7 | 0.1 | 4973 | 62.8 | 57.76 | 57．58\％ |
| 8 | 881 | 0.622 | 9.9 | 0.1 | 884 | 72.1 | 76.198 | 60.926 |
| 9 | 1219 | 0.333 | 14 | 0.1 | 1224 | 41.8 | 33.226 | 21.31 G |
| 10 | 1558 | 0.382 | 12 | 0.1 | 1567 | 49.4 | 40.487 | $31.95 \%$ |
| 11 | 1896 | 0.209 | 10.7 | 3.3 | 1906 | 28.5 | 3.492 | 4．19： |
| 12 | 2234 | 0.284 | 9.8 | 3.2 | 2245 | 36 | 23.063 | 19.89 |
| 13 | 2574 | 0.407 | 13.4 | 3 | 2588 | 49.9 | 49.629 | 44.794 |
| 14 | 2914 | 0.595 | 11.5 | 3.1 | 2929 | 70.5 | 84.68 | 82.229 |
| 15 | 3251 | 0.781 | 12.3 | 3.1 | 3268 | 90.5 | 117.424 | 117.259 |
| 16 | 3589 | 0.668 | 13.5 | 3 | 3608 | 77.1 | 87.987 | 96.406 |
| 17 | 3930 | 0.452 | 11.9 | 3.1 | 3952 | 52.7 | 46.511 | 51.72 |
| 18 | 4268 | 0.235 | 10.9 | 3 | 4293 | 27.7 | 5.253 | 3.08 |
| 19 | 4606 | 0.194 | 12 | 3.2 | 4633 | 21.3 | －2．088 | －5．77 |

Columns are color coded by factor type：
－Input factors are white．
－Output factors are gray．

Selecting an output column highlights the input columns associated with it by turning the header cells cream.

Standard editing facilities are available. Double-click an input cell to edit the value.

Cut and paste using the desktop clipboard. Cells, columns, and rows can be copied directly to and from other applications (for example, Excel).

Note You can only edit input values, not output values.

## Plotting Outputs

Use this to plot the outputs of your data sets.
To view a plot,

2 Select an expression from the list to view.
A plot of the selected output factor appears in the top pane.


3 Use the pop-up menus below the plot to change the factors displayed.

To zoom in on an area of interest,

- Press both mouse buttons simultaneously and drag a rectangle; double-click the graph to return to full size.


## Plotting Multiple Selections

You can plot a multiple selection by using standard Ctrl+click and Shift+click operations.

A legend at the top of the screen displays the key to the graph.

## Multiple Plot Outputs



When exactly two items are displayed, further plot options are available:

- Plot the first item against the second item (X-Y Selection).
- Display the error using one of the following options:
- Error
- Absolute error
- Relative error (\%)
- Absolute relative error (\%)


## Using Color to Display Information

You can use the plot view to display more information by coloring the plots.
1 Select View > Plot or click
2 Highlight the correct expression in the Output Expressions (Project and Data Set) pane.

3 Select Color by Value from the right-click menu of the plot.
4 Select from the pop-up menu the variable you want to use to color the plot.


In the following figure, you can see

- A plot of the Sum vs Data Set Point (this is the strategy from a torque feature calibration).
- The points are colored by load.
- For this example it can be seen that, in general, the higher the load, the higher the value of torque.



## Restricting the Color

You might be interested in only part of the display; for example, you might only be interested in points with a low engine speed. The various display options enable you to color only the points that you are interested in.

To restrict the color,
1 Select the Limit range box, or right-click the plot and select Limit Color Range.

Three limit markers appear in the color bar. The colors in the color bar are compressed within the limit markers. This increases the range of colors over the range you are interested in (between the limits), making it easier to see the distribution of points.

2 Adjust the maximum, midpoint, and minimum of the range by dragging the limit markers on the color bar.

3 Examine the data points and those that are outside the range.
Use the right-click menu to alter the view of the points outside the range:

- Select Exclude to remove all points outside the limits from the display.
- Select Color Outside Limits to display all points in color, including those outside the limits. Points outside the limits are still colored, but only dark red or dark blue, depending on which end of the range they are.
- Select No Color Outside Limits to display the points as in the example shown. Points outside the limits are plotted as empty circles.



## Linking Factors in a Data Set

A factor can be linked to another. The factor then takes on the values of that other factor, overwriting the original values.

For example, you might want to link a variable spark with a model for maximum brake torque (MBT) to evaluate a torque model.

To link two factors,
1 Select Data -> Links. This opens a dialog box.
2 Select the data set factor that you want to overwrite.
CAGE generates a list of factors that you could possibly link to the selected factor. (For example, you cannot link to a factor that depends on the selected factor.)

3 Select the factor that you want to link the selected factor with.
4 Click to link the two factors.


CAGE then overwrites the data set factor with the link.

To break a link and return to normal evaluation, click
Once all the links have been created or broken as you want, click OK to exit the dialog.

See also:

- "Setting Up Data Sets" on page 7-4


## Assigning Columns of Data

To analyze imported data, you need to assign columns of data to input factors in the CAGE data set.

Data can be imported into a data set from outside CAGE, for example, from an engine test cell. In many cases, this data contains a set of input points (or operating points) and the values of important measurable variables at those points. To compare data like this with models (and/or tables) in a CAGE data set, you have to assign columns of the data to the corresponding input factors in the data set.

To assign data,

## 1 Select Data > Assign.

2 In the dialog box, highlight the column that you want to assign and the variable that you want to assign it to.

3 Click
 to assign.

To unassign data,
1 Select Data > Assign.
2 In the dialog box, highlight the variable that you want to unassign.
3 Click $\xrightarrow{\bullet}$ to unassign.

Note Assigning data to a CAGE expression overwrites that expression in the data set. This does not affect the expression in the other parts of the CAGE project.

## Manipulating Models in Data Set View

A model in a data set can be treated as either an input or an output. This is particularly useful when a model is used as an input to another model and you want to view specific values of the input model. For example, linking a model of MBT Spark to a Spark model allows the evaluation of a TQ model at MBT.

To change a model to an input,
1 Highlight the desired model in either the factor view or the table view.
2 Select Treat as Input from the right-click menu.
To revert a model to an output,
1 Highlight the desired model in either the factor view or the table view.
2 Select Treat as Output from the right-click menu.

## Filling Tables from Experimental Data

Any table in the project whose axes (normalizers) exist as factors in the data set can be filled from imported experimental data (or any data set, such as optimization output).

CAGE extrapolates the values of the experimental data over the range of your table. Then it fills the table by selecting the values of the extrapolation at your breakpoints.

To fill the table with values based on the experimental data,
1 To view the Table Filler display, click (Fill Table From Data Set) in the toolbar; or select View > Table Filler.

You can use this display to specify the table you want to fill and the factor you want to use to fill it.

2 In the lower pane, select the table from the Table to fill list. This is the table that you want to fill.

3 Select the experimental data from the Factor to fill table list. This is the data that you want to use to fill the table.

For example, see the following display.


The upper pane displays the breakpoints of your table as crosses and the operating points where there is data as blue dots. Data sets display the points in the experimental data, not the values at the breakpoints. You can inspect the spread of the data compared to the breakpoints of your table before you fill the table.

4 To view the table after it is filled, make sure the Show table history after fill box at the bottom left is selected. This is selected by default.

5 To fill the table, click Fill Table.

If the Show table history after fill box is selected, the History dialog box opens, similar to the one shown.


6 Click Close to close the History dialog box and return you to the Table Filler display.

7 To view the graph of your table, select Data $>$ Plot $>$ Surface .


This display shows the table filled with the experimental points overlaid as purple dots.

## Creating Rules

You can ignore points in the data set when you fill your lookup table.
By defining a region to include or exclude such points, you create a rule for the table filling.

For example, you might want to fill a lookup table that has a range of operating points that is smaller than the range of the experimental data.

To ignore points in the data set,
1 Select Data $>$ Plot $>$ Data Set. This displays the view of where the breakpoints lie in relation to the experimental data.

2 To define the region that you want to include, left-click and drag the plot. For example, see the following display.

This region defines a rule in the Table filling rules pane.


3 To fill the table based on an extrapolation over these data points only, click Fill Table.

The display of the surface now shows the table filled only by reference to the data points that are included in the range of the table.

You can now review your data set using the options in the View and Plot panes of Data Sets.

You can add any number of rules to follow when filling tables. For example, you might be aware that a particular test run included in the chosen area is not good data. You can click and drag to enclose any chosen point, then right-click that rule (in the Table filling rules pane) and select Exclude Points. You can set any number of rules to make sure you fill the table by using just the points you are interested in.

## Right-Click Options

Select Data -> Table Fill to reach the following options:

- Enable Rule: Apply the rule to the data.
- Disable Rule: Do not apply the rule, but also do not delete it.
- Exclude Points: Do not include these points in table filling.
- Include Points: Include points in table filling.
- Promote Rule: Change order of rules.
- Demote Rule: Change order of rules.
- Clear Rule: Delete this rule.

You can use these options to enable an iterative process. You can fine-tune the selection of data points: try different selections of data to fill your tables, check the results, then reuse the same rules for the same or different tables.

## Surface Viewer

This section includes the following topics:
The Surface Viewer in CAGE (p. 8-2) Introduction to the Surface Viewer.
Viewing a Model or Strategy (p. 8-3) How to view models or strategies.
Setting Variable Ranges (p. 8-5) How to set ranges for display.
Displaying the Model or Feature This section describes the display (p. 8-7)

Making Movies (p. 8-14)
Displaying Errors (p. 8-16)

Printing and Exporting the Display How to print and export displays. (p. 8-18)

How to display errors: predicted error of the model and the error between a model and a strategy (feature error). options available: surface, contour, single line, single value, multiline, movie, or table.

## The Surface Viewer in CAGE

The Surface Viewer enables you to view the model or the feature as it varies over the ranges of its variables. You can automatically step through values of a variable, to make a movie of the behavior of the feature or model. You can view the model or feature using a variety of plot types.

Note The Surface Viewer is only available when you are viewing models, tradeoffs or the feature node of a feature calibration.

Following is an example of the Surface Viewer displays.

| - Surface Viewer |  |  | - [-ㅁ] $x$ |
| :---: | :---: | :---: | :---: |
| File View Tools Window Help |  |  |  |
|  |  |  |  |
| Item | $\triangle$ | Project/TQ_N804_L13 | Project/NOEMISS_N804_L13 |
|  |  |  |  |
| Data to plot |  |  |  |
| Plot type | Surface $\square$ |  | SPK $50{ }^{\circ} 0$ EGR |
| Surface 1 He ... Strategy $\quad \square$ |  |  |  |
| Surface 1 Sh... ${ }^{\text {None }}$ |  | Project/MCEMMISS_N804_L13 | Project/SOOT_N804_L13 |
| Surface 2 He ... NoneMark poirts outside boun |  |  |  |
| Inputs |  |  | -9 - |
| X-axis: <br> Y-axis: | $x$ $\square$ <br> $x$ $\square$ |  |  |
| Name | Value |  | SPK |
| $\times$ | streetorm vectors |  |  |
| Ready |  |  |  |

## Viewing a Model or Strategy

To access the surface viewer, select Tools > Surface Viewer or click on the toolbar.

These are the main steps to view the model or feature using the Surface Viewer dialog box:

1 The model or feature selected when you open the Surface Viewer is displayed in the plot. If you have more than one model or feature, select what to display from the top Items list.

You can multiselect up to 4 items at once using Ctrl+click (the plot view on the right divides into a maximum of 4 plots). All the settings below the Items list apply to all plots. If one of the features selected in the Items list does not contain the appropriate input variables you select to plot, there will be no plot for that item.

2 Select the ranges for the variables. (See "Setting Variable Ranges" on page 8-5.)

3 Choose the plot type to display. (See "Displaying the Model or Feature" on page 8-7.). You can view surfaces, contour plots, single and multilines, movies, tables, and single values.

For example, as you view a feature, you can view either the strategy, the model associated with that feature, the error between the model and the strategy, or the prediction error if the model was imported from the Model Browser. You can also use one of these factors to shade the surface formed by one of the other factors, and you can select any two factors to display simultaneously as two surfaces.

- You can make a movie. (See "Making Movies" on page 8-14). This enables you to view the model or feature as it steps through several values of a variable. For example, if you want to view a feature calibrated for maximum brake torque (MBT) as it varies over exhaust gas recycling (EGR), you can make a movie of the feature.
- You can also print or export the display. (See "Printing and Exporting the Display" on page 8-18.)



## Setting Variable Ranges

The Surface Viewer does not work over continuous ranges, only at discrete points. You must specify, for the model or feature, the discrete points you want to include in the display. You can display models or features over a range of points. To edit the displayed values of a variable, double-click in the value box for the appropriate variable.

- Variables not being used for the axes plotted have a single value for that plot; to edit the displayed value for these variables you can type directly into the edit box after double-clicking.
- For variables specified by the axes drop-down menus, the value box displays the range over which that variable is plotted and the number of points plotted across that range. To edit both the range and the number of points, double-click the value box. The Value Editor opens.

| Walue Editor |  |  |  | $x$ |
| :---: | :---: | :---: | :---: | :---: |
|  | Min | Max | num |  |
| © Uniform vector | 500.0 | 6500.0 | 31 |  |
|  | (use spaces or tabs to separate entries) |  |  |  |
| $\bigcirc$ Freeform vector | 05700.05900 .06100 .06300 .06500 .0 |  |  |  |
|  | OK |  | ncel |  |

Here you can indicate the points to include in the display. You can specify

- The minimum and maximum values and the number of points across that range by choosing Uniform Vector and typing in the edit boxes Min, Max, and Number of points.
- Each discrete point at which you want to evaluate the model (or feature), by choosing Freeform vector, and then typing the required values.
For example, if you want to display the variable $x$ at $0,1,7,30$, and 50 , enter the following in the Freeform vector edit box, separated by tabs or spaces:

$$
0173050
$$

Click OK to apply your changes to the plot.

When you alter the variables, you can select whether you want the display to update automatically or not. You can toggle the automatic update on and off by selecting Tools > Auto-Evaluate. When you want to update the display, select Tools > Evaluate Now . Both of these options have equivalent toolbar buttons:

```
+ =-
```


## Displaying the Model or Feature

The Plot Type drop-down menu gives the options on how to display the model or feature, as shown below.

| Plot type: | Surface |
| :--- | :--- |
|  | Surface |
|  | Contour <br> Line <br> Single Value <br> Mutiline <br> Movie <br> 2-D Table <br> 1-D Table |

Use the options in this menu to display the model or feature in the following ways:

- "Surface" on page 8-8
- "Contour" on page 8-10
- "Line" on page 8-11
- "Single Value" on page 8-11
- "Multiline" on page 8-12
- "Table" on page 8-12
- Movie. See "Making Movies" on page 8-14.

When plotting multiple models or features, it can be useful to link axes rotation or use common Y- or Z- ranges. Use the display options (toolbar button or View menu).

In any of these views you can select View > Statistics, or click the equivalent toolbar button. This opens a dialog box with a list of the summary statistics (mean, standard deviation, maximum, or minimum) of your currently selected model, strategy, or error for the current display.

For the plots (not movie, single value or tables) you can use the File menu or toolbar to print, copy to clipboard or print to figure. You can also export plot values to CSV file. See "Printing and Exporting the Display" on page 8-18.

You can alter display options for all plots (not value or tables) with the View menu or toolbar button.

## Surface



You can rotate the surface plots by left-clicking and dragging.
If you are using the surface viewer to view a feature, you can choose the following options to display:

- Model
- Strategy
- Prediction Error
- Error (between the model and the strategy)

When viewing models there are no strategy options. You can choose these options from the drop-down menus for Surface 1 Height, Surface 1 Shading, and Surface 2 Height, as illustrated below.


You can view any of these options alone as a primary surface (by leaving the last two options set to None). You can add a second option to shade the primary surface, for example to color your model surface with the error between the model and the strategy, to highlight problem areas.

When you choose to shade a primary surface, a color bar appears to the right of the plot to show you the scale. You can change the maximum and minimum values of the shading factor by typing in the edit boxes above and below the color bar. You can see an example like this in "Viewing a Model or Strategy" on page 8-3.

You can add a second surface to display any two of the options simultaneously, for example, your model and your strategy.

If you have a boundary model, you can display the boundary by selecting the check box.

Select the Inputs to plot from the $\mathbf{X}$-axis and $\mathbf{Y}$-axis drop-down lists, and specify the ranges of inputs in Value controls. See "Setting Variable Ranges" on page 8-5.

Note For information on the two different error displays available using the surface view, see the next section, "Displaying Errors" on page 8-16.

## Contour



You can specify where you want contours by clicking Set Contour Values. Use the check box to return to automatic contour value selection. You can also control number of contours, filling and labels in the display options (toolbar or View menu).

You can enable Cursor Mode (use the View menu or toolbar button) and then click on the plot lines to display the values at a point (plotted with an X). The values are shown in the status bar.

## Line



A line plot - you can display up to three different lines (strategy, model, prediction error and error between the model and strategy). Use the Line drop-down lists to select what to plot. You can select the check box to clip to a boundary if available.

You can enable Cursor Mode (use the View menu or toolbar button) and then click on the plot lines to display the values at a point (plotted with an X). The values are shown in the status bar.

## Single Value

This displays the value of the model, strategy, prediction error or error at the point you have specified in the variable value boxes.

## Multiline



Select the variables to plot from the $\mathbf{X}$-axis and Line colors drop-down menus. Control the number of lines by altering the Values. You can use the check box to clip to a boundary if available.

You can enable Cursor Mode (use the View menu or toolbar button) and then click on the plot lines to display the values at a point (plotted with an X). The values are shown in the status bar.

Table

| Project/Branch 1/Fn_Feature |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| xiy | 0.000 | 0.500 | 1.000 |  |
| -5.000 | 35.000 | 33.776 | 30.403 | $\triangle$ |
| -4.500 | 30.250 | 29.026 | 25.653 |  |
| -4.000 | 26.000 | 24.776 | 21.403 |  |
| -3.500 | 22.250 | 21.026 | 17.653 |  |
| -3.000 | 19.000 | 17.776 | 14.403 |  |
| -2.500 | 16.250 | 15.026 | 11.653 |  |
| -2.000 | 14.000 | 12.776 | 9.403 |  |
| -1.500 | 12.250 | 11.026 | 7.653 |  |
| -1.000 | 11.000 | 9.776 | 6.403 |  |
| -0.500 | 10.250 | 9.026 | 5.653 |  |
| 0.000 | 10.000 | 8.776 | 5.403 |  |
| 0.500 | 10.250 | 9.026 | 5.653 |  |
| 1.000 | 11.000 | 9.776 | 6.403 |  |
| 1 ron | 11900 | 11.000 | Torn |  |

You can select a 2-D or 1-D table to display. Select the check box to mark cells outside the boundary.

Choose variables to be the axes of your table and set the range and number of points in the same way as for all the plots. Set single values for any other variables. For more information, see "Setting Variable Ranges" on page 8-5.

For 2-D tables you can use the Cell values drop-down menu to select whether to display the model output or the prediction error.

For 1-D tables you can select what to display in columns 1, 2 and 3: Model, Prediction error, Strategy or Error (strategy model) (for features), or choose None for 2 and 3 to display only a single column. When viewing models there are no strategy options.

## Making Movies

How to make a movie that allows you to see an evaluation over two variables at successive values of a third variable.

Choose Movie from the Plot Type drop-down menu in the Data to Plot pane.


The movie option allows you to see an evaluation over two variables at successive values of a third variable. For example, a model of torque might have speed (N), load (L), and air/fuel ratio (A) as inputs.

The movie option allows you to view how the torque model behaves over the ranges of speed and load for successive values of air/fuel ratio.

1 Select three variables from the $\mathbf{X}$-axis, $\mathbf{Y}$-axis, and Time drop-down menus, to indicate which variable you want to display. You can view the model surface plotted across the range of two variables, and define the third variable as "time" to see the model surface change across the third variable's range.

2 Define the variable ranges using the Value boxes for the inputs. See "Setting Variable Ranges" on page 8-5.

3 Select the check box to mark boundaries if available.

## 4 Click Play.

5 You can click the buttons at each end of the progress bar under the plot to step through the movie, or click anywhere along the bar (or click and drag the blue pointer) to display a particular point in the movie. You can rotate the plot (including during play).

## Displaying Errors

There are two different error displays available in the surface display options for primary and secondary surfaces and surface shading:

- Error between the model and the strategy (See "Feature Error Data" on page 8-16 following.)
- Prediction error of the model (See "Prediction Error Data" on page 8-16.)


## Feature Error Data

When you are viewing a feature, this displays the error between the strategy and the model.

To display the error, select Error (strategy-model) from the drop-down menu for primary or secondary surface. You can also choose to shade your primary surface with the error by using the Surface 1 Shading menu.

To view the error statistics, select View > Statistics. This opens a dialog box with a list of the summary statistics for the error between model or feature.

## Prediction Error Data

If the model is imported from the Model Browser, it is possible to display the prediction error (PE) data.

Prediction Error Variance (PEV) is a very useful way to investigate the predictive capability of your model. It gives a measure of the precision of a model's predictions. PEV can also be examined in the Model Browser, both in the Prediction Error Variance Viewer and to shade surfaces in the Model Selection and Model Evaluation views. Here you can examine the PEV of designs and models. When you export the model to CAGE you can see this data in the Surface Viewer in the Prediction Error option. See the Model Browser GUI Reference and Technical Documents for details about the calculation of Prediction Error.

## Viewing the Prediction Error

Select Prediction Error from the drop-down display menus for primary or secondary surfaces. You can also choose Prediction Error to shade your primary surface. As with all other plots, you can view the statistics for the Prediction Error displayed by selecting View > Statistics. The mean, standard deviation, and so on are calculated over the range specified in the variable value boxes.

## Printing and Exporting the Display

To print the display, select File -> Print, or you can select Print to Figure. Selecting File > Copy to Clipboard copies the plot image to the clipboard. This is useful if you want to place plot images into other applications. These print options also have equivalent toolbar buttons.

You can also export the display data to a comma-separated variable file.
To export the display, select File > Export to CSV. The currently selected option is exported. The primary input to the first plot is exported (this is the top left if you have multiple plots). The output is the values at the grid of points specified by the current ranges and input values. The inputs for shading and secondary surfaces are not exported.

Note that you cannot print table plots, but you can click and drag to select cells and press Ctrl-C to copy the values to the clipboard, or you can export them to CSV files and then load them into Excel.

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[^0]:    See Also evaluate

[^1]:    See Also
    getRunInterfaceVersion

